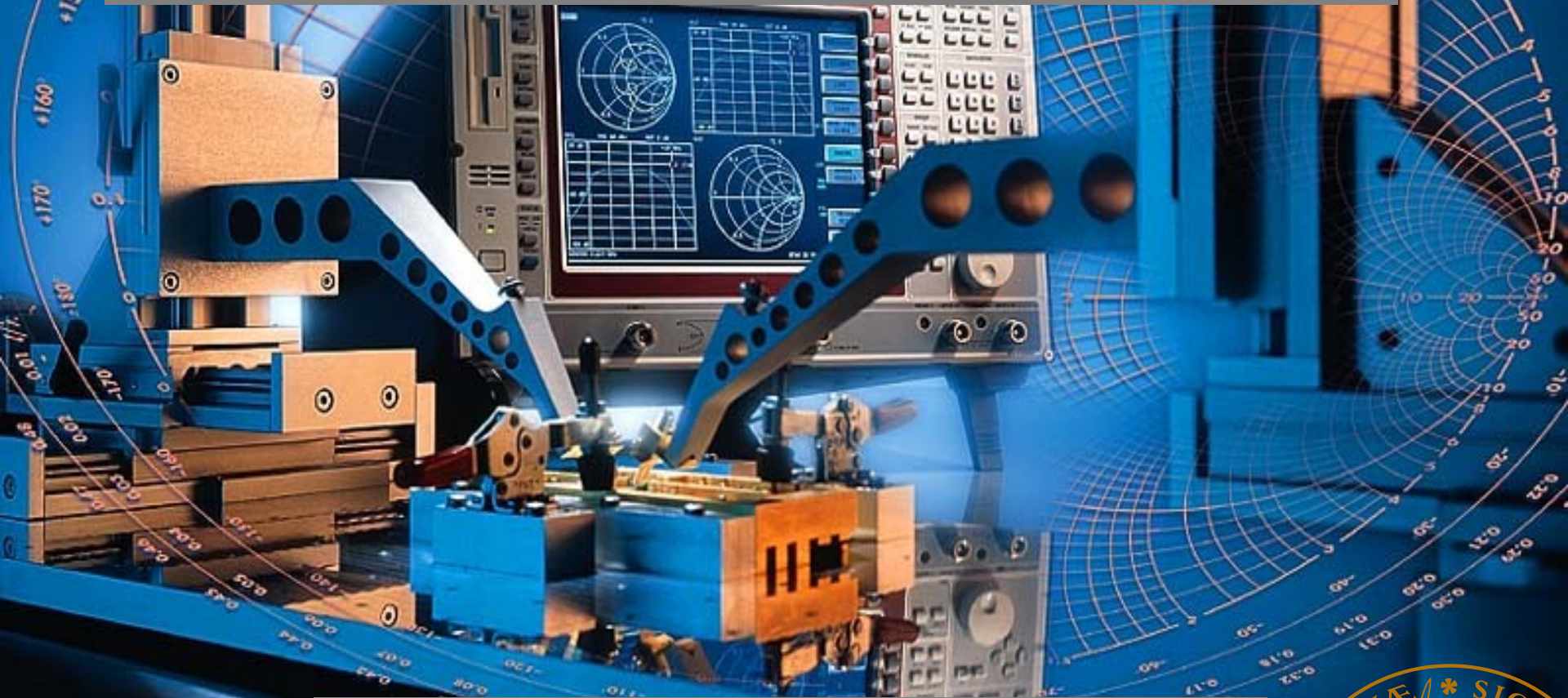


Lecture 3

2019-11-11

# RF Amplifier Design



Lars Ohlsson Fhager  
Electrical and Information Technology



# Course Administration

- Register in LADOK  
(<https://www.student.lu.se/>)
  - Sign up (beforehand or on manual list)
  - Register
  
- LU Canvas > ETIN50  
(<https://canvas.education.lu.se/>)
  - Course materials
  - Track lab progress
  - Hand in and grade reports

# Schedule

- Lab Sessions
  - Only the morning slot of the labs will be offered due to the number of students this year
- This week: 1x Lecture, Handin 1 published, 2x Exercise, Lab 1
  - Hand-in assignment 1: “Input Impedance and Mismatch Loss” now published, due Fri, Nov 22, 23:59
  - Lab 1: “Parallel Resonant Circuits”  
Thu, Nov 14, 8:00-12:00
  - Preparation tasks are compulsory to start labwork
  - 2x Exercises => make sure to have done lab prep. before and ask
  - Also, demo of “deslib” toolbox for MATLAB on E3

# Lecture 3

- The Smith Chart
  - Structure
    - Reflection Coefficient and Impedance
    - Scales
  - Applications
    - Reflection Coefficient and Electrical Length
    - Impedance and Admittance
    - Series Connection
    - Parallel Connection
    - Combined Z and Y Scales
    - Circuit Q
    - Standing-Wave Ratio

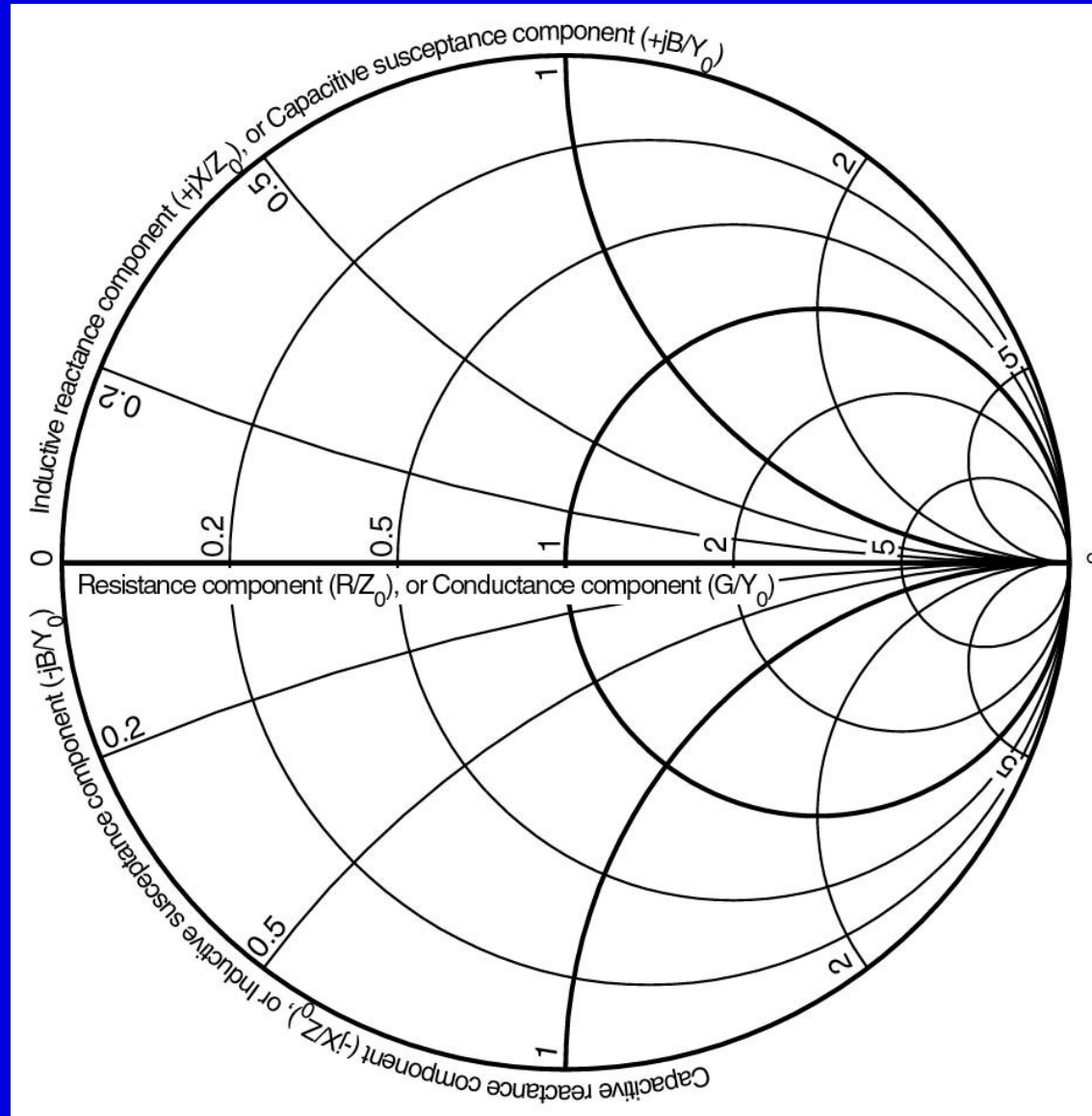
## Reading Guide

- Chapter 4

# The Smith Chart

The chart was invented by Phillip Smith in the early 1930-ties

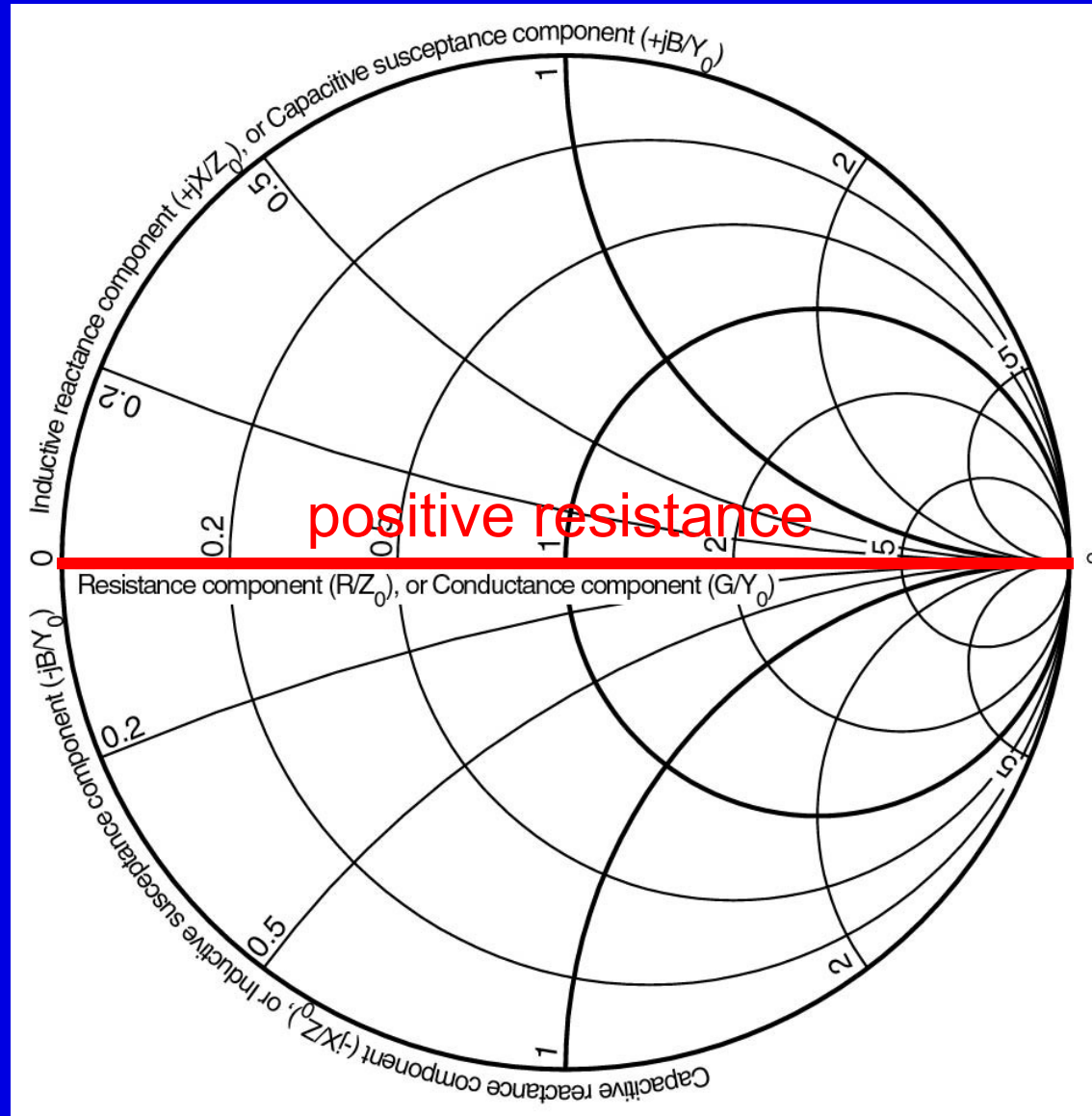
Transform between the  $\Gamma$ - and  $Z$ -plane



# The Smith Chart

The chart was invented by Phillip Smith in the early 1930-ties

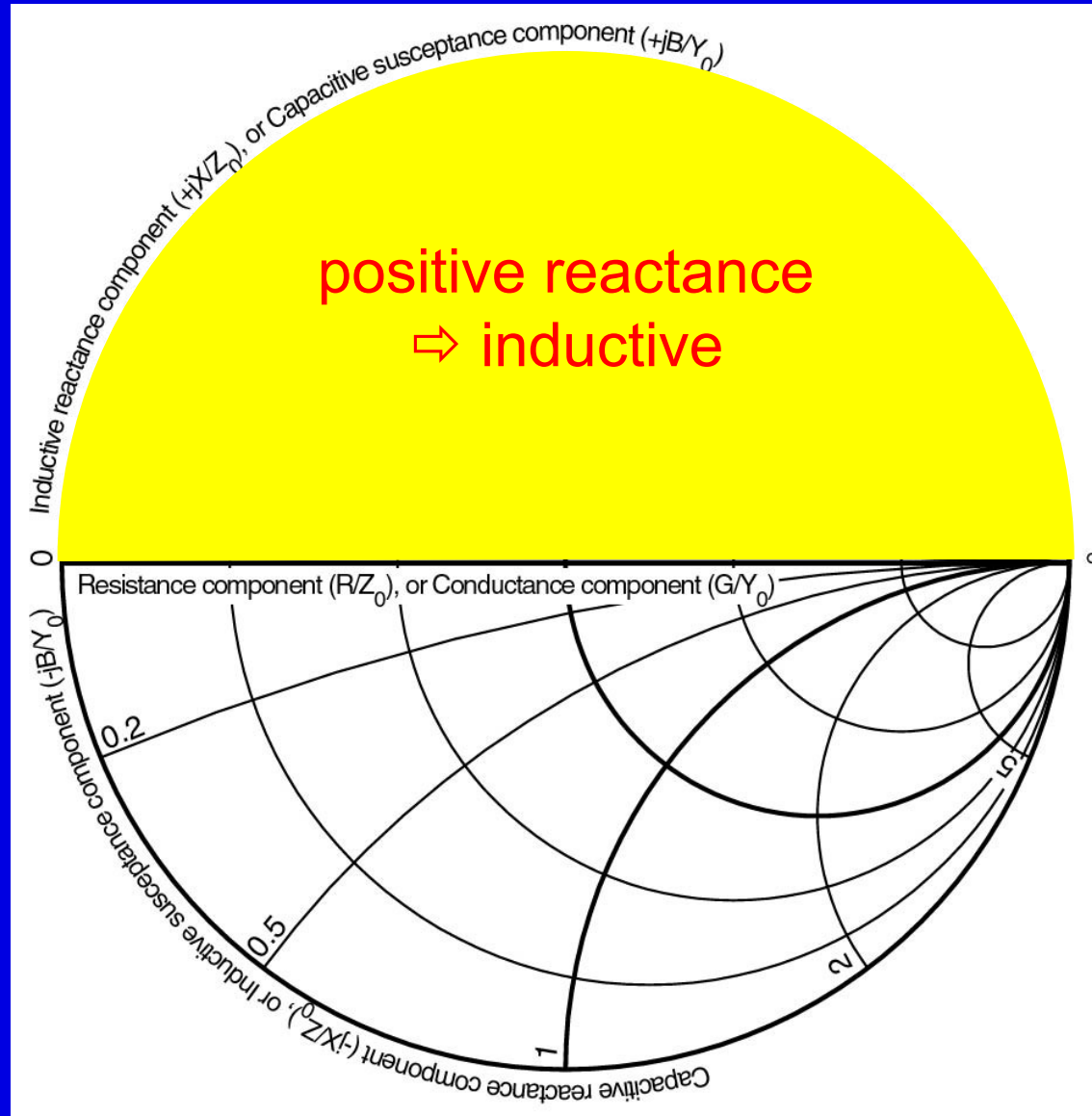
Transform between the  $\Gamma$ - and  $Z$ -plane



# The Smith Chart

The chart was invented by Phillip Smith in the early 1930-ties

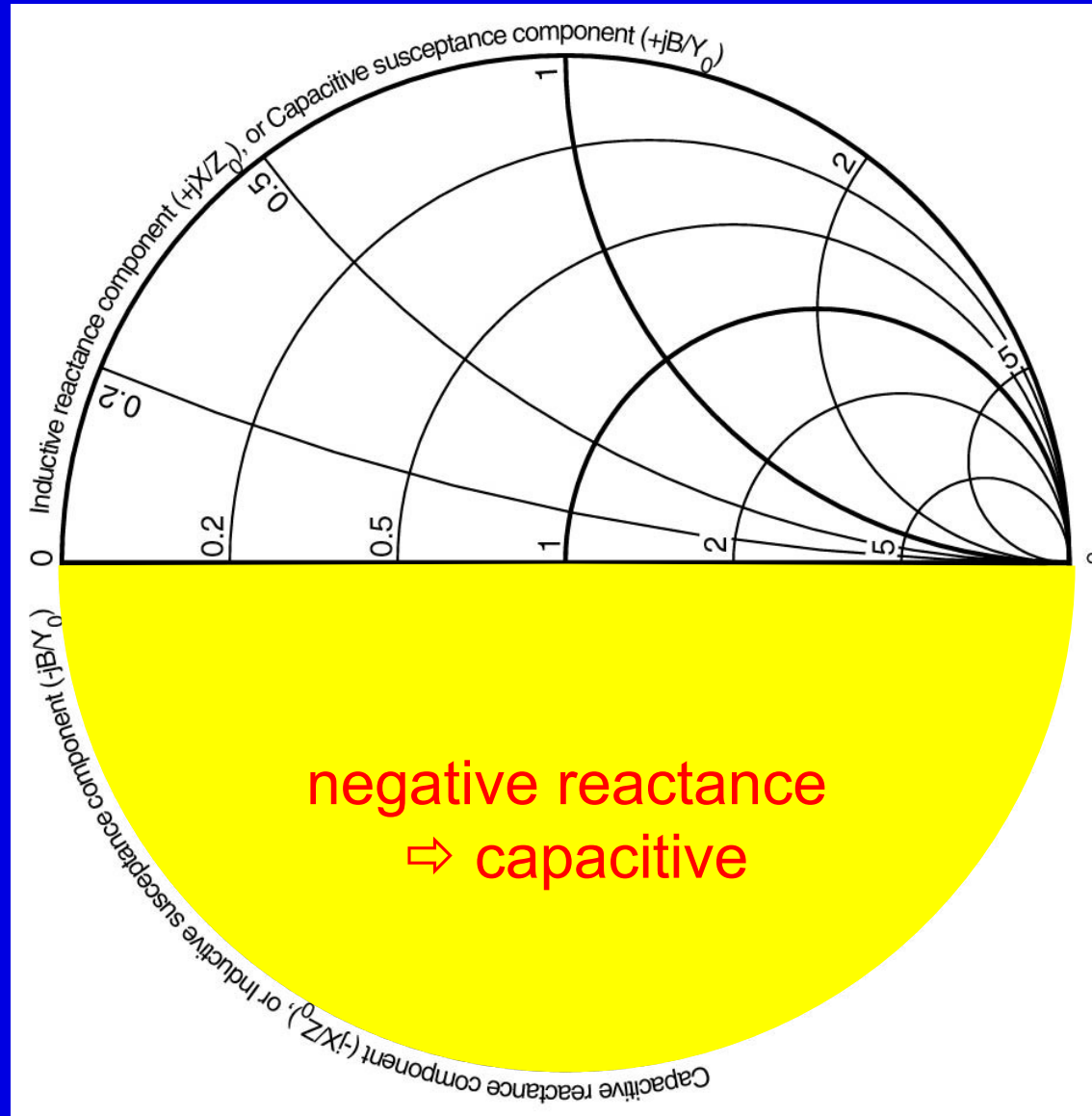
Transform between the  $\Gamma$ - and  $Z$ -plane



# The Smith Chart

The chart was invented by Phillip Smith in the early 1930-ties

Transform between the  $\Gamma$ - and  $Z$ -plane



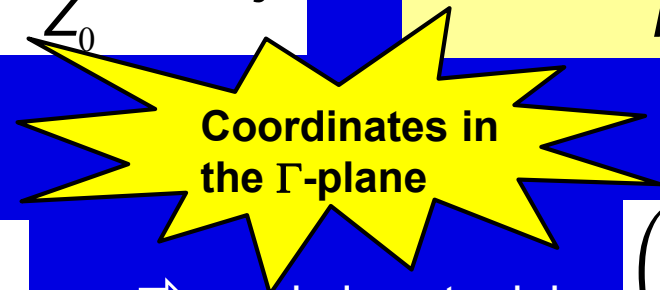


# The Structure of the Smith Chart

- Impedance  $Z = R + jX$

- Reflection coefficient  $\Gamma = \rho \angle \phi = \rho \exp(j\phi) = p + jq$

- Conversion:  $\Gamma = \frac{z-1}{z+1}$  where  $z = \frac{Z}{Z_0} = r + jx \Rightarrow p + jq = \frac{r-1+jx}{r+1+jx}$

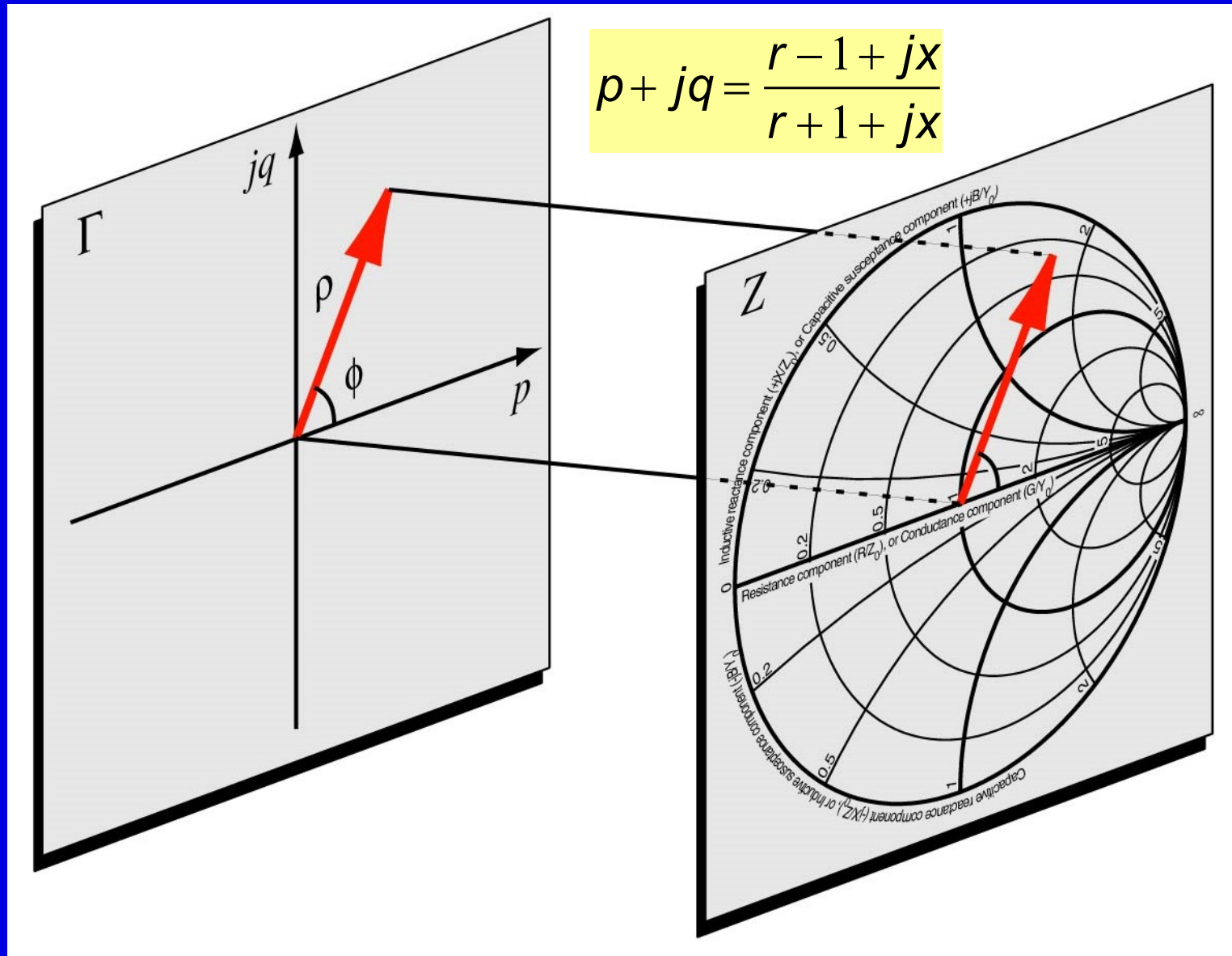


- split up the expression in

- real part:  $\left(p - \frac{r}{r+1}\right)^2 + q^2 = \left(\frac{1}{r+1}\right)^2 \Rightarrow$  circles at origin  $\left(\frac{r}{r+1}, 0\right)$  and radius  $\frac{1}{r+1}$

- Imaginary part:  $\left(q - \frac{1}{x}\right)^2 + (1-p)^2 = \left(\frac{1}{x}\right)^2 \Rightarrow$  circles at origin  $\left(1, \frac{1}{x}\right)$  and radius  $\frac{1}{x}$

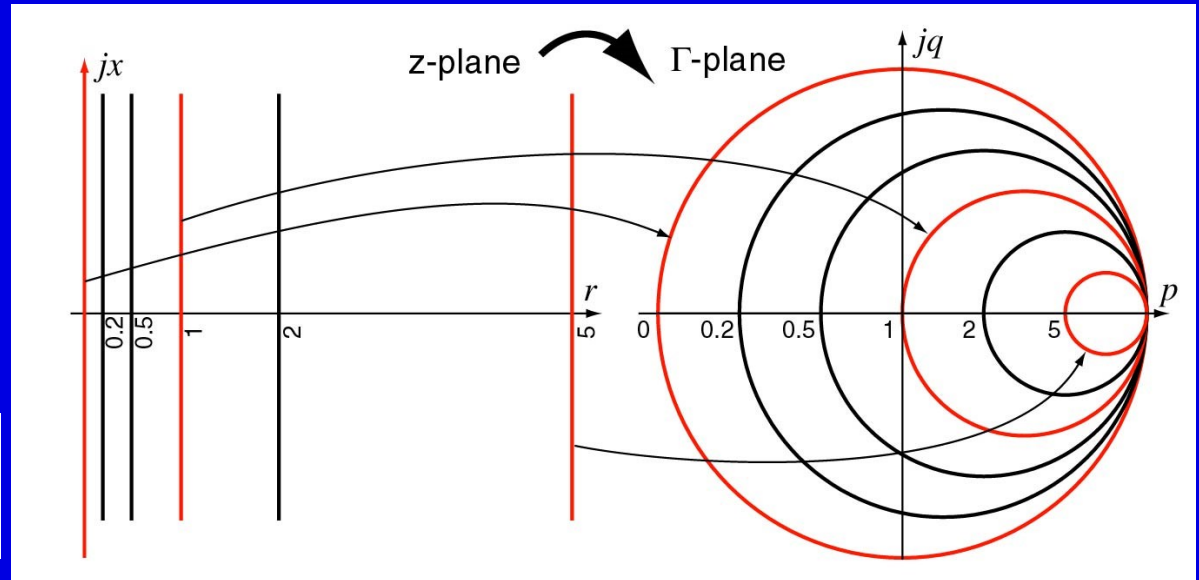
# Reflection Coefficient $\Rightarrow$ Impedance



# The Smith Chart Circles

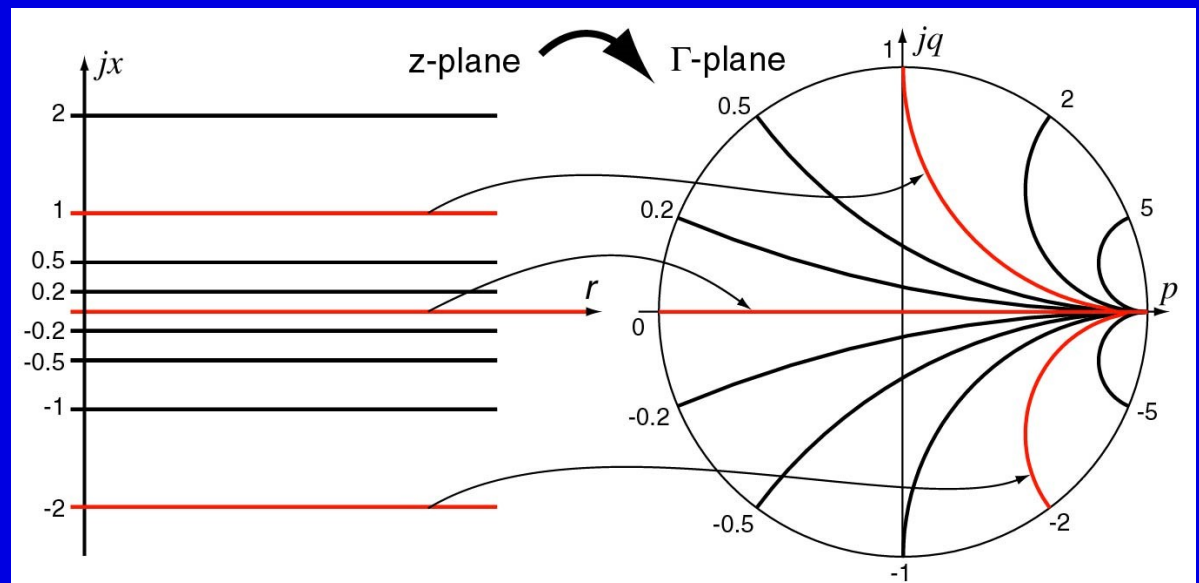
- Constant resistance lines  $\Rightarrow$  resistance circles

$$\left(p - \frac{r}{r+1}\right)^2 + q^2 = \left(\frac{1}{r+1}\right)^2$$



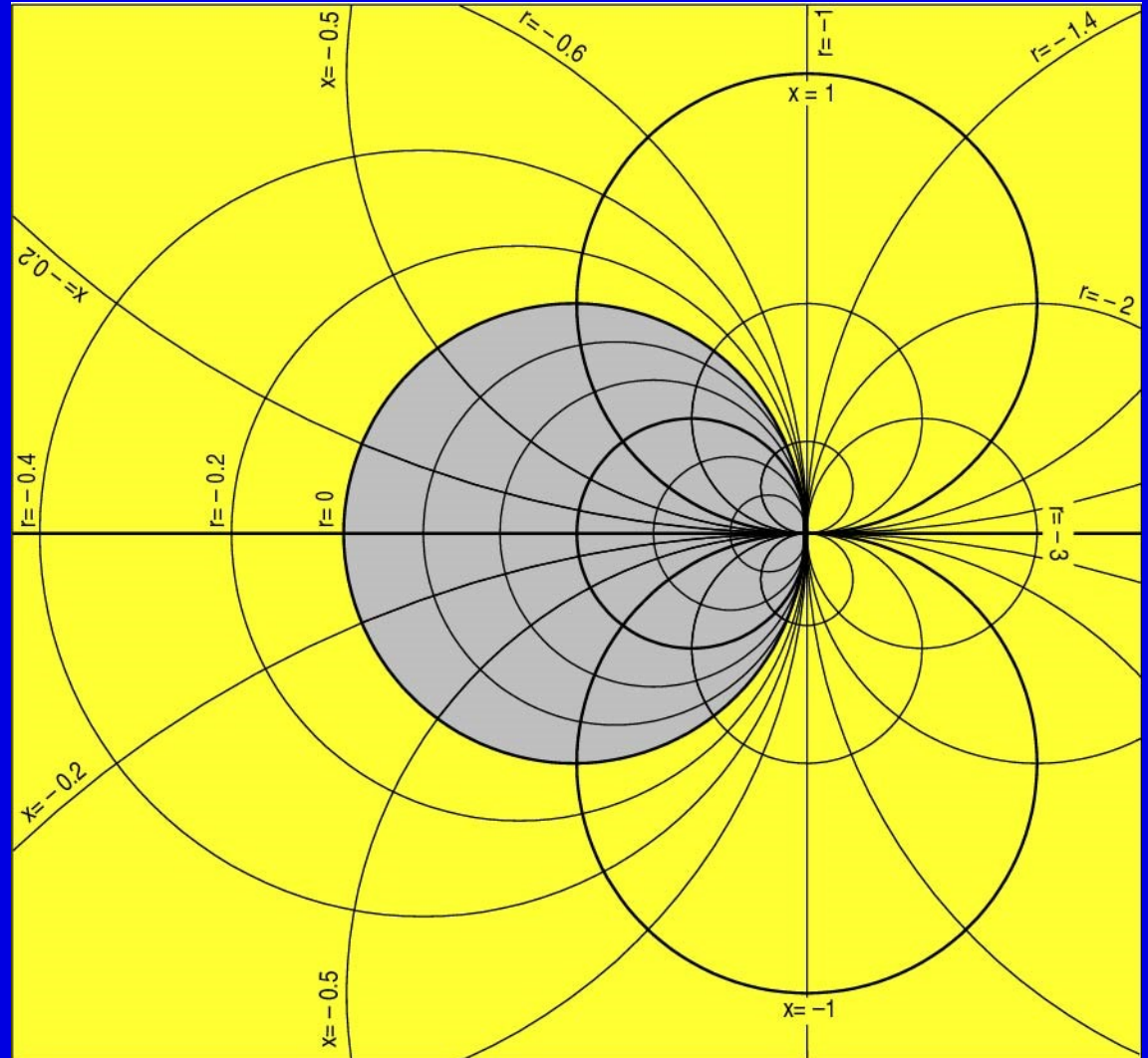
- Constant reactance lines  $\Rightarrow$  reactance circles

$$\left(q - \frac{1}{x}\right)^2 + (1-p)^2 = \left(\frac{1}{x}\right)^2$$

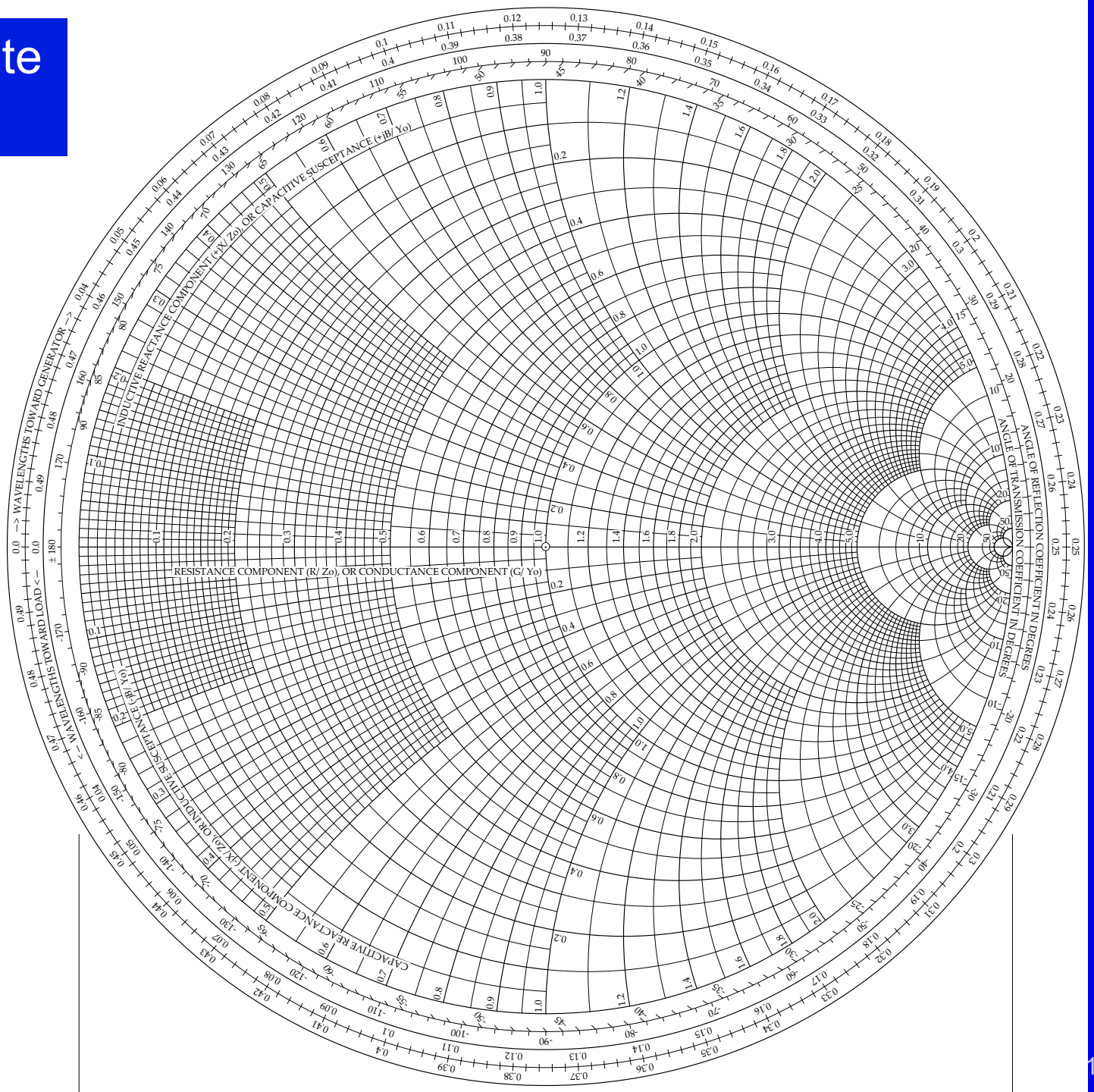


# Negative Resistance

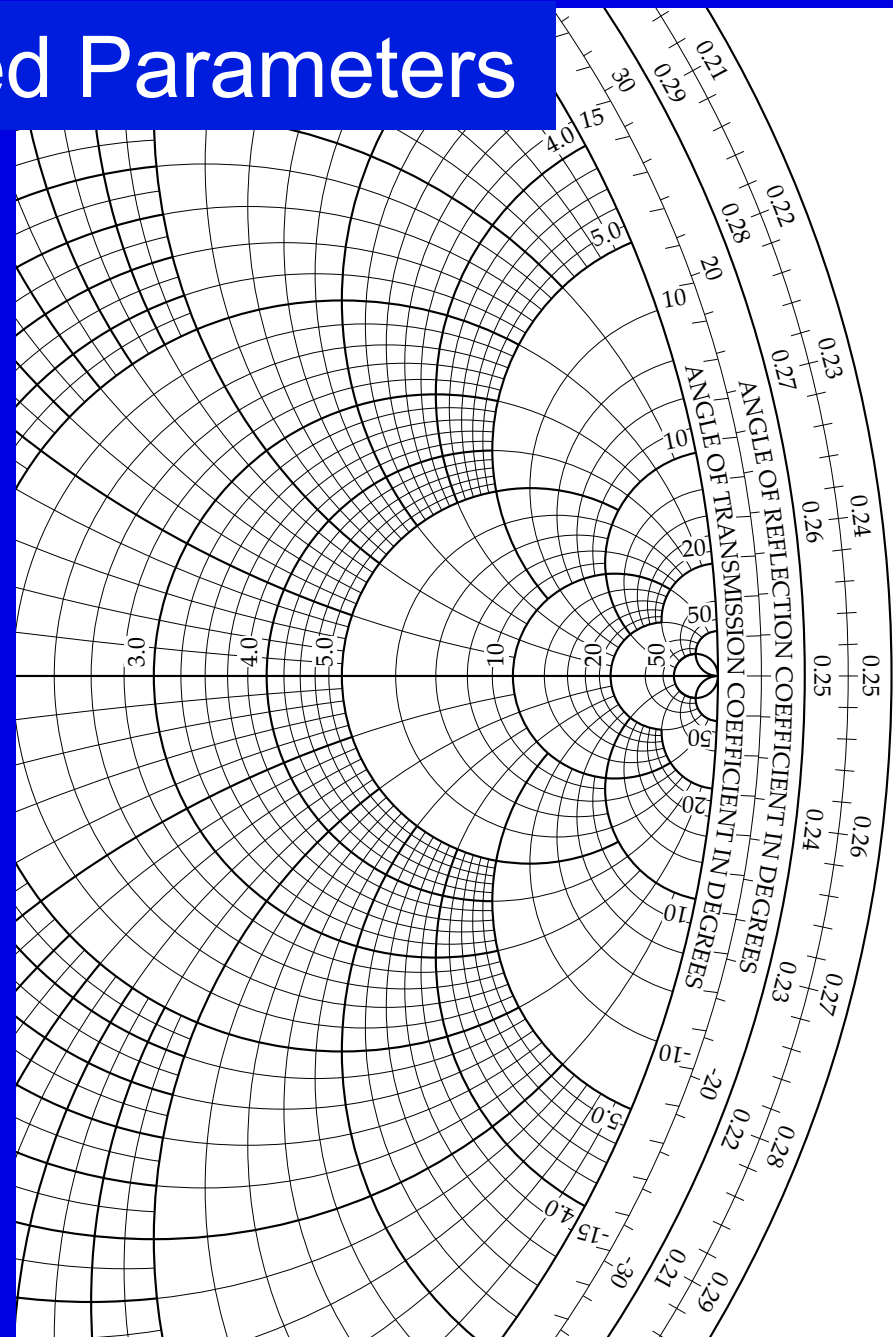
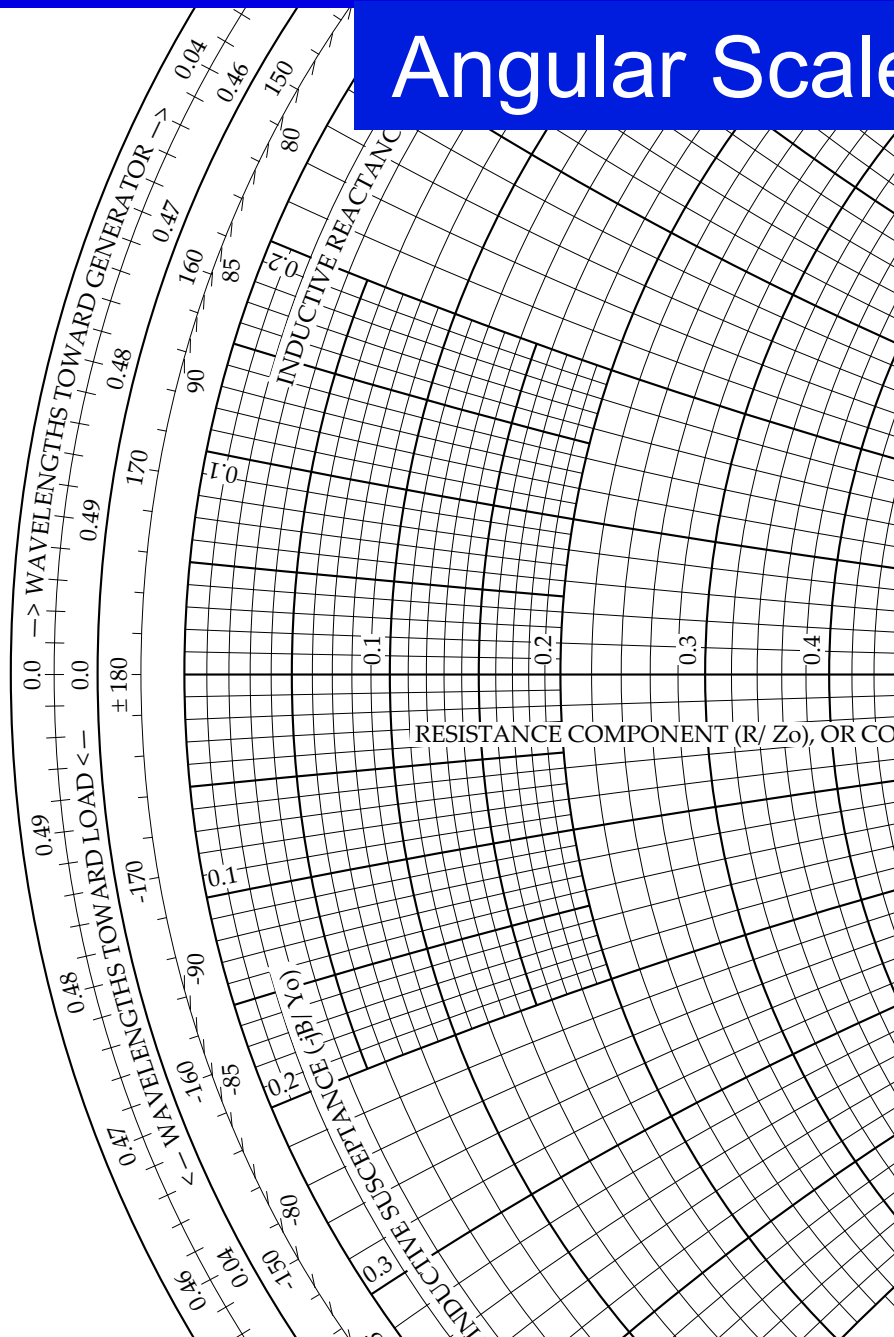
- Negative resistance is mapped **outside** Smith chart unit circle



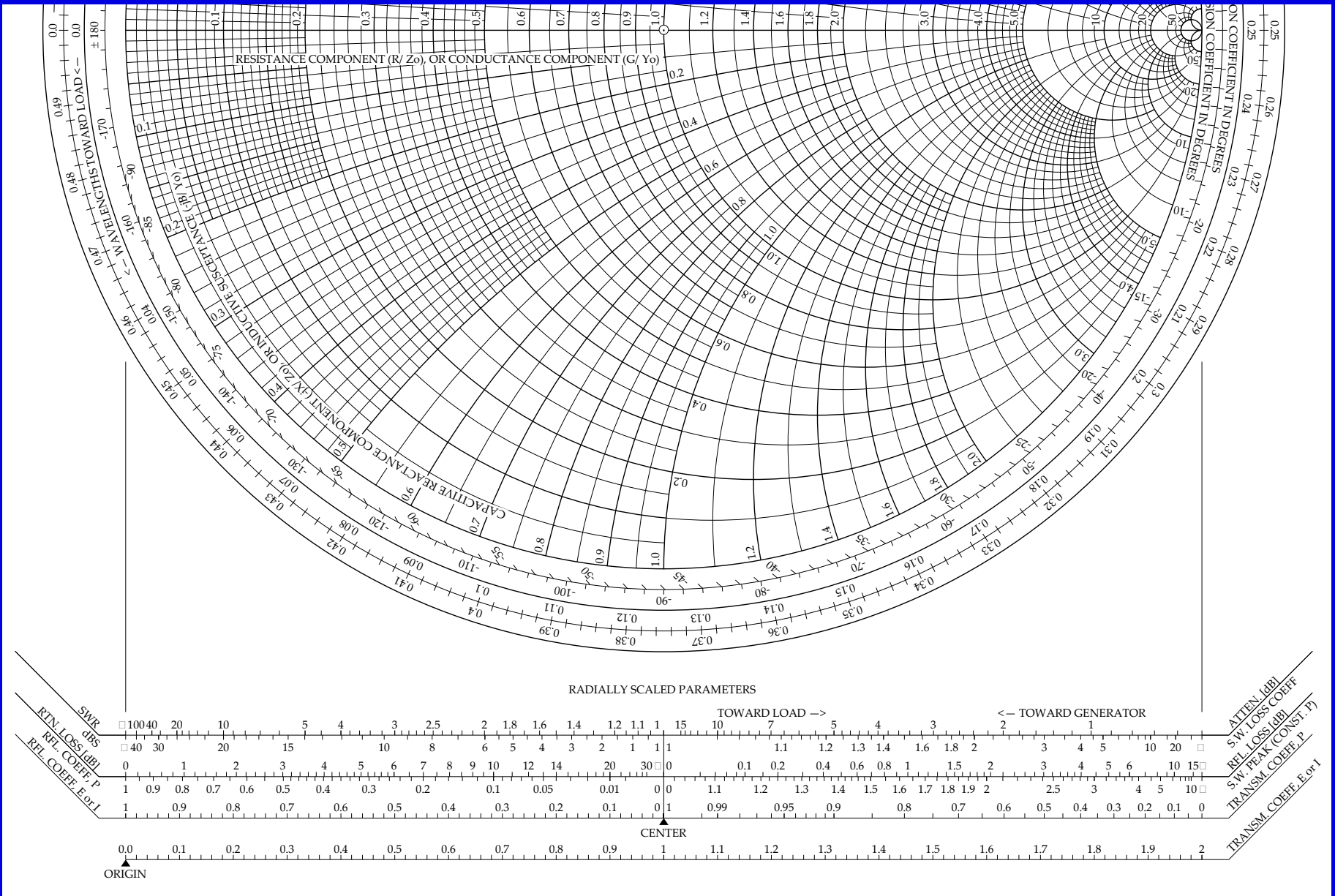
# The Complete Smith Chart



# Angular Scaled Parameters



# Radially Scaled Parameters

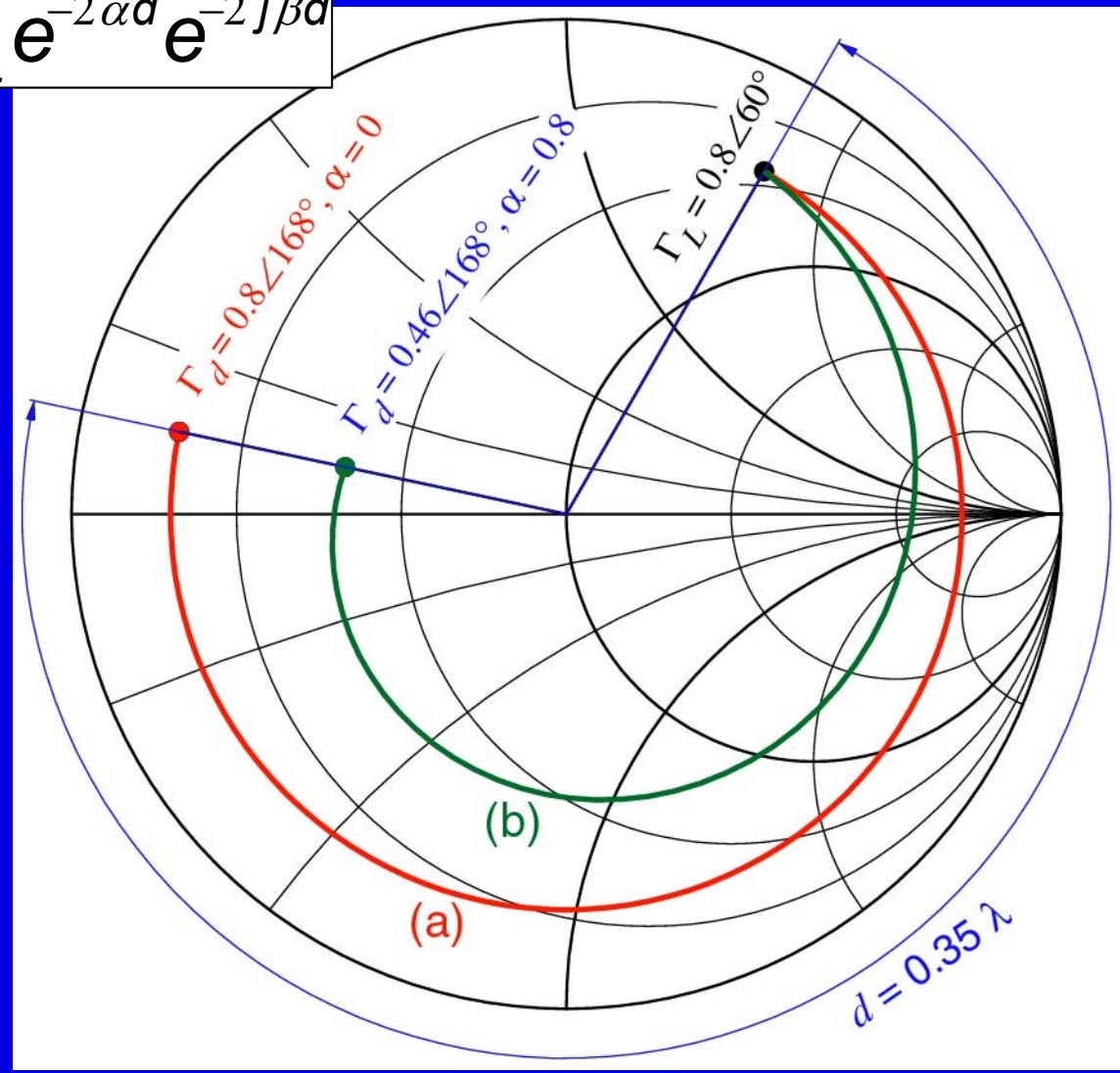


# Reflection Coefficient and Electrical Length

$$\Gamma_d = \Gamma_L e^{-2\gamma d} = \Gamma_L e^{-2\alpha d} e^{-2j\beta d}$$

transmission through

- a) a lossless line
- b) a lossy line

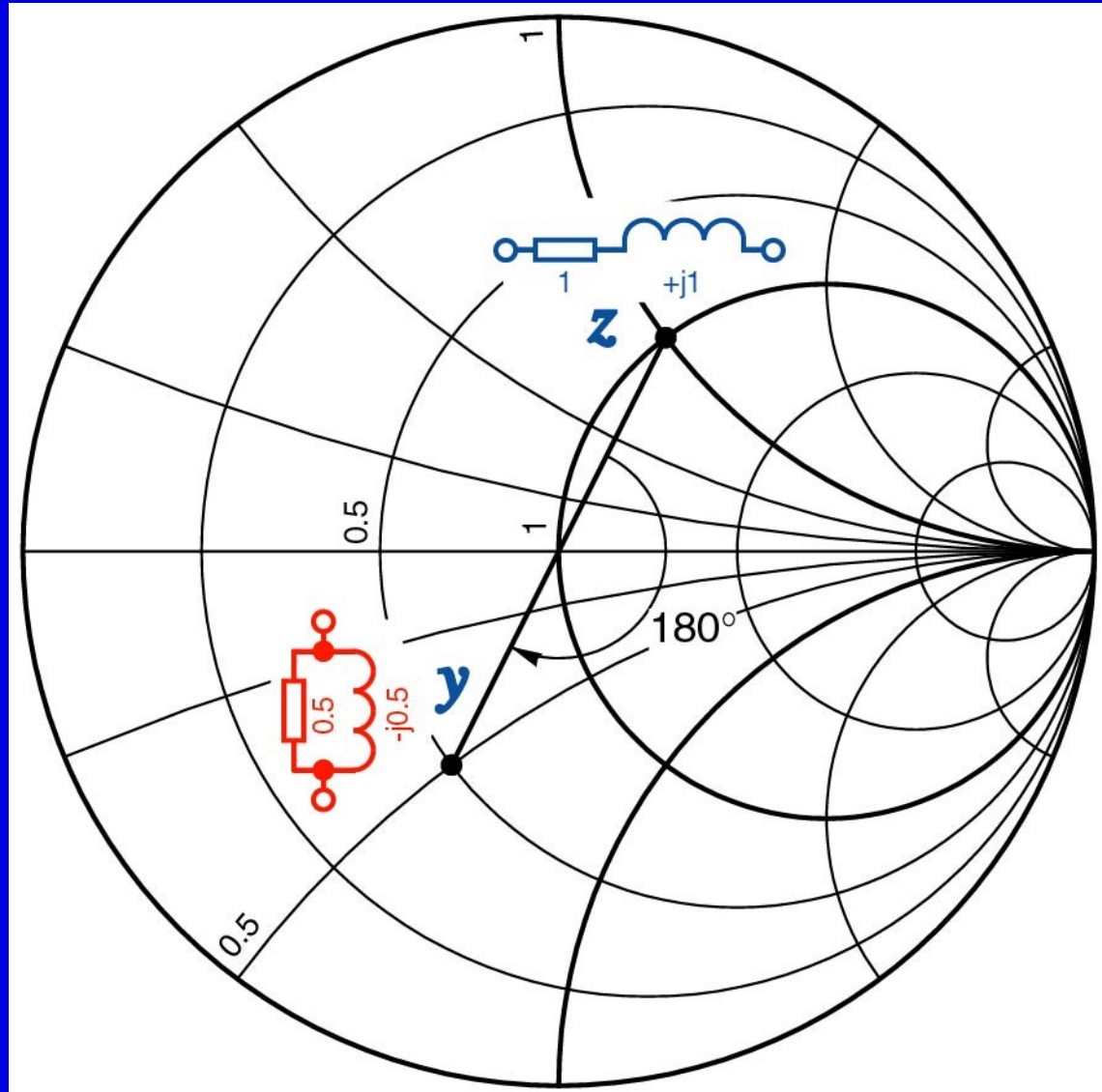




# Conversion of Impedance $\Rightarrow$ Admittance

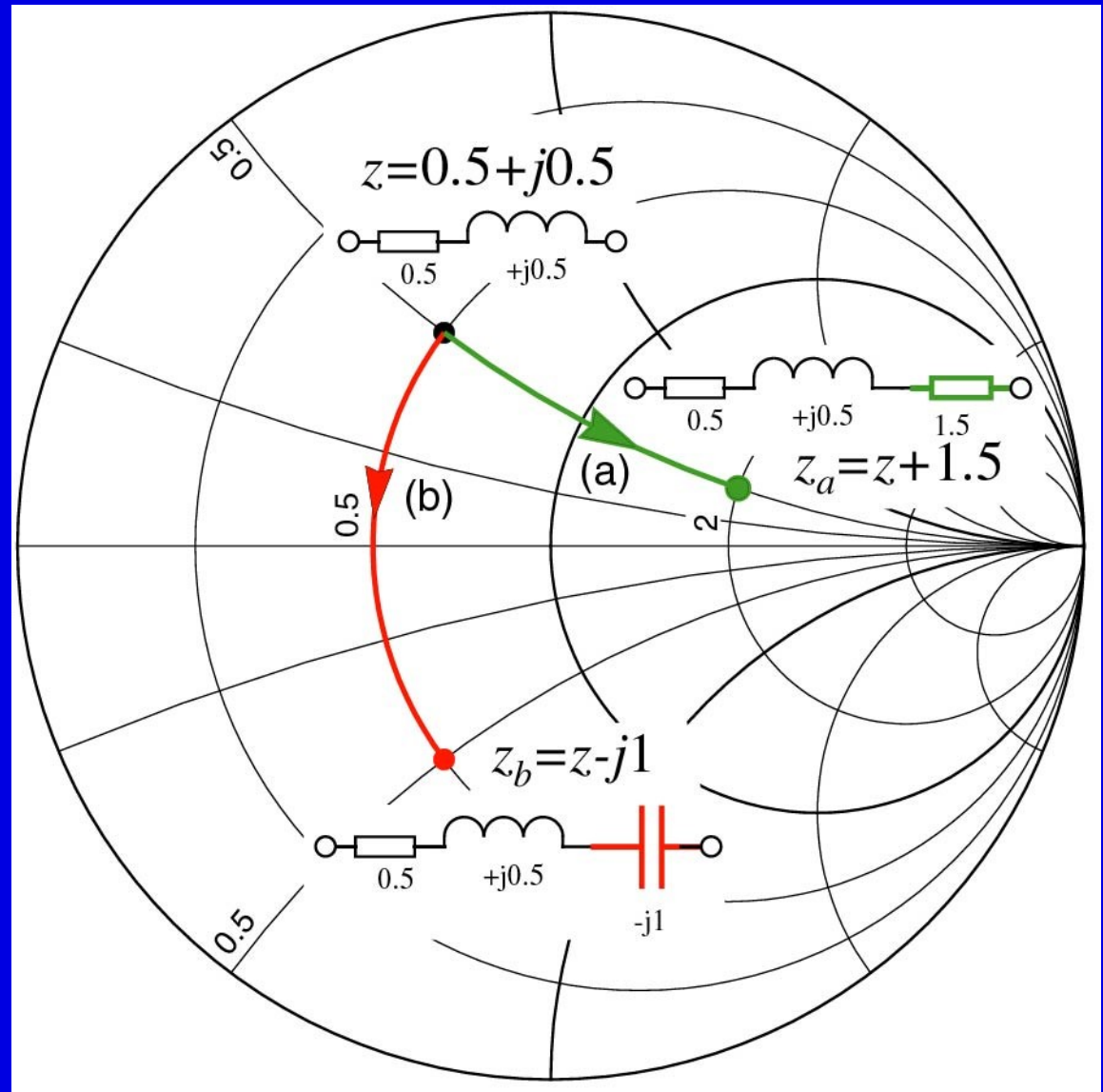
$$Z = \frac{1}{y}$$

$$\begin{aligned}\Gamma(y) &= \frac{1/y - 1}{1/y + 1} = \\ &= -\frac{y - 1}{y + 1} = \\ &= -\Gamma(z) = e^{j\pi}\Gamma(z)\end{aligned}$$



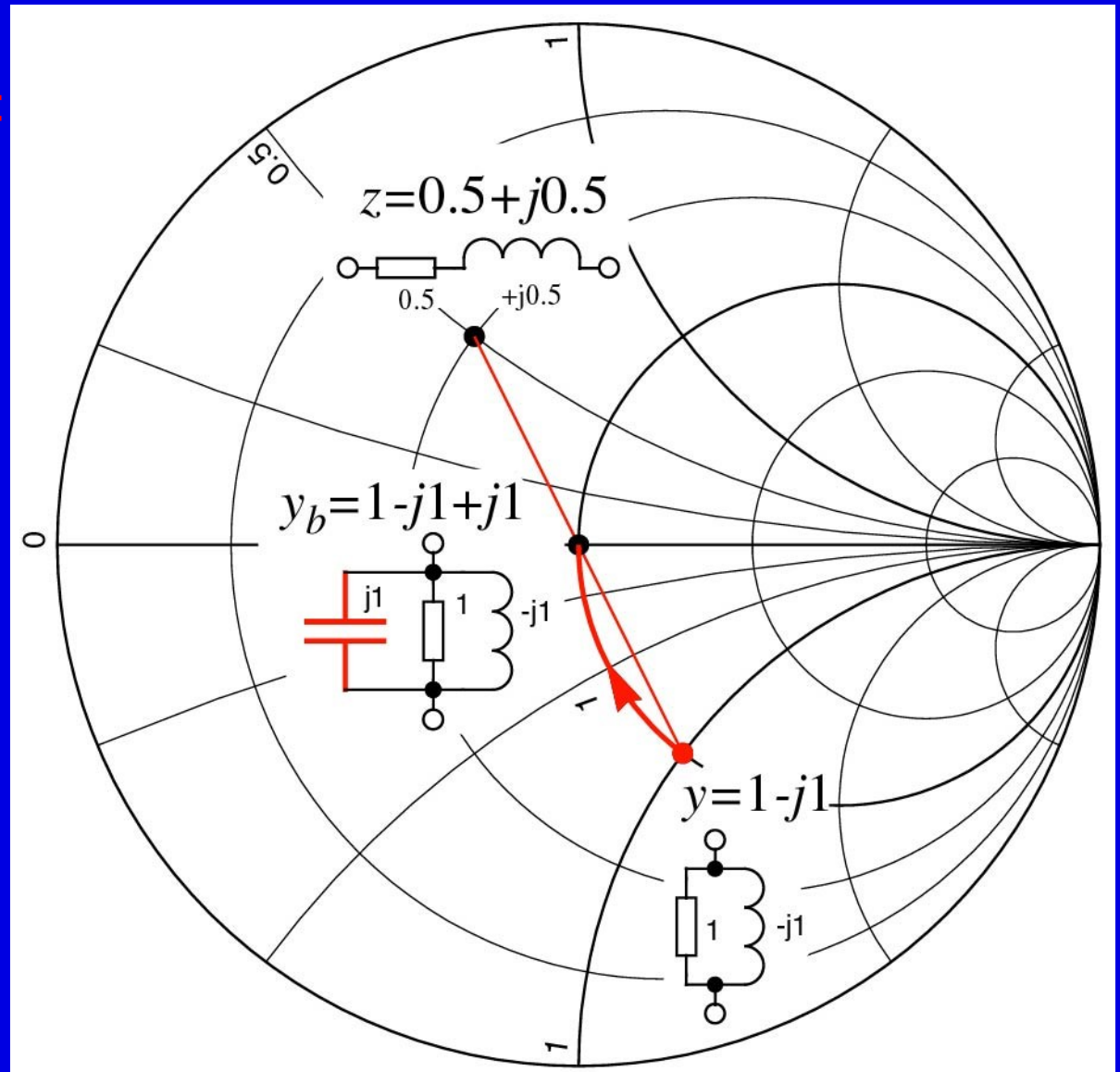
# Series Connection

- **Addition of resistance:**
  - sliding at a constant reactance circle
- **Addition of reactance:**
  - sliding at a constant resistance circle



# Parallel Connection

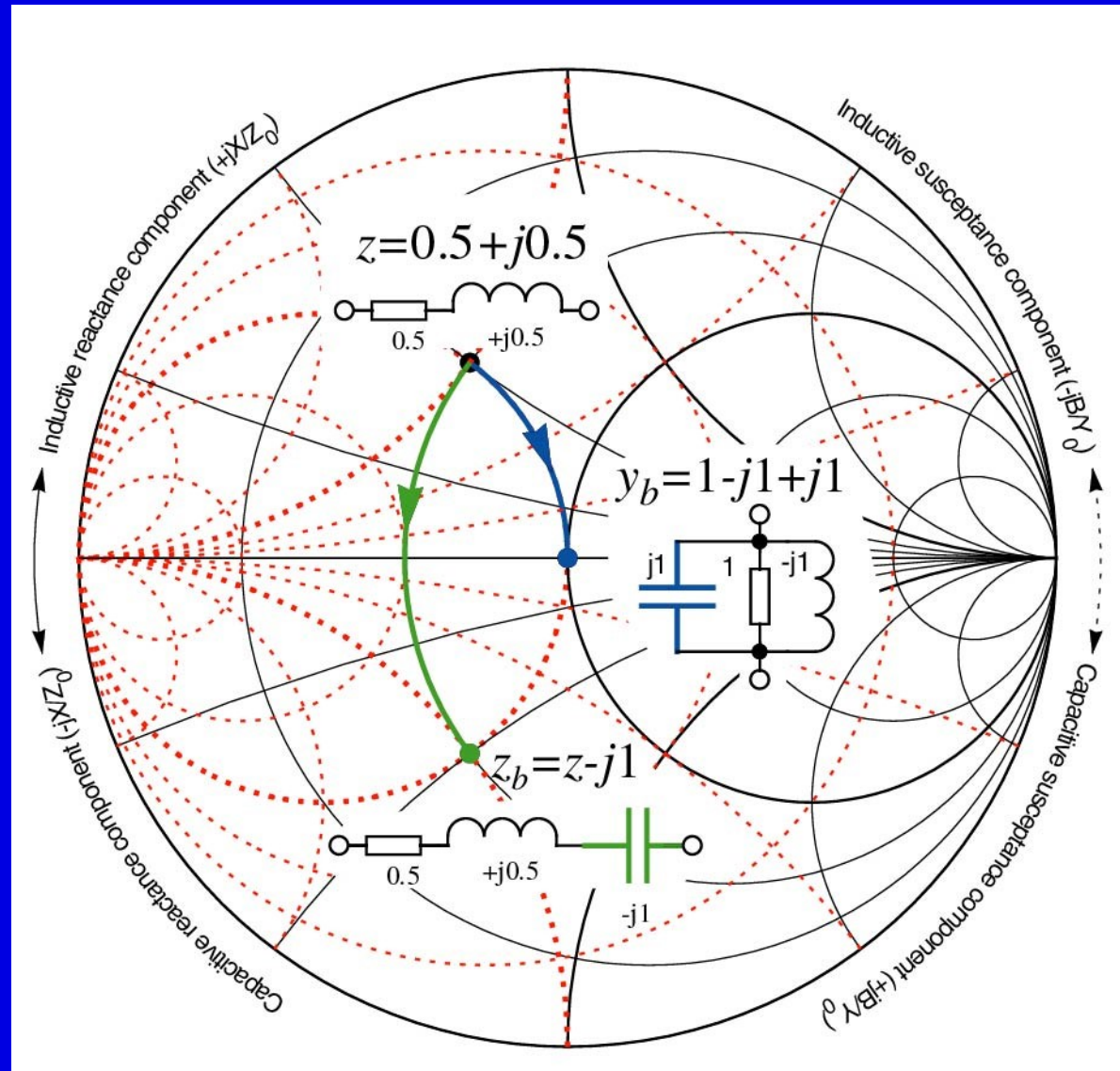
- Addition of susceptance:
  - motion at a constant conductance circle



# The Inverted Smith Chart

- The chart holds both **Z-** and **Y scales**
- The inverted Smith chart is used to read **admittance**

- **Series connection of X:**
  - slide along a constant resistance circle
- **Parallel connection of X:**
  - slide along a constant conductance circle

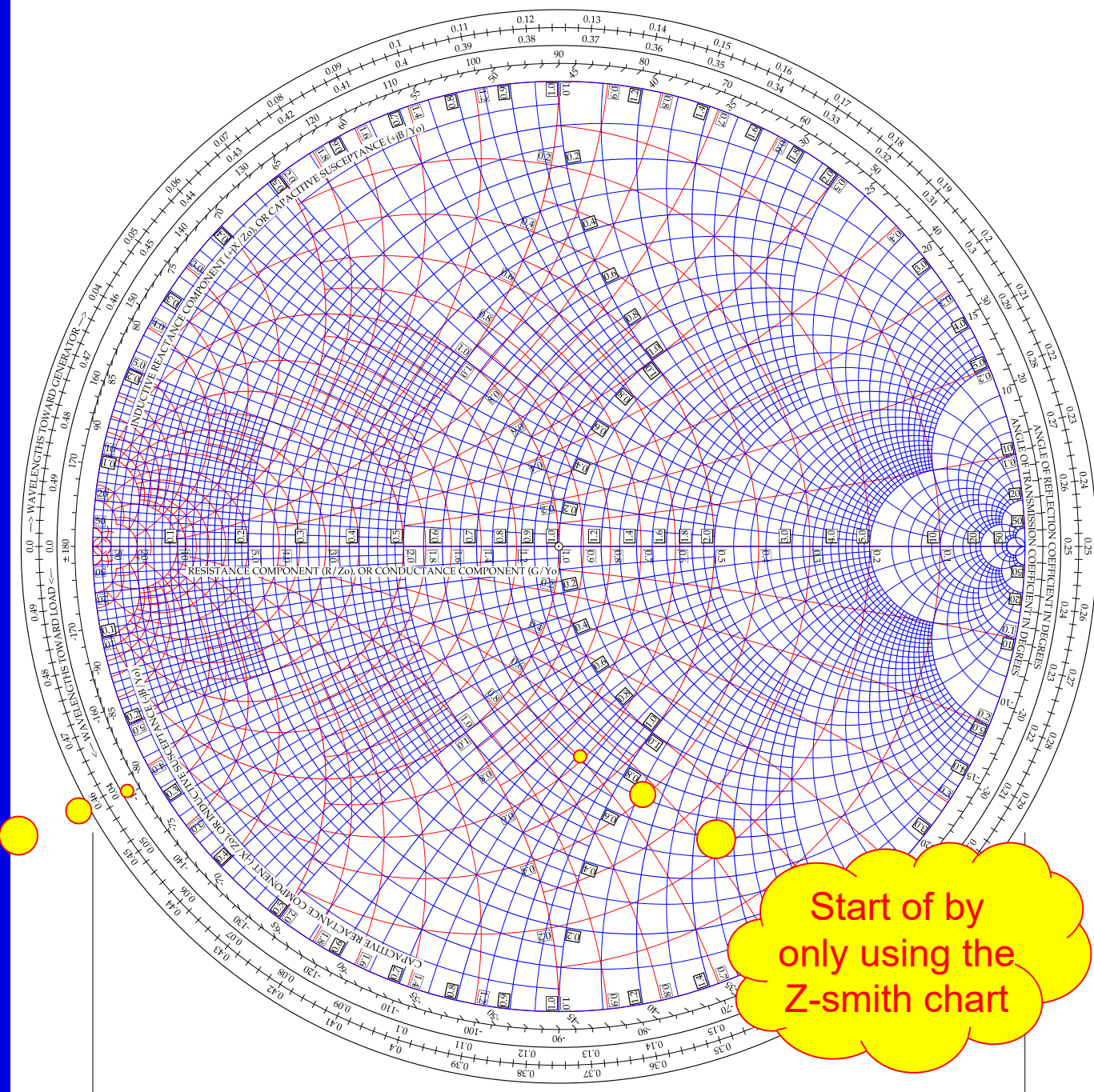


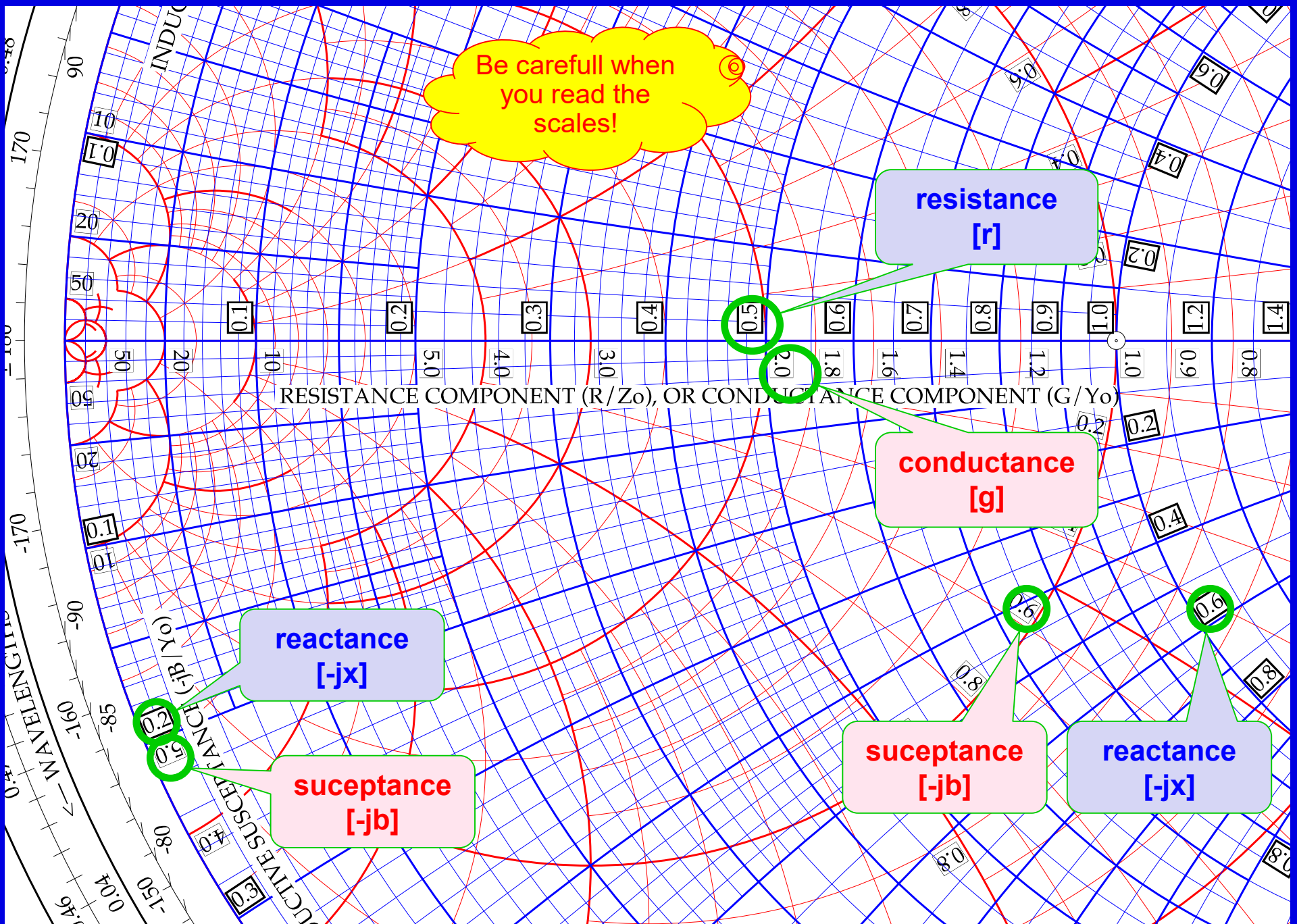
# Combined Impedance and Admittance Chart

- The chart holds both **Z**- and **Y**-scales
- The **inverted Smith chart** is used to read admittance

Be carefull when you read the scales!

Start of by only using the Z-smith chart

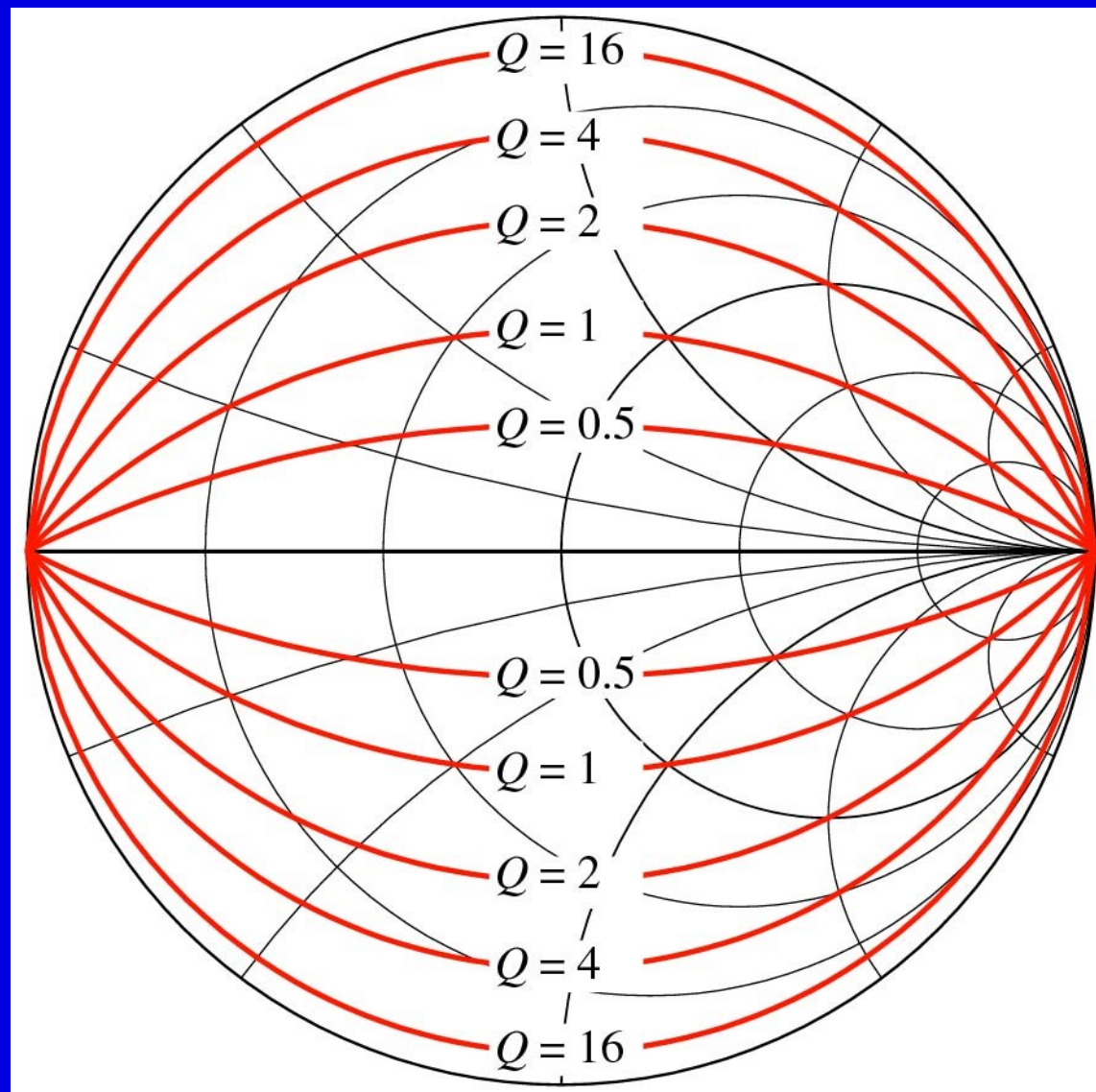




# Circuit Q

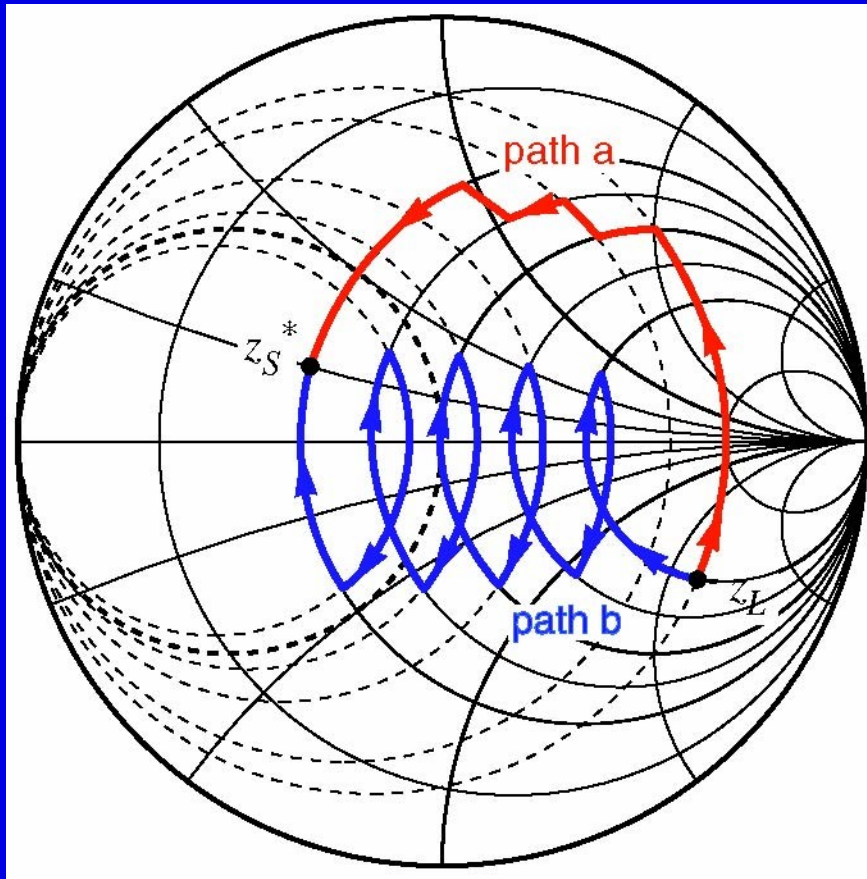
- If the Smith chart shows impedance, the circuit Q will be calculated as for a series connection:

$$Q = \frac{X}{r}$$

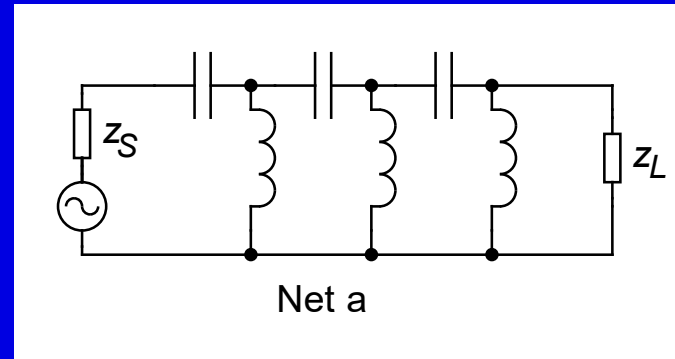


# Matching Networks

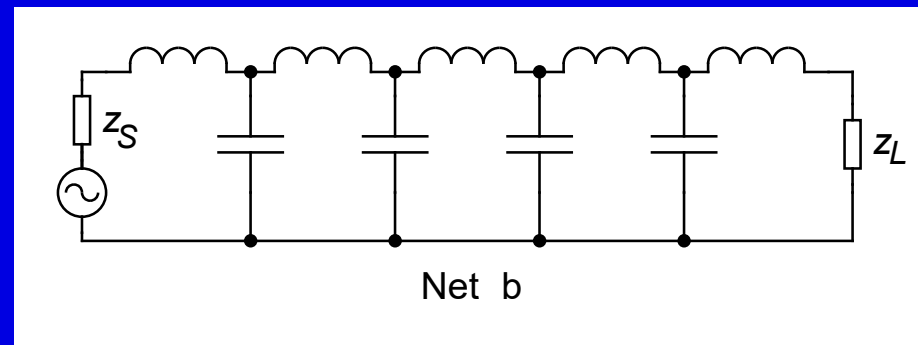
- By choosing a “path” in the Smith chart the circuit Q and the bandwidth of the network may be affected



High circuit Q = narrow bandwidth



Low circuit Q = wide bandwidth



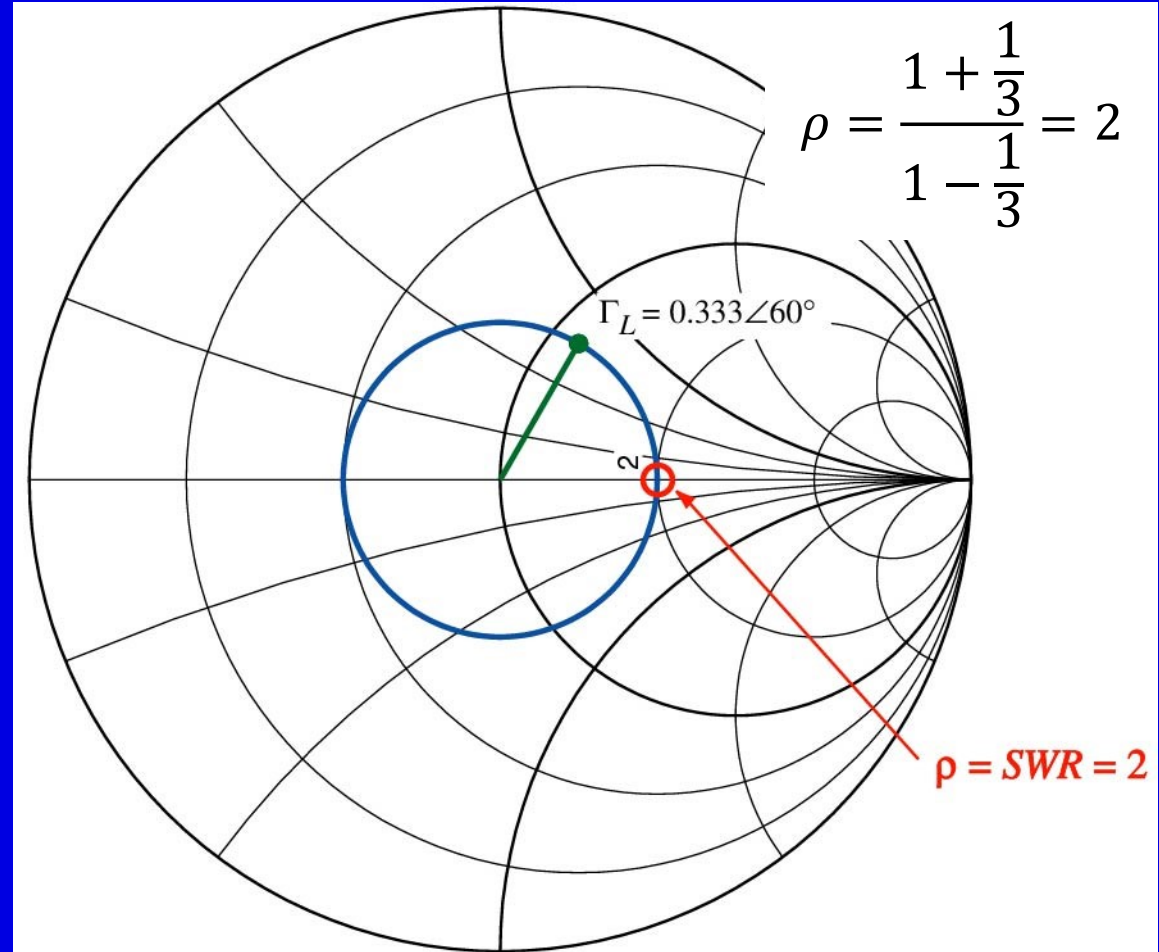


# Reading the Standing-Wave Ratio

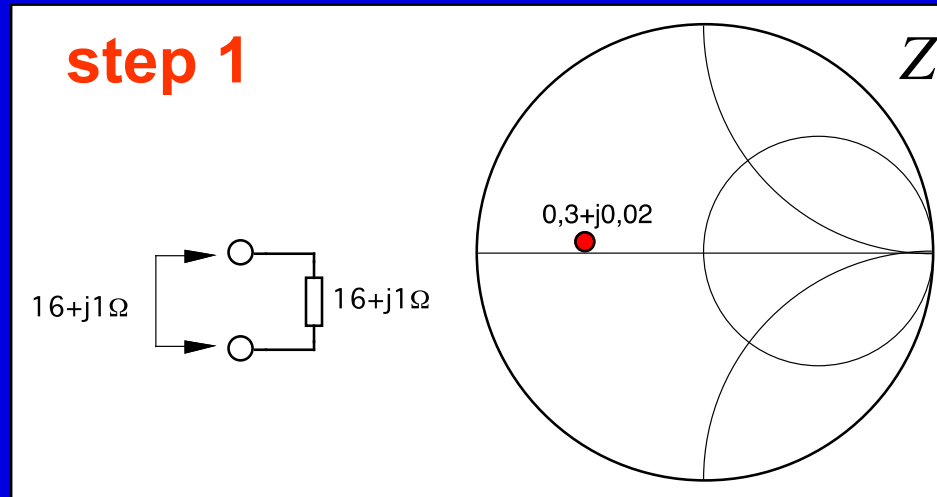
$$\begin{aligned}\rho = \text{SWR} &= \frac{|V_{\max}|}{|V_{\min}|} = \\ &= \frac{|I_{\max}|}{|I_{\min}|} = \frac{1 + |\Gamma|}{1 - |\Gamma|}\end{aligned}$$

$$r \geq 1, x = 0 :$$

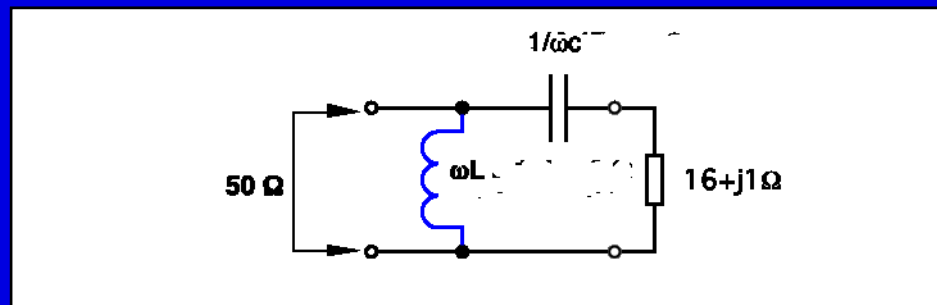
$$\rho = \frac{1 + \Gamma}{1 - \Gamma} = r$$



# Experiment: Design a matching network by using the Smith chart and the VNA

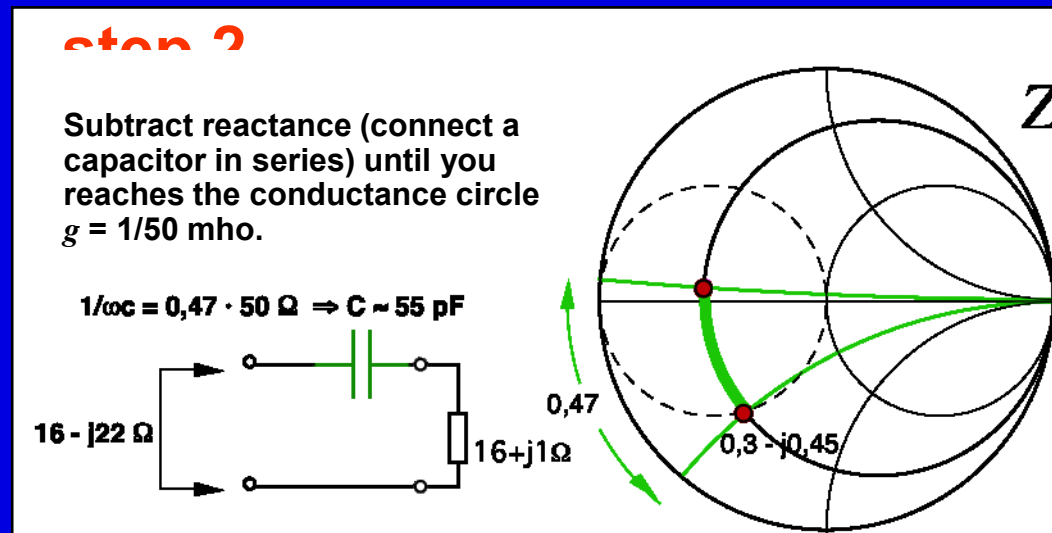


- ① Use the VNA to measure the load impedance
- ② Choose a network topology to match  $Z_L$  to  $50\Omega$  (note: infinite options, but let's try a simple high pass L-topology)



# Experiment: Design a matching network by using the Smith chart and the VNA

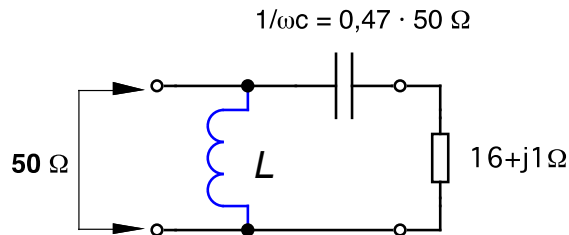
- ③ Determine the capacitance from the Smith Chart
- ④ Connect the capacitor
- ⑤ Verify the result by the VNA



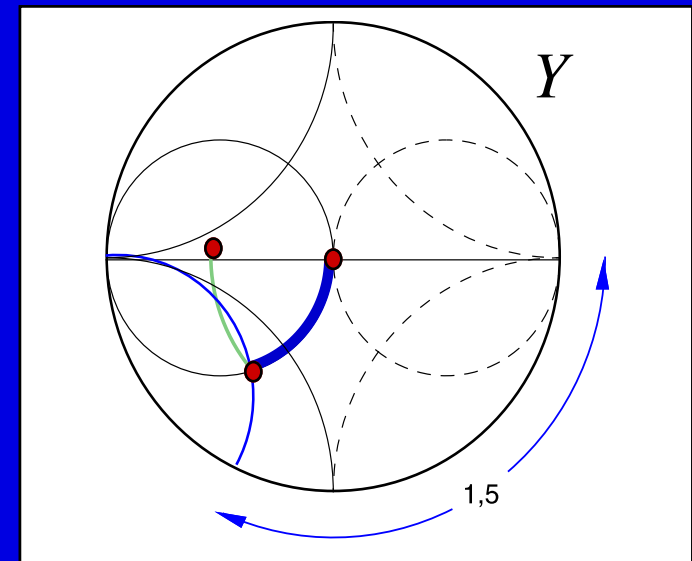
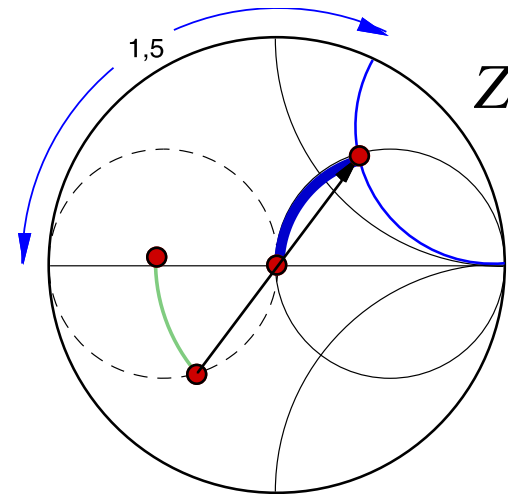
# Experiment: Design a matching network by using the Smith chart and the VNA

## step 3

Add susceptance (connect an inductor in parallel) until you end up in  $Y = Y_0 = 1/50 \text{ mho}$ .



$$\frac{1}{\omega L} = bY_0 \Rightarrow L = 42 \text{ nH}$$



- ⑥ Determine the inductance from the Smith Chart (you can use either the ordinary Z chart or the Y-Z chart)
- ⑦ Connect the inductor
- ⑧ Verify the result by the VNA

# Practice Connections in the Smith Chart

- No gain, without pain (headache)