RADIO SYSTEMS – ETIN15



Lecture no:

5

Digital modulation

Anders J Johansson, Department of Electrical and Information Technology anders.j.johansson@eit.lth.se

3 April 2017

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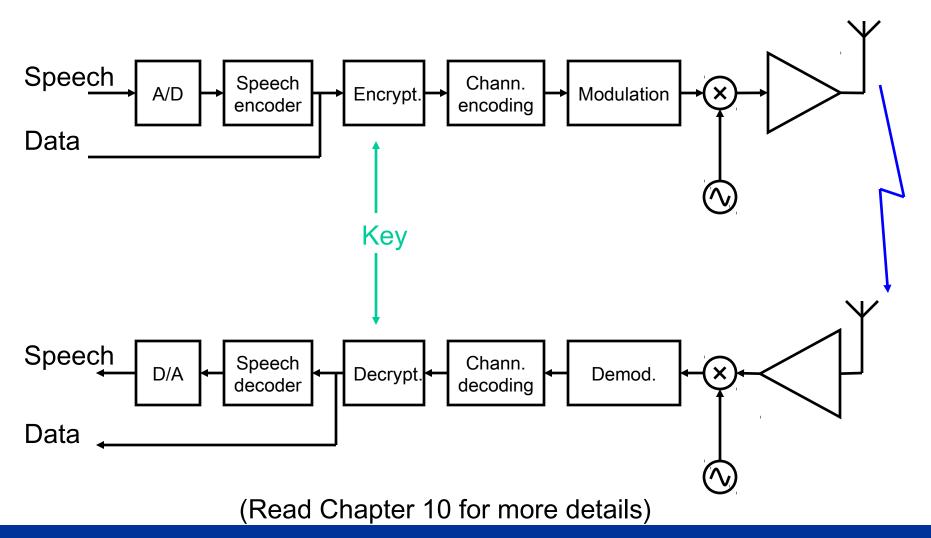


- Brief overview of a wireless communication link
- Radio signals and complex notation (again)
- Modulation basics
- Important modulation formats



STRUCTURE OF A WIRELESS COMMUNICATION LINK

A simple structure



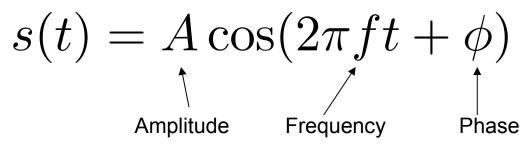
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RADIO SIGNALS AND COMPLEX NOTATION (from Lecture 3)

Simple model of a radio signal

A transmitted radio signal can be written

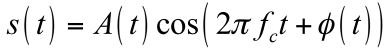


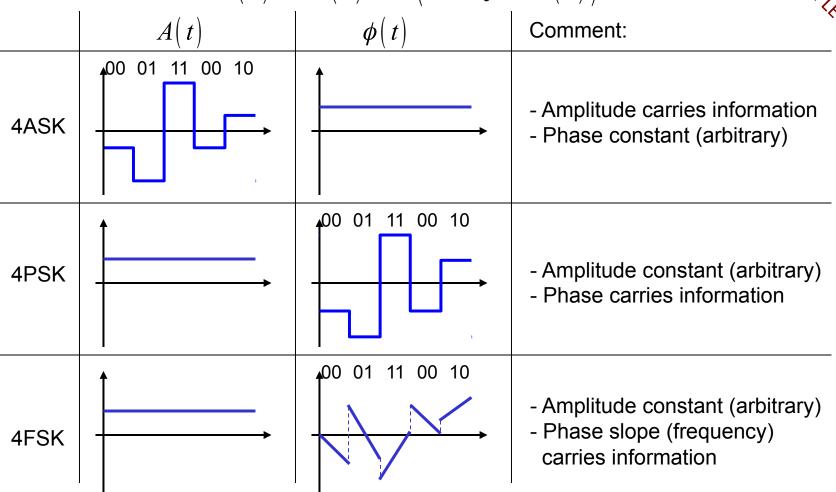
- By letting the transmitted information change the amplitude, the frequency, or the phase, we get the tree basic types of digital modulation techniques
 - ASK (Amplitude Shift Keying)
 - FSK (Frequency Shift Keying)
 - PSK (Phase Shift Keying)



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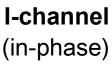
Example: Amplitude, phase and frequency modulation

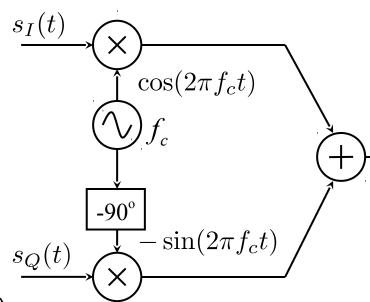




The IQ modulator

ON LECTURE





Transmited radio signal

$$s(t) = s_I(t) \cos(2\pi f_c t)$$

$$- s_Q(t) \sin(2\pi f_c t)$$

Q-channel

(quadrature)

Take a step into the complex domain:

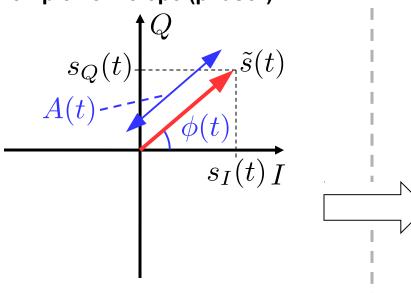
Complex envelope
$$\tilde{s}(t) = s_I(t) + j s_Q(t)$$

$$e^{j2\pi f_c t}$$

Interpreting the complex notation



Complex envelope (phasor)



Polar coordinates:

$$\tilde{s}(t) = s_I(t) + js_Q(t) = A(t)e^{j\phi(t)}$$

Transmitted radio signal

$$s(t) = \operatorname{Re} \left\{ \tilde{s}(t) e^{j2\pi f_c t} \right\}$$

$$= \operatorname{Re} \left\{ A(t) e^{j\phi(t)} e^{j2\pi f_c t} \right\}$$

$$= \operatorname{Re} \left\{ A(t) e^{j(2\pi f_c t + \phi(t))} \right\}$$

$$= A(t) \cos \left(2\pi f_c t + \phi(t) \right)$$

By manipulating the amplitude A(t) and the phase $\Phi(t)$ of the complex envelope (phasor), we can create any type of modulation/radio signal.

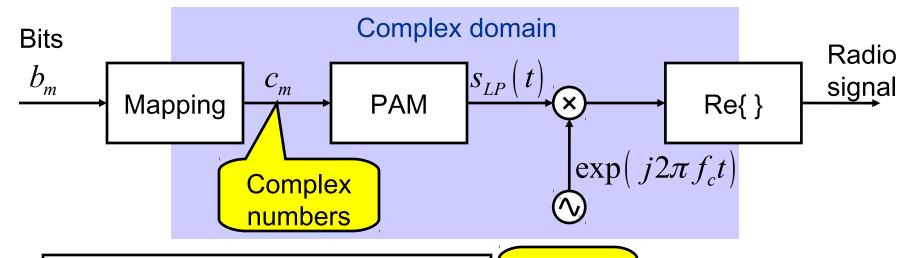
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MODULATION BASICS

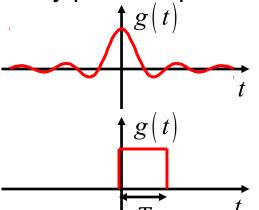
Pulse amplitude modulation (PAM) The modulation process





PAM:
$$s_{LP}(t) = \sum_{m=-\infty}^{\infty} c_m g(t - mT_s)$$
 Symbol time

Many possible pulses



"Standard" basis pulse criteria

$$\int_{-\infty}^{\infty} |g(t)|^2 dt = 1 \text{ or } = T_s$$
 (energy norm.)

$$\int_{-\infty}^{-\infty} g(t)g^*(t-mT_s)dt = 0 \text{ for } m \neq 0 \quad \text{(orthogonality)}$$

Pulse amplitude modulation (PAM) Basis pulses and spectrum



Assuming that the complex numbers c_m representing the data are independent, then the **power spectral density** of the base band PAM signal becomes:

$$S_{LP}(f) \sim \left| \int_{-\infty}^{\infty} g(t) e^{-j2\pi f t} dt \right|^{2}$$

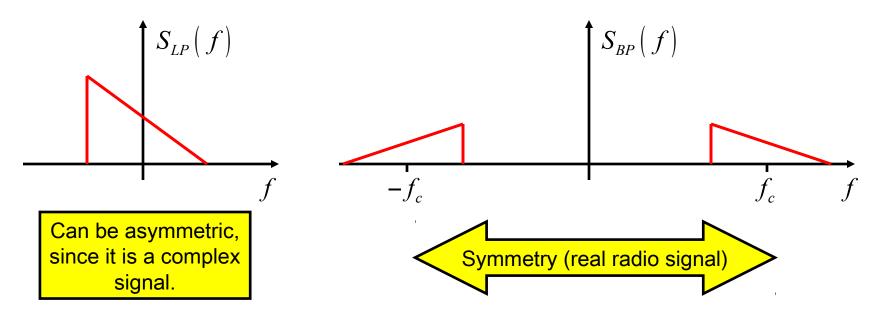
which translates into a radio signal (band pass) with

$$S_{BP}(f) = \frac{1}{2} \left(S_{LP}(f - f_c) + S_{LP}(-f - f_c) \right)$$

Pulse amplitude modulation (PAM) Basis pulses and spectrum



Illustration of power spectral density of the (complex) base-band signal, $S_{LP}(f)$, and the (real) radio signal, $S_{BP}(f)$.



What we need are basis pulses g(t) with nice properties like:

- Narrow spectrum (low side-lobes)
- Relatively short in time (low delay)

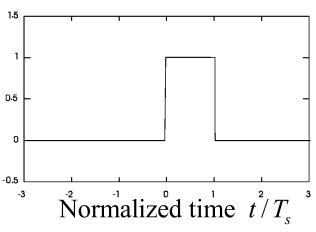
Pulse amplitude modulation (PAM) Basis pulses

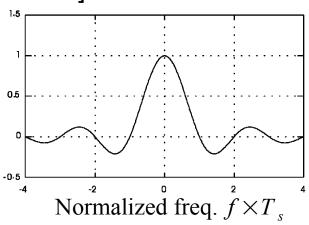




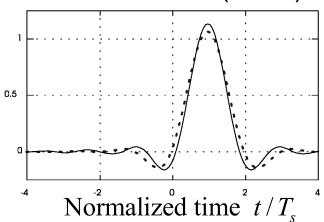
FREQ. DOMAIN

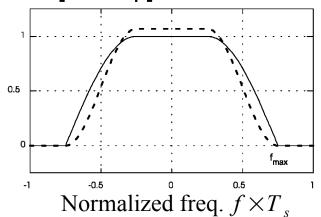
Rectangular [in time]





(Root-) Raised-cosine [in freq.]

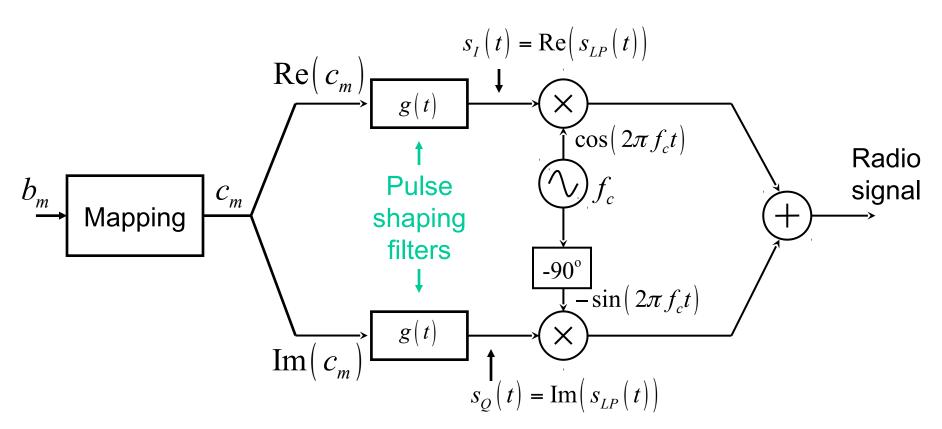




Pulse amplitude modulation (PAM) Interpretation as IQ-modulator

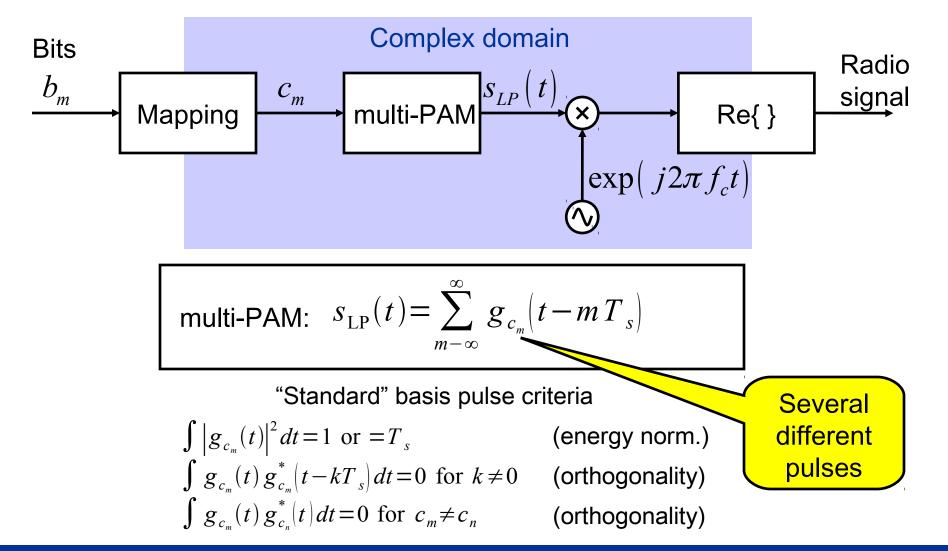


For real valued basis functions g(t) we can view PAM as:



(Both the rectangular and the (root-) raised-cosine pulses are real valued.)

Multi-PAM Modulation with multiple pulses



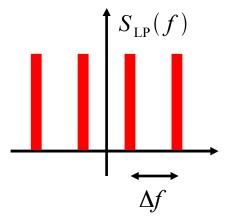
Multi-PAM Modulation with multiple pulses

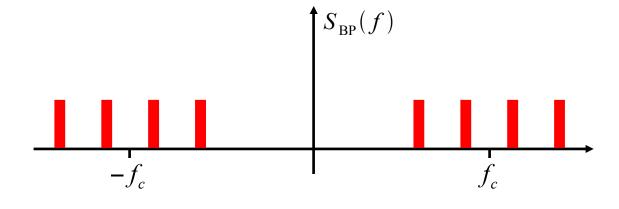


Frequency-shift keying (FSK) with M (even) different transmission frequencies can be interpreted as multi-PAM if the basis functions are chosen as:

$$g_k(t) = e^{-j\pi k\Delta f t}$$
 for $0 \le t \le T_s$

and for k = +/-1, +/-3, ..., +/-M/2

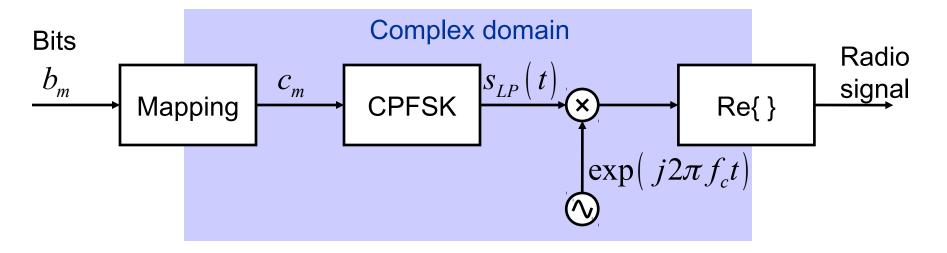




Bits: 00 01 10 11

Continuous-phase FSK (CPFSK) The modulation process





CPFSK:
$$s_{\text{LP}}(t) = A \exp(j \Phi_{\text{CPFSK}}(t))$$

where the amplitude A is constant and the phase is

$$\Phi_{\text{CPFSK}}(t) = 2\pi h_{\text{mod}} \sum_{m=-\infty}^{\infty} c_m \int_{-\infty}^{t} \tilde{g} \underbrace{(u - mT) du}_{\text{DI}}$$

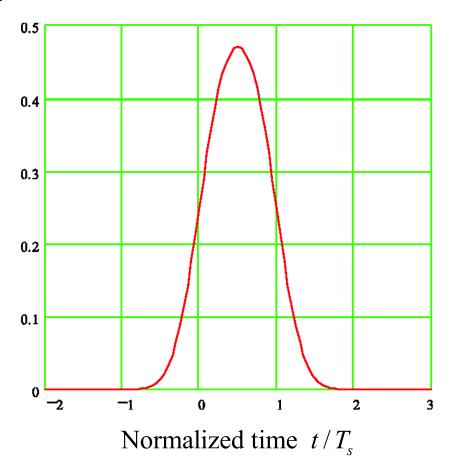
where h_{mod} is the modulation index.

Phase basis pulse

Continuous-phase FSK (CPFSK) The Gaussian phase basis pulse



In addition to the rectangular phase basis pulse, the Gaussian is the most common.



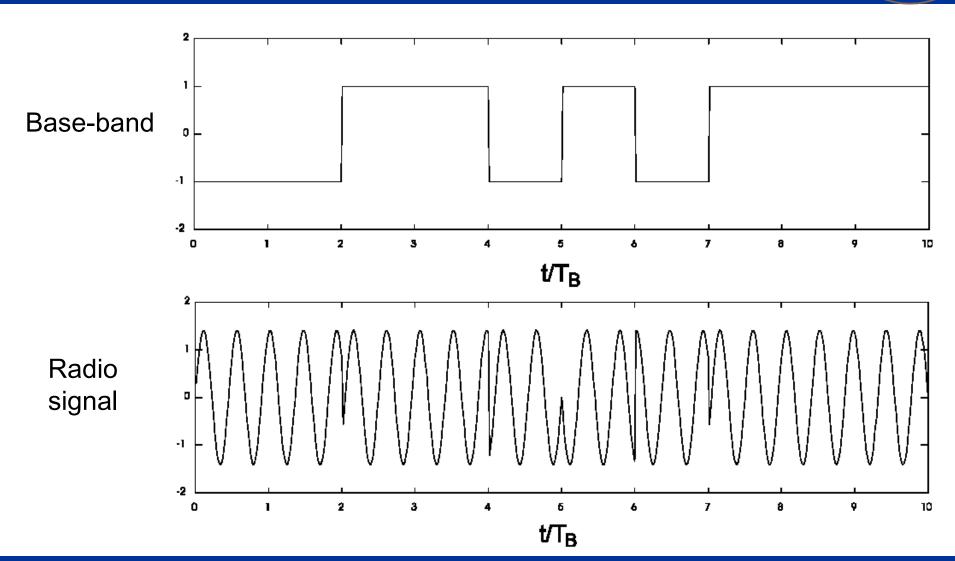
 $BT_s = 0.5$



IMPORTANT MODULATION FORMATS

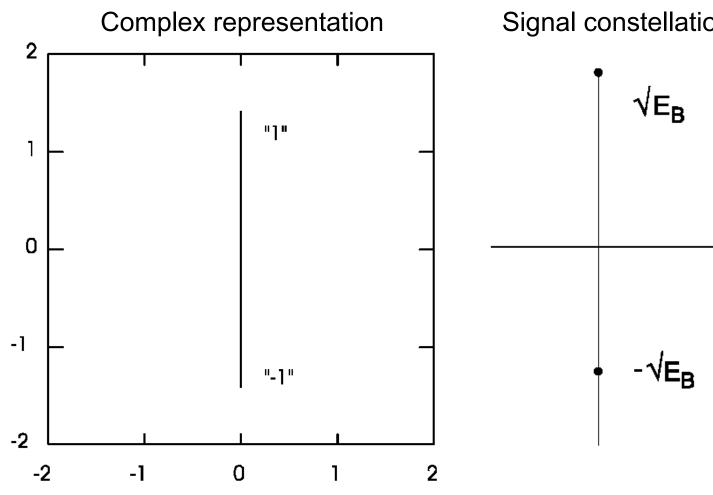
Binary phase-shift keying (BPSK) Rectangular pulses



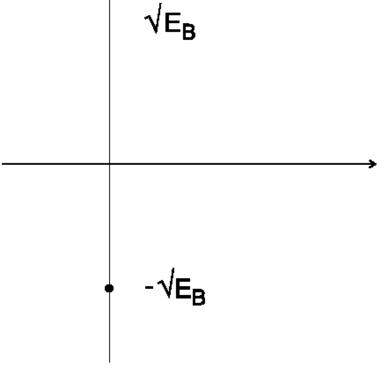


Binary phase-shift keying (BPSK) Rectangular pulses





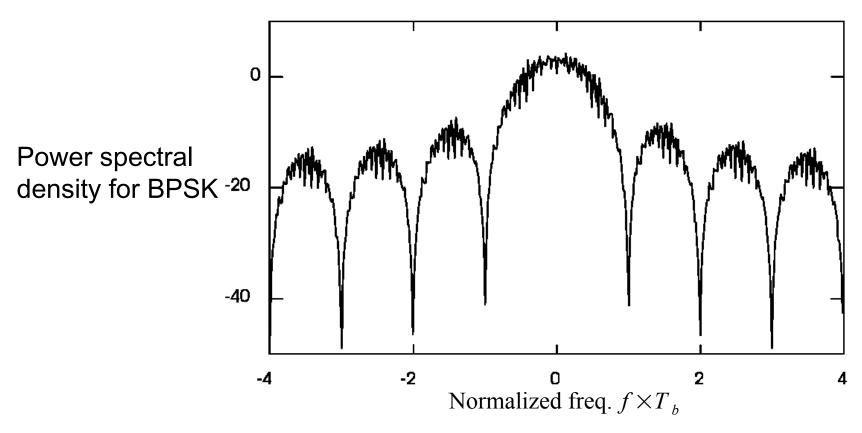
Signal constellation diagram



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Binary phase-shift keying (BPSK) Rectangular pulses

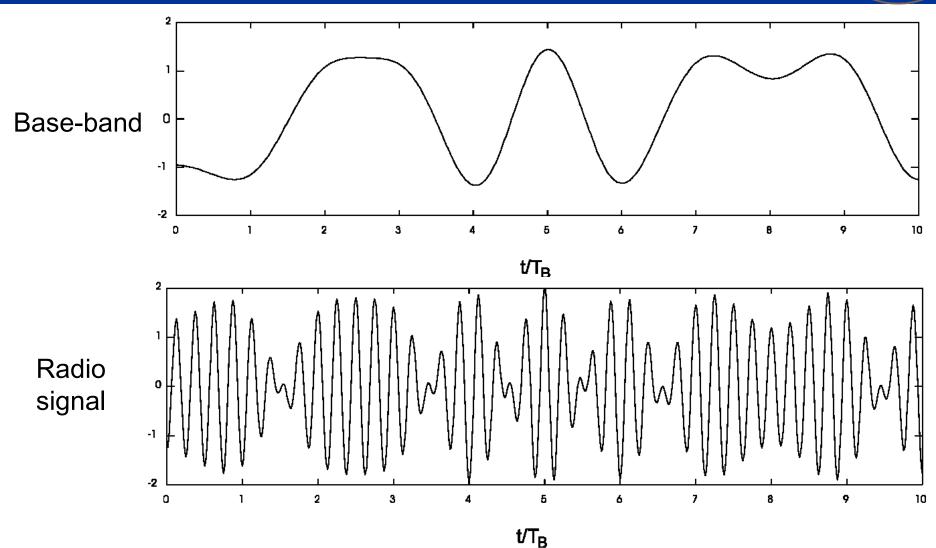




Contained percentage of total energy	spectral efficiency
90%	0.59Bit/s/Hz
99%	0.05Bit/s/Hz

Binary phase-shift keying (BPSK) Raised-cosine pulses (roll-off 0.5)

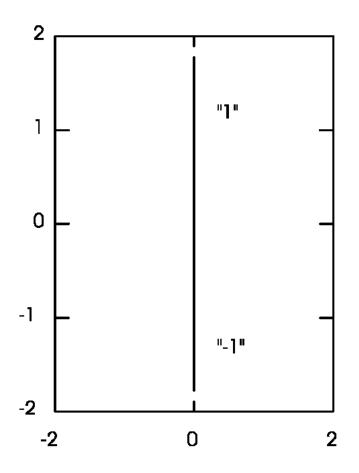




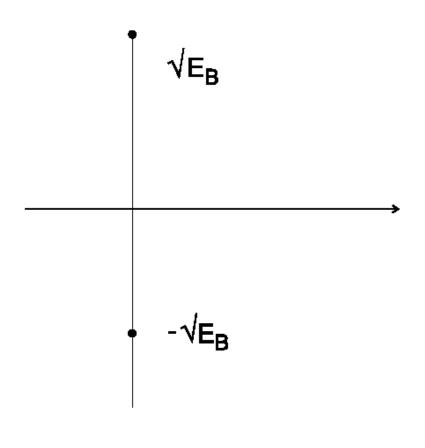
Binary phase-shift keying (BPSK) Raised-cosine pulses (roll-off 0.5)



Complex representation

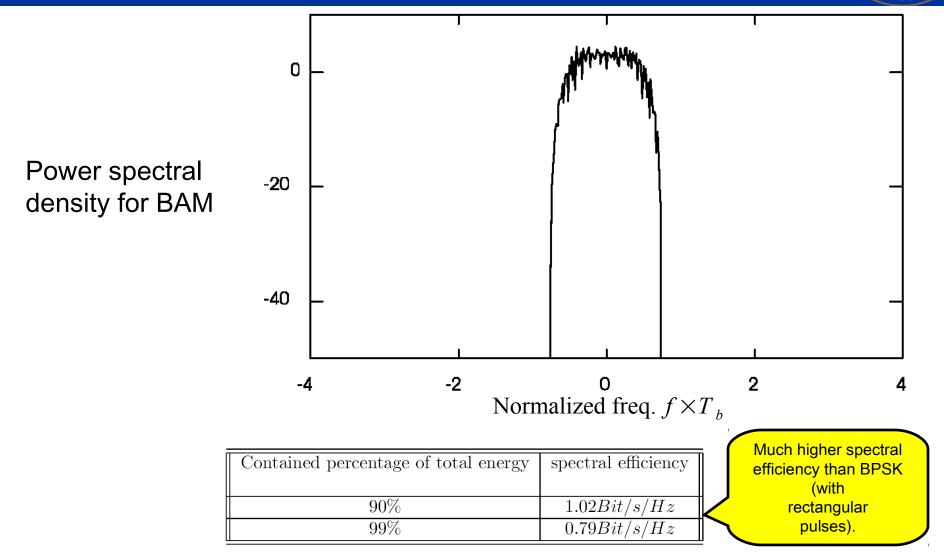


Signal constellation diagram



Binary phase-shift keying (BPSK) Raised-cosine pulses (roll-off 0.5)

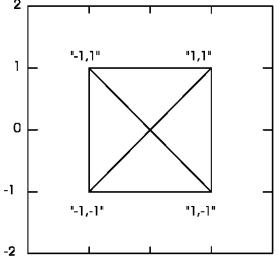




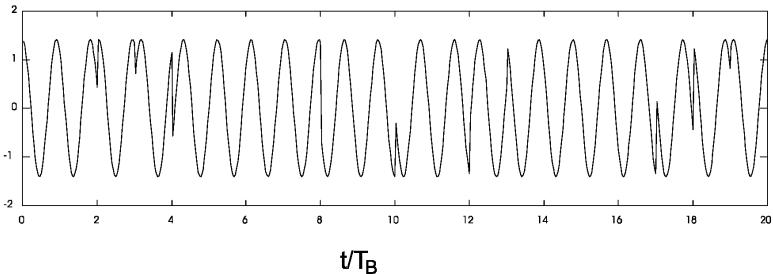
Quaternary PSK (QPSK or 4-PSK) Rectangular pulses







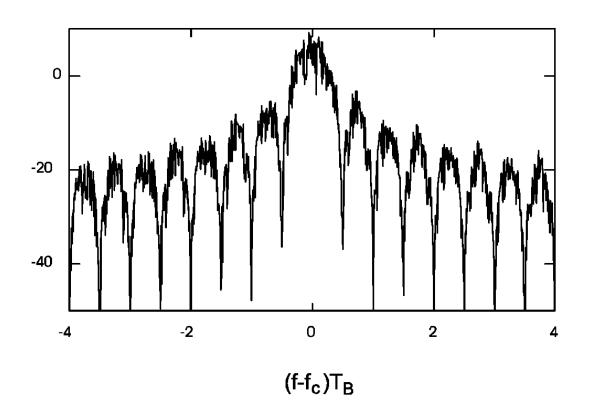
Radio signal



Quaternary PSK (QPSK or 4-PSK) Rectangular pulses



Power spectral density for QPSK



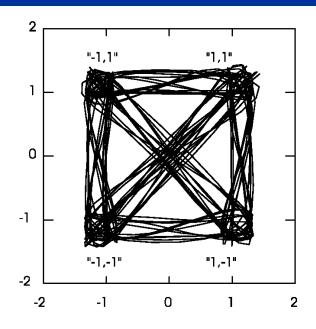
Cont	tained percentage of total energy	spectral efficiency
	90%	1,18Bit/s/Hz
	99%	0.10Bit/s/Hz

Twice the spectrum efficiency of BPSK (with rect. pulses). TWO bits/pulse instead of one.

Quadrature ampl.-modulation (QAM) Root raised-cos pulses (roll-off 0.5)



Complex representation



Contained percentage of total energy	spectral efficiency
0004	0.04D'1/-/H-
90%	$\begin{array}{c c} 2.04Bit/s/Hz \\ \hline 1.58Bit/s/Hz \end{array}$

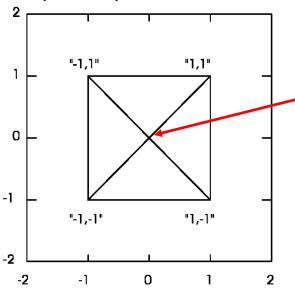
Much higher spectral efficiency than QPSK (with rectangular pulses).

Amplitude variations The problem



Signals with high amplitude variations leads to less efficient amplifiers.

Complex representation of QPSK



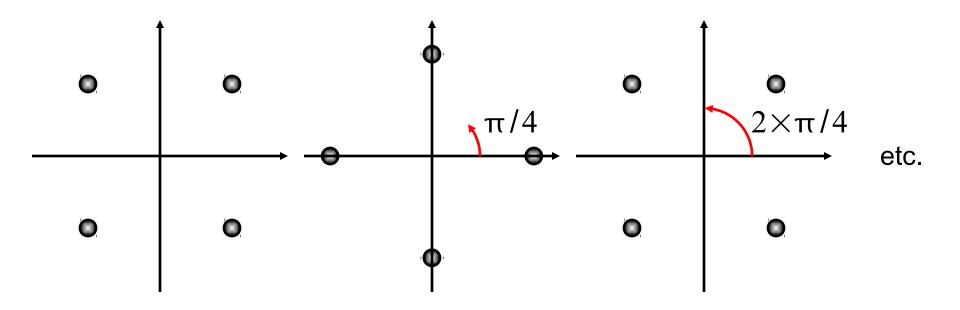
It is a problem that the signal passes through the origin, where the amplitude is ZERO. (Infinite amplitude variation.)

Can we solve this problem in a simple way?

Amplitude variations A solution



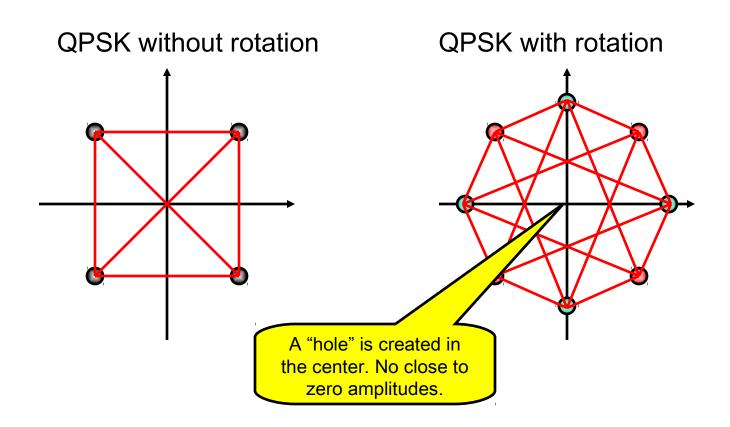
Let's rotate the signal constellation diagram for each transmitted symbol!



Amplitude variations A solution



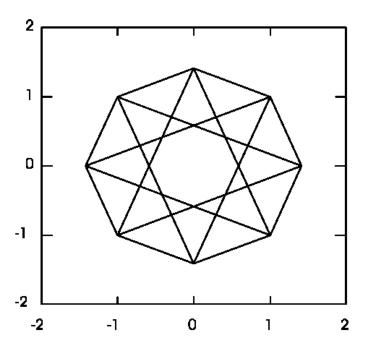
Looking at the complex representation ...



π / 4- Differential QPSK (DQPSK)

THE TOTAL TO

Complex representation



Still uses the same rectangular pulses as QPSK - the power spectral density and the spectral efficiency are the same.

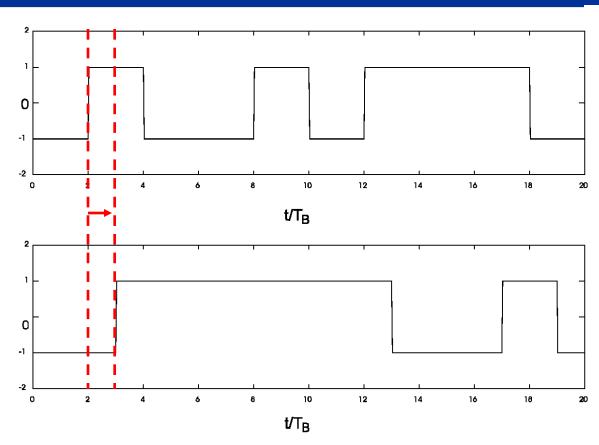
This modulation type is used in several standards for mobile communications (due to it's low amplitude variations).

Offset QPSK (OQPSK) Rectangular pulses



In-phase signal

Quadrature signal

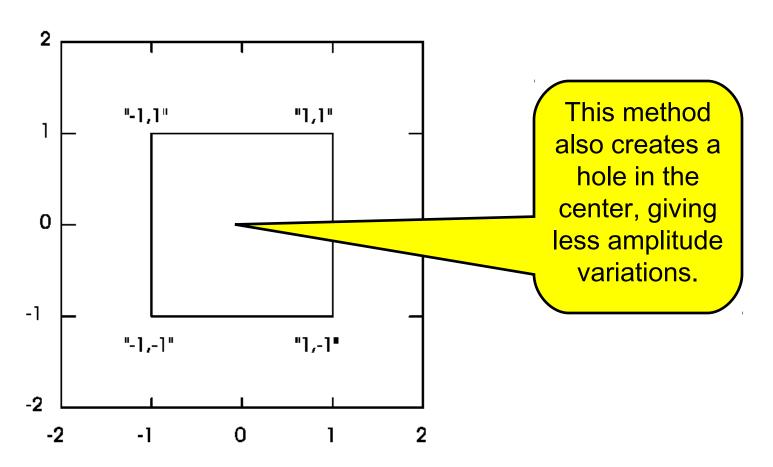


There is **one bit-time** offset between the in-pase and the quadrature part of the signal (a delay on the Q channel). This makes the transitions between pulses take place at different times!

Offset QPSK Rectangular pulses

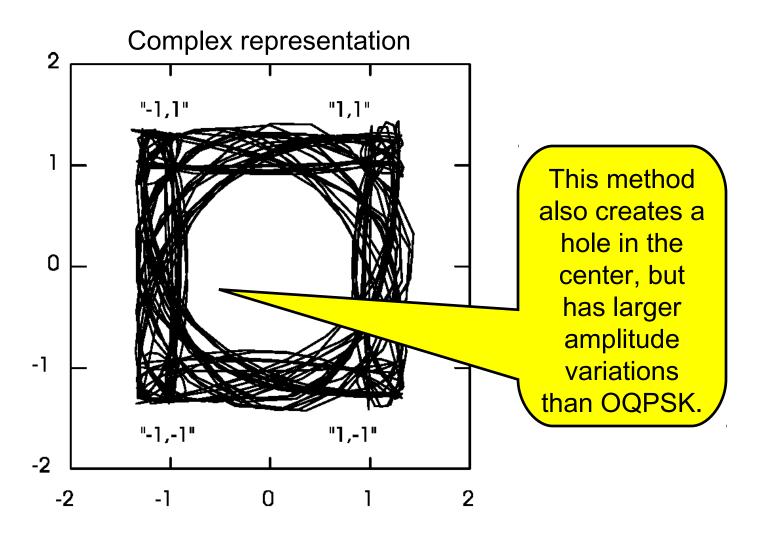


Complex representation



Offset QAM (OQAM) Raised-cosine pulses





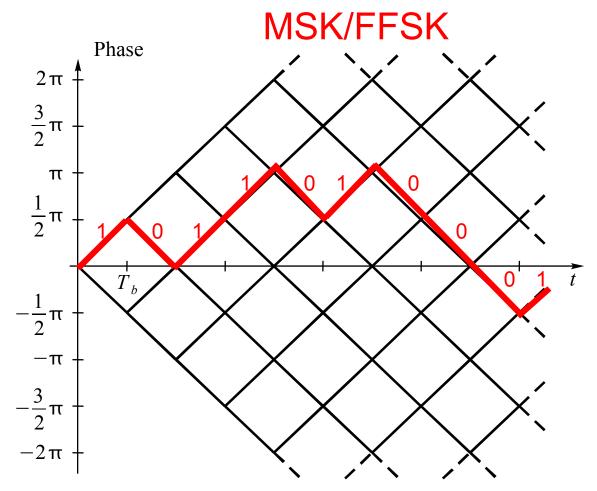
Continuous-phase modulation

Basic idea:

- Keep amplitude constant
- Change phase continuously

In this particular example we change the phase in a piecewise linear fashion by $\pm \pi/2$, depending on the data transmitted.

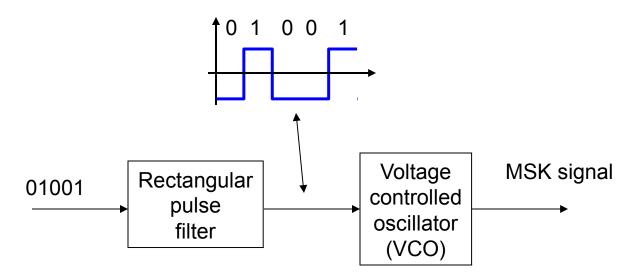
This type of modulation — can be interpreted both as phase and frequency modulation. It is called MSK (minimum shift keying) or FFSK (fast frequency shift keying).



Minimum shift keying (MSK)



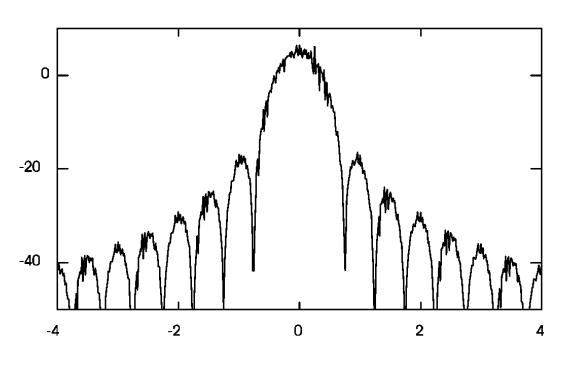
Simple MSK implementation



Minimum shift keying (MSK)



Power spectral density of MSK

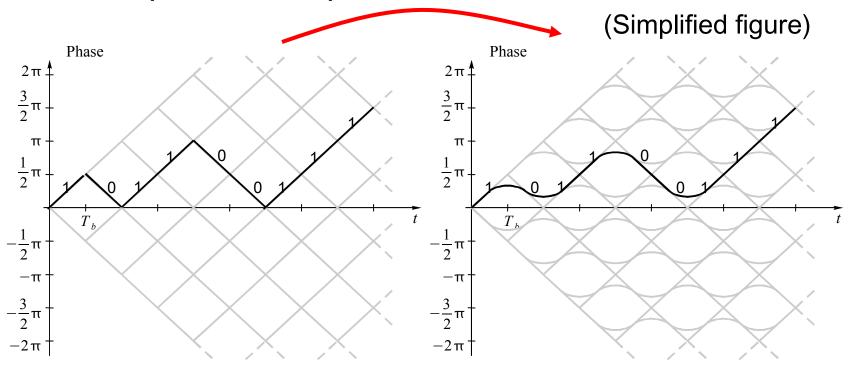


 $(f-f_c)T_B$

Contained percentage of total energy	spectral efficiency
90 %	$1,29 \; \mathrm{Bit} \; / \; \mathrm{s} \; / \; \mathrm{Hz}$
99 %	0,85 Bit / s / Hz



Further improvement of the phase: Remove 'corners'

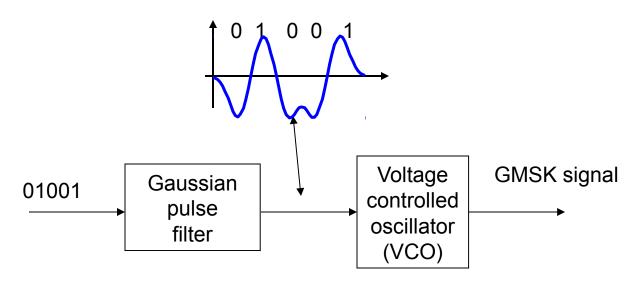


MSK (Rectangular pulse filter)

Gaussian filtered MSK - GMSK (Gaussian pulse filter)



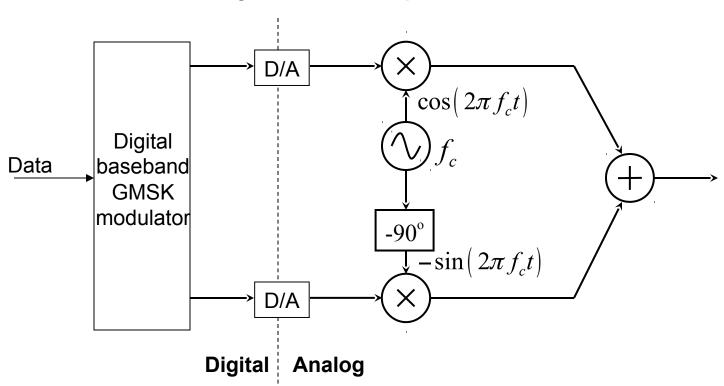
Simple GMSK implementation



When implemented this "simple" way, it is usually called **G**aussian filtered frequency shift keying (GFSK).

GSFK is used in e.g. Bluetooth.

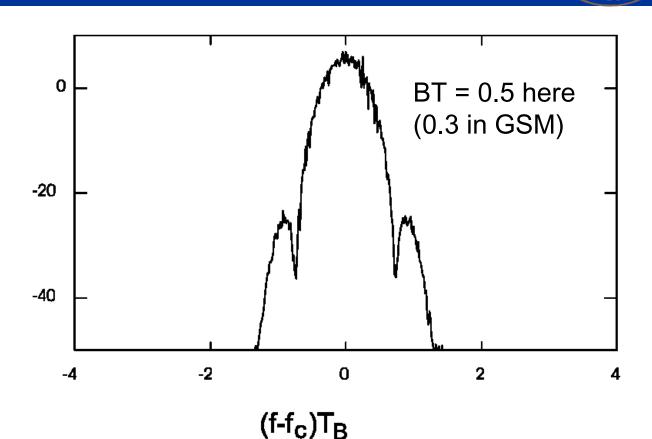
Digital GMSK implementation



This is a more precise implementation of GMSK, which is used in e.g. GSM.

W. Toologian Too

Power spectral density of GMSK.



Contained percentage of total energy	spectral efficiency
90~%	$1,45~\mathrm{Bit}$ / s / Hz
99 %	$0.97~\mathrm{Bit}~/~\mathrm{s}~/~\mathrm{Hz}$

How do we use all these spectral efficiencies?



Example:

Assume that we want to use MSK to transmit 50 kbit/sec, and want to know the required transmission bandwidth.

Take a look at the spectral efficiency table:

	Contained percentage of total energy	spectral efficiency
\llbracket	90 %	$1,29 \; \mathrm{Bit} \; / \; \mathrm{s} \; / \; \mathrm{Hz}$
	99~%	$0.85~\mathrm{Bit}$ / s / Hz

The 90% and 99% bandwidths become:

$$B_{90\%} = 50000/1.29 = 38.8 \text{ kHz}$$

$$B_{99\%} = 50000 / 0.85 = 58.8 \text{ kHz}$$

Summary



	Modulation method	spectral efficiency	spectral efficiency
		for 90 $\%$ of	for 99 % of
		total energy	total energy
		Bit / s / Hz	Bit / s / Hz
BPSK with	BPSK	0,59	0,05
root-raised —	\rightarrow BAM (α =0.5)	1,02	0,79
cosine pulses	QPSK, OQPSK,	1,18	0,10
puises	MSK	1,29	0,85
	$GMSK (B_G T= 0.5)$	1,45	0,97
	QAM ($\alpha = 0.5$)	2,04	1,58

TABLE 11.1 in textbook.