

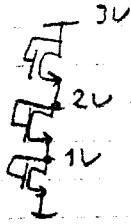
Solutions to the
written Exam in

Analog IC Design

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1) a) Neglecting the body effect, the transistors being identical, they will have the same voltage drop, that is



The current:

$$I_D = \frac{1}{2} \mu_n C_{ox} \frac{W}{L} (V_{GS} - V_T)^2 = \frac{1}{2} \cdot 115 \cdot 10^6 \cdot 10 \cdot (1 - 0,46)^2 = 0,17 \text{ mA}$$

b) With body effect the threshold voltages of the upper transistors would increase, increasing the voltage drop over those transistors, and reducing the current.
⇒ reduced node voltages and drain current.

2a

$$V_{GS} : V_{ov8} = \sqrt{\frac{2I_{BIAS}}{\mu_n C_{ox} (W/L)_8}} = \sqrt{\frac{100 \mu A}{40 \mu \cdot 40}} = 0,25 V$$

$$V_{GS} = V_{DD} + V_{tp0} - V_{ov8} = 3 - 0,60 - 0,25 = \underline{2,15 V}$$

Assume M_5, M_7 & M_2 in saturation \Rightarrow

$$I_{DS} \approx I_{D8} = \underline{50 \mu A}, \quad I_{D7} = I_{D2} = \frac{1}{2} I_{DS} = \underline{25 \mu A}$$

$$V_{ov5} = V_{ov8} = \sqrt{2} \cdot V_{ov7} = \sqrt{2} \cdot V_{ov2} \Rightarrow$$

$$V_{ov5} = 0,25, \quad V_{ov1} = V_{ov2} = 0,18 V$$

$$V_{S1,2} = V_I - V_{tp0} + V_{ov1} = 1,5 + 0,60 + 0,18 = \underline{2,28 V} = V_{DS}$$

$$V_{GDS} = 2,15 - 2,28 = -0,13 V > V_{tp0} = -0,60 \Rightarrow M_5 \text{ in saturation}$$

(if assumption M_1, M_2 in saturation is valid)

$$V_{ov3,4} = \sqrt{\frac{2I_{D3}}{\mu_n C_{ox} (W/L)_3}} = \sqrt{\frac{2 \cdot 25 \mu}{115 \mu \cdot 8}} = 0,23 V$$

$$V_{D3} = V_{G10} + V_{ov3} = 0,46 + 0,23 = \underline{0,69 V} \Rightarrow M_7 \text{ in saturation}$$

$$I_{D7} \approx I_{BIAS} \cdot \frac{(W/L)_7}{(W/L)_8} = 50 \mu A \cdot 2,5 = \underline{125 \mu A}$$

$$V_{ov6} = \sqrt{\frac{2I_{D6}}{\mu_n C_{ox} (W/L)_6}} = \sqrt{\frac{2I_{D7}}{\mu_n C_{ox} (W/L)_6}} = \sqrt{\frac{250 \mu}{115 \mu \cdot 40}} = 0,233$$

$$\Rightarrow V_{D4} = V_{G10} + V_{ov6} = \underline{0,69 V} (= V_{D3}) \Rightarrow M_2 \text{ in saturation}$$

The assumption that all transistors are in saturation is valid.

b

$$BW = \frac{g_{m1}}{C_c}$$

$$g_{m1} = \sqrt{2 \mu_p C_{ox} \left(\frac{W}{L}\right)_1 I_{D1}} = \sqrt{2 \cdot 40 \mu \cdot 40 \cdot 25 \mu} = 0,28 \text{ mS}$$

$$\rightarrow BW = \frac{0,28 \text{ m}}{2 \text{ p}} = 2\pi \cdot 22 \text{ M} = 22 \text{ MHz}$$

$$c. \quad g_{m6} = \sqrt{2 \mu_n C_{ox} \left(\frac{W}{L}\right)_6 I_{D6}} = \sqrt{2 \cdot 115 \mu \cdot 40 \cdot 125 \mu} = 1,1 \text{ mS}$$

$$P_2 \approx -\frac{g_{m6}}{C_1 + C_2} = -\frac{1,1 \text{ m}}{5,6 \text{ p}} = -2\pi \cdot 30,5 \text{ M} = -30 \text{ MHz}$$

$$Z = \frac{1}{\left(\frac{1}{g_{m6}} - R_2\right) \cdot C_c} = \text{close to } \infty, \text{ ignore}$$

$$\phi_m = 90^\circ - \arctan\left(\frac{22 \text{ M}}{30 \text{ M}}\right) = 54^\circ$$

3.

$$C = 2 \text{ pF} = 2000 \text{ fF}$$

$$\text{poly 1 - poly 2} : 0,86 \text{ fF}/(\mu\text{m})^2, 0,082 \text{ fF}/\mu\text{m}$$

assume quadratic shape with side a (μm) \Rightarrow

$$C = 0,86 \cdot a^2 + 4a \cdot 0,082 a \text{ fF} = 2000 \Rightarrow a = 48 \mu\text{m}$$

$$C_{\text{bottom}} = 48^2 \cdot 0,119 + 48 \cdot 4 \cdot 0,052 \text{ fF} = 284 \text{ fF}$$

$$\text{ratio} = \frac{284}{2000} = 14\%$$

m2-m3-m4 :

$$C \sim \frac{1}{t_{\text{ox}}}, C_{\text{polys}} = 0,86 \text{ fF}/(\mu\text{m})^2, t_{\text{pox}} = 41 \text{ nm} \Rightarrow$$

$$t_{\text{max2}} = 1,00 \mu\text{m} \Rightarrow C_{\text{m2-m3}} = 0,86 \cdot \frac{41}{1000} = 0,035 \text{ fF}/(\mu\text{m})^2$$

$$t_{\text{max3}} = 1,00 \mu\text{m} \Rightarrow C_{\text{m3-m4}} = 0,035 \text{ fF}/(\mu\text{m})^2$$

$$C = (0,035 + 0,035) a^2 \text{ fF} \Rightarrow a = \sqrt{\frac{2000}{0,070}} = 169 \mu\text{m}$$

$$C_{\text{bottom}} = 169^2 \cdot 0,012 + 4 \cdot 169 \cdot 0,036 = 367 \text{ fF}$$

$$\text{ratio} = \frac{367}{2000} = 18\%$$

p1-m1-m2-m3-m4 :

$$t_{\text{max}} = 1,00 \mu\text{m} \Rightarrow C_{\text{m1-m2}} = 0,035 \text{ fF}/(\mu\text{m})^2$$

$$t_{\text{pox}} = 0,645 \mu\text{m} \Rightarrow C_{\text{m1-p1}} = 0,055 \text{ fF}/(\mu\text{m})^2$$

$$a = \sqrt{\frac{2000}{0,070 + 0,035 + 0,055}} = 112 \mu\text{m}$$

$$C_{\text{bottom}} = 112^2 \cdot 0,119 + 4 \cdot 112 \cdot 0,052 = 1,5 \text{ pF}$$

$$\text{ratio} = \frac{1,5}{2} = 76\%$$

Conclusion : The area becomes much larger without the poly1-poly2 option. It is possible to achieve almost the same $C_{\text{bottom}} / C_{\text{desired}}$ without poly2, but at a severe area penalty.

4

$$a) I_d = \mu_n C_{ox} \frac{W}{L} \left((V_{GS} - V_t) V_{DS} - \frac{V_{DS}^2}{2} \right) \approx \mu_n C_{ox} \frac{W}{L} (V_{GS} - V_t) V_{DS}$$

for small V_{DS}

$$\Rightarrow R = \frac{1}{\frac{\partial I_d}{\partial V_{DS}}} = \frac{1}{\mu_n C_{ox} \frac{W}{L} (V_{GS} - V_t)} = \frac{1}{115 \cdot 10^{-6} \cdot \frac{W}{L} \cdot 2} = 1 \text{ M}\Omega \Rightarrow$$

$$\frac{L}{W} = 230$$

$$\text{Gate-channel capacitance} < 1 \text{ pF} \Rightarrow C_{gc} = C_{ox} W L < 2 \text{ pF}$$

$$\Rightarrow W L < \frac{2000}{4,6} (\mu\text{m})^2 = 434 (\mu\text{m})^2$$

$$\begin{cases} W L = 434 \\ \frac{L}{W} = 230 \end{cases} \Rightarrow \begin{cases} W \cdot 230 W = 434 \\ L/W = 230 \end{cases} \Rightarrow \begin{cases} W = 1,35 \mu\text{m} \\ L = 310,5 \mu\text{m} \end{cases}$$

$$b) I_d = \mu_n C_{ox} \frac{W}{L} \left[(V_{GS} - V_t) V_{DS} - \frac{V_{DS}^2}{2} \right] =$$

$$= \mu_n C_{ox} \frac{W}{L} \left[(V_{DD} - V_{CM} + \frac{V_d}{2} - V_t) V_d - \frac{V_d^2}{2} \right] =$$

$$= \mu_n C_{ox} \frac{W}{L} [V_{DD} - V_{CM} - V_t] \cdot V_d, \text{ linear function of } V_d. \\ \text{(in triode region)}$$

$$c) R_{nom} = \frac{1}{\mu_n C_{ox} \frac{W}{L} (V_{DD} - V_{CM_{nom}} - V_t)}$$

$$R = \frac{1}{\mu_n C_{ox} \frac{W}{L} (V_{DD} - V_{CM} - V_t)}$$

$$\frac{R}{R_{nom}} = \frac{V_{DD} - V_{CM_{nom}} - V_t}{V_{DD} - V_{CM} - V_t} = 1,2 \Rightarrow \frac{3 - 1 - 0,46}{3 - V_{CM} - 0,46} = \frac{1,54}{2,54 - V_{CM}} = 1,2$$

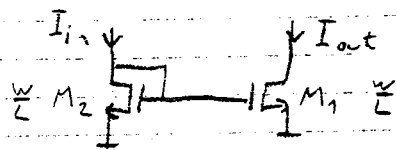
$$\Rightarrow 1,54 = 3,048 - 1,2 V_{CM} \Rightarrow V_{CM} = 1,26 \text{ V}$$

$$\frac{R}{R_{nom}} = 0,8 \Rightarrow \frac{1,54}{2,54 - V_{CM}} = 0,8 \Rightarrow 1,54 = 2,032 - 0,8 V_{CM} \Rightarrow V_{CM} = 0,62 \text{ V}$$

$\Rightarrow V_{CM}$ must be between 0,62 V and 1,26 V for

the resistance to stay within 20% of the nominal.
(of course process variations must be added to this...)

5. Since $V_{out, min}$ is just 200 mV, a simple current mirror should be used:



To minimize noise, use maximum overdrive = $V_{out, min} = 200$ mV

$$I_{in} = \frac{1}{2} \mu_n C_{ox} \left(\frac{W}{L}\right)_2 V_{ov2}^2 \Rightarrow \left(\frac{W}{L}\right)_2 = \frac{2I_{in}}{\mu_n C_{ox} V_{ov}^2} = \frac{200 \mu}{115 \mu \cdot 0,2^2} = 44$$

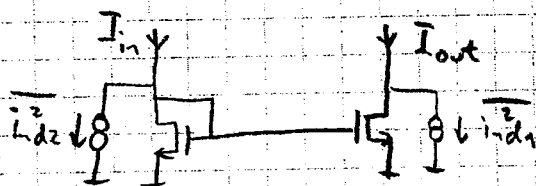
$$r_{out} = r_{dsn} \cdot \frac{L}{I_{out}} \Rightarrow L = \frac{r_{out}}{r_{dsn}} \cdot I_{out} = \frac{1M}{55} \cdot 100 \mu = 1,8 \mu m$$

choose $L = 2 \mu m$ & $W = 88 \mu m$, 4 fingers

$$C_{out} = C_{db1} + C_{dg1} < \frac{W}{2} \cdot 1,2 \mu m \cdot 0,93 \text{ fF}/\mu m^2 + 2,4 \mu m \cdot 0,28 \text{ fF}/\mu m^2 + W \cdot C_{sdo} =$$

$$= 49,1 \text{ fF} + 0,7 \text{ fF} + 18,5 \text{ fF} = 68 \text{ fF} < 0,1 \text{ pF}, \text{ OK}$$

Calculate the output noise:



The noise $\overline{i_{ind2}}$ is mirrored to the output by the unity gain current mirror \Rightarrow

$$\text{total output noise } \overline{i_{out}^2} = \overline{i_{ind1}^2} + \overline{i_{ind2}^2} =$$

$$= 4kT \gamma g_{m1} + 4kT \gamma g_{m2} = \left\{ g_{m1} = g_{m2}, \gamma_1 = \gamma_2 = \frac{2}{3} \right\} = \frac{16}{3} kT \gamma g_m$$

$$g_m = \frac{2I_d}{V_{ov}} = \frac{200 \mu}{0,2} = 1 \text{ mS}$$

$$\Rightarrow \overline{i_{ind}^2} = \frac{16}{3} \cdot 1,38 \cdot 10^{-23} \cdot 300 \cdot 1 \text{ m} = 2,2 \cdot 10^{-23} \text{ A}^2/\text{Hz}$$

in the range 10 kHz to 100 kHz:

$$\overline{i_{ind}^2} (10k-100k) = 2,2 \cdot 10^{-23} \text{ A}^2/\text{Hz} \cdot 90 \text{ kHz} = 1,99 \cdot 10^{-18} \text{ A}^2$$

$$\underline{i_{n, rms} = \sqrt{1,99 \cdot 10^{-18}} = 1,4 \text{ nA} < 2 \text{ nA}, \text{ OK}}$$