



# EM modeling and power cables

Sven Nordebo

Department of Physics and Electrical Engineering  
Linnæus University, Sweden

# Outline

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## Research activities

Electromagnetic losses in three-phase power cables

On the natural modes of helical structures

# Previous and planned research activities

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## Previous research activities

- ▶ VR-ABB-PhD: Electromagnetic dispersion modeling and analysis for power cables. Broadband pulse propagation on HVDC power cables, for fault localization, length estimation, etc.

## Current and planned research activities within the SSF-project: *Complex analysis and convex optimization for EM design*

- ▶ SSF-ABB-PhD: Electromagnetic losses in cable armour. Characterization, measurements and estimation of the induced conduction and hysteresis losses in the cable steel armour.
- ▶ SSF-ABB-mobility: Electromagnetic losses in three-phase power cables. On the natural modes of helical structures.

# Outline

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Research activities

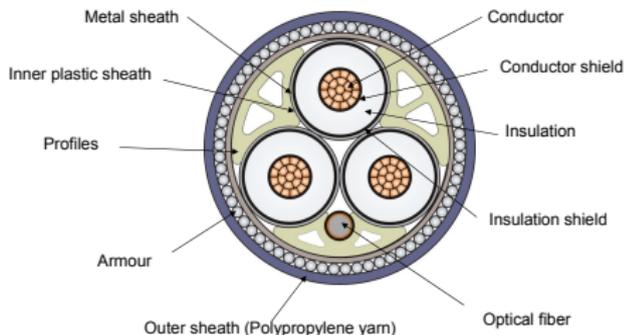
**Electromagnetic losses in three-phase power cables**

On the natural modes of helical structures

# Electromagnetic losses in three-phase power cables

There is a great potential of accurate electromagnetic modeling, analysis, and optimization (design) of three-phase power cables, with regard to

- ▶ conductor losses, skin-effect
- ▶ induced conduction losses in metal sheaths and armour
- ▶ iron losses in armour (hysteresis losses)



Images from: Workshop on Mathematical Modelling of Wave Phenomena 2013, Linnæus University.

Presentation by Danijela Palmgren: [http://lnu.se/polopoly\\_fs/1.85931!Palmgren.pdf](http://lnu.se/polopoly_fs/1.85931!Palmgren.pdf)

# Electromagnetic losses in three-phase power cables

## Armour loss measurement: Armoured cable



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**ABB**

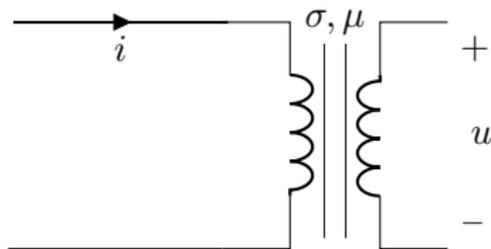
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# Estimation of electromagnetic losses in cable armour

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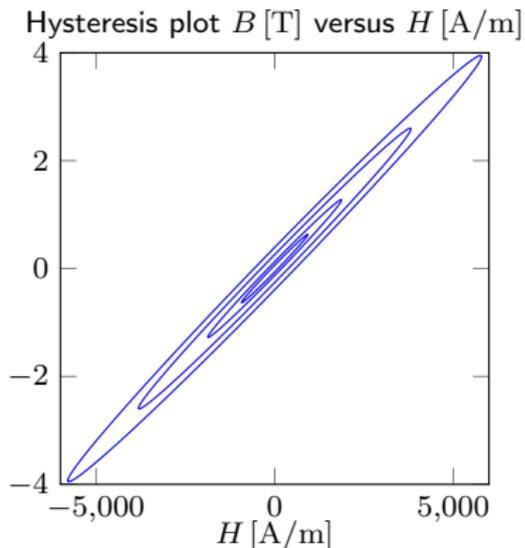
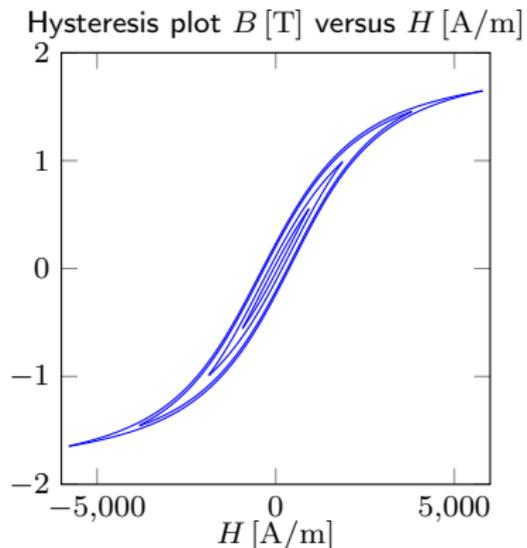
- ▶ Build and model a transformer based on the cable steel
- ▶ Conduction losses (eddy currents)  $J = \sigma E \Rightarrow D = \epsilon_0(\epsilon_r + i\frac{\sigma}{\omega\epsilon_0})E$
- ▶ Iron losses (hysteresis effect)  $B = \mu_0\mu(H)$
- ▶ How to estimate, simultaneously, the conduction losses as well as the (non-linear) hysteresis losses in the cable steel?
  - ▶ Linear model, proximity effects
  - ▶ Micromagnetic models: Jiles-Atherton model (1984-1986)
  - ▶ Variational models based on thermodynamics (1997-2011)
- ▶ Identify model (material) parameters based on measurements. EM-theory, estimation theory, convex optimization.



# Estimation of electromagnetic losses in cable armour

## Modeling of magnetic hysteresis losses in steel

Left: Classical non-linear Jiles-Atherton model. Right: Linear model.

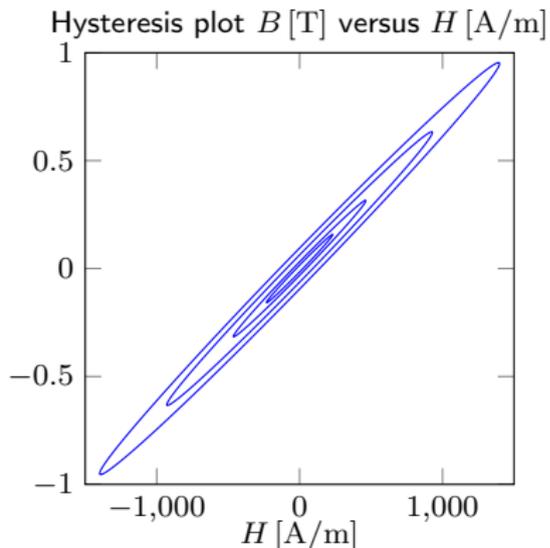
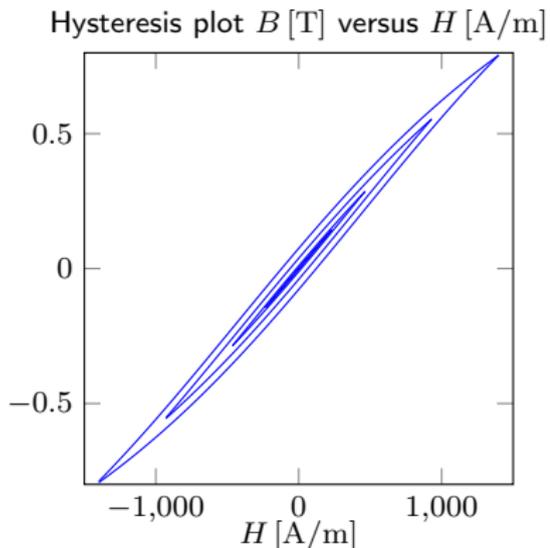


# Estimation of electromagnetic losses in cable armour

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## Modeling of magnetic hysteresis losses in steel

Left: Classical non-linear Jiles-Atherton model. Right: Linear model.



# Outline

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Research activities

Electromagnetic losses in three-phase power cables

**On the natural modes of helical structures**

# On the natural modes of helical structures

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Floquet wave number for periodic structures  $\mathbf{J}(\mathbf{r}) = \tilde{\mathbf{J}}(\mathbf{r})e^{i\beta z}$

Periodic electric Green's dyadic

$$\mathbf{E}(\mathbf{r}) = i\omega\mu_0\mu \int_S \int_0^P \mathbf{G}_{\text{ep}}(\mathbf{r}, \mathbf{r}', k, \beta) \cdot \mathbf{J}(\mathbf{r}') dS' dz'$$

Poisson summation formula

$$\begin{aligned} \mathbf{G}_{\text{ep}}(\mathbf{r}, \mathbf{r}', k, \beta) &= \sum_{n=-\infty}^{\infty} \mathbf{G}_e(\mathbf{r}, \mathbf{r}' + \hat{\mathbf{z}}np, k) e^{i\beta pn} \\ &= \frac{1}{p} \sum_{n=-\infty}^{\infty} \mathbf{G}_e(\boldsymbol{\rho}, \boldsymbol{\rho}', k, \beta + n\frac{2\pi}{p}) e^{i(\beta + n\frac{2\pi}{p})(z-z')} \end{aligned}$$

Spectral representation of the free-space electric Green's dyadic

$$\mathbf{G}_e(\mathbf{r}, \mathbf{r}', k) = \left\{ \mathbf{I} + \frac{1}{k^2} \nabla \nabla \right\} \frac{e^{ik|\mathbf{r}-\mathbf{r}'|}}{4\pi|\mathbf{r}-\mathbf{r}'|} = \frac{1}{2\pi} \int_{-\infty}^{\infty} \mathbf{G}_e(\boldsymbol{\rho}, \boldsymbol{\rho}', k, \alpha) e^{i\alpha(z-z')} d\alpha$$

# On the natural modes of helical structures

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- ▶ Periodic volume integral equation for the electric field, based on the Floquet mode  $e^{i\beta z}$

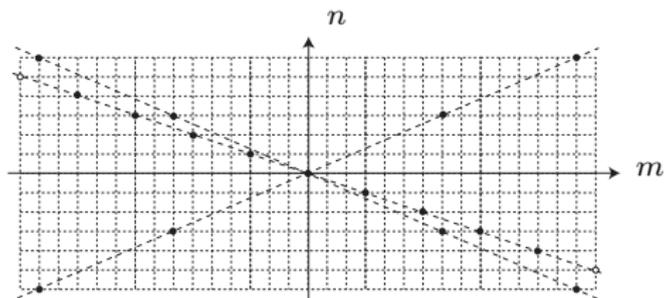
$$[\mathbf{I} + \hat{\rho}\hat{\rho} \cdot \chi(\mathbf{r})] \cdot \mathbf{E}(\mathbf{r}) - k^2 \int_S \int_0^p \mathbf{G}_{\text{ep}}^0(\mathbf{r}, \mathbf{r}', k, \beta) \cdot \chi(\mathbf{r}') \cdot \mathbf{E}(\mathbf{r}') dS' dz' = \mathbf{0}$$

- ▶ Expansion of the periodic dyadic Green's function  $\mathbf{G}_{\text{ep}}^0(\mathbf{r}, \mathbf{r}', k, \beta)$  in cylindrical vector waves.
- ▶ A two-dimensional Fourier series expansion yields an infinite system of coupled one-dimensional integral equations

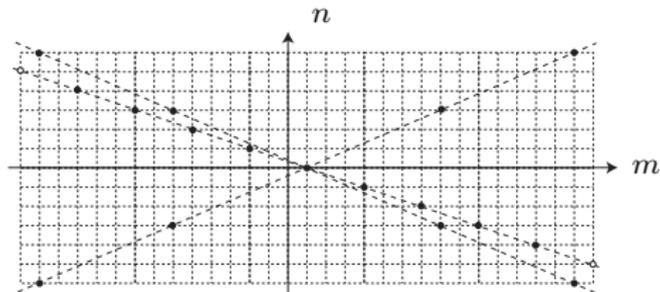
$$\begin{aligned} \mathbf{E}_{mn}(\boldsymbol{\rho}) + \hat{\rho}\hat{\rho} \cdot \sum_{m'} \sum_{n'} \chi_{m-m', n-n'}(\boldsymbol{\rho}) \cdot \mathbf{E}_{m'n'}(\boldsymbol{\rho}) \\ - k^2 2\pi \int_0^a \mathbf{a}_m(\boldsymbol{\rho}, \boldsymbol{\rho}', k, \beta + n \frac{2\pi}{p}) \cdot \sum_{m'} \sum_{n'} \chi_{m-m', n-n'}(\boldsymbol{\rho}') \cdot \mathbf{E}_{m'n'}(\boldsymbol{\rho}') \rho' d\rho' \\ = \mathbf{0} \end{aligned}$$

# On the natural modes of helical structures

Material twist-modes  $\chi_{mn}$  in Fourier space



Azimuthal Floquet mode  $\mathbf{E}_{mn}$  containing the “excitation” factor  $e^{i\phi}$   
Quasi-static assumption: The mode shapes of  $\mathbf{E}$  is the same as for  $\chi$



# On the natural modes of helical structures

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## Issues

- ▶ Proper treatment of the source point (here in cylindrical coordinates)

$$\mathbf{G}_e(\mathbf{r}, \mathbf{r}', k) = \left\{ \mathbf{I} + \frac{1}{k^2} \nabla \nabla \right\} \frac{e^{ik|\mathbf{r}-\mathbf{r}'|}}{4\pi|\mathbf{r}-\mathbf{r}'|} = \mathbf{G}_e^0(\mathbf{r}, \mathbf{r}', k) - \frac{1}{k^2} \hat{\rho} \hat{\rho} \delta(\mathbf{r}-\mathbf{r}')$$

- ▶ The volume integral formulation is known to be “strongly” singular.
- ▶ Each one-dimensional integral operator is only weakly singular (discontinuous kernel).
- ▶ Spectral theory, characterization of spectral properties similar to Fredholm theory?
- ▶ Analytic function theory view. Existence of modes (residues), radiation modes are the contributions from an integration along the branch-cut.