- 1. Ballistic Transport in QWFET
 - a. (2p) $E_n = \frac{\hbar^2 \pi^2 n^2}{2m^* t_w} \rightarrow E_1 = 0.38 \text{ eV}, E_2 = 1.51 \text{ eV}$

b. (3p)
$$C_{ox} = 0.035 \text{ F/m}^2$$
, $C_C = 0.069 \text{ F/m}^2$, $C_q = 0.027 \text{ F/m}^2$

In on-state $C_G = \left(\frac{1}{c_{ox}} + \frac{1}{c_C} + \frac{1}{c_q}\right)^{-1} = 0.013 \text{ F/m}^2.$

However, in saturation $C_G = \left(\frac{1}{c_{ox}} + \frac{1}{c_C} + \frac{2}{c_q}\right)^{-1} = 0.0085 \text{ F/m}^2$. The question was not clear on what was asked for, so both answers are correct. However, the result in saturation should be used in d-f.

c. (3p) As the drain bias increases, the drain fermi level is pulled down and less and less carriers will be injected from the drain into the channel. The reason is that the top of the band in the channel ends up further and further above the drain fermi level where in the limit a negligible amount of electrons reside. Then the only carriers in the channel will be the carriers injected from the source traveling from source to drain. Assuming no short channel effects, this amount of electrons is not affected by further change in drain bias, thus the current saturates.

d. (3p).
$$V_T = 3.0 - 3.2 + 0.38 V = 0.18 V$$
. $V_{ds,sat} = \frac{V_{gs} - V_T}{1 + \frac{C_q}{2C'_{ox}}} = 0.21 V < V_{DS} \rightarrow Yes$.

e. (2p)
$$I_{DS} = T * I_{DS, ballistic} = 0.6*15.7 \text{mA} = 10 \text{ mA}$$

f. (2p)
$$g_m = \frac{\partial I_{DS}}{\partial V_{GS}} = \frac{\partial}{\partial V_{GS}} (T * I_{DS, ballistic}) = 44 \text{ mS}$$

- 2. High frequency operation
 - a. (4p) Implicitly assumes operation in saturation \rightarrow Use C_q/2 \rightarrow C_G = 0.0082 F/m² \rightarrow C_{gg} = C_G*W*L_G = 7.4 fF. $f_T = \frac{C_{gg}}{2\pi g_m} = 1.2$ THz (1190 GHz)
 - b. (6p) $R_s = R_D = 62$ Ohm. ($R_{contact} = 16 \Omega$, $R_{access} = 3.1 \Omega$, $R_{spacer} = 43 \Omega$). The undoped spacer region is the main contributor to the resistance.

$$\rho_{s,access} = \frac{1}{\sigma_{s,access}} = \frac{1}{qn_{access}\mu_{access}} = 1.25 * 10^{-5} \Omega m$$

$$\rho_{s,spacer} = \frac{1}{\sigma_{s,spacer}} = \frac{1}{qn_{spacer}\mu_{spacer}} = 5.2 * 10^{-4} \Omega m$$

$$R_{SH} = \frac{\rho_{s,access}}{t_w} = 2080 \ \Omega, L_T = \sqrt{\frac{\rho_\sigma}{R_{SH}}} = 69 \ nm$$

$$\begin{split} R_{contact} &= \frac{\sqrt{R_{SH}\rho_{\sigma}}}{W} \operatorname{coth} \left(\frac{L_{C} = 100 \ nm}{L_{T} = 69 \ nm} \right) = 16 \ \Omega \\ R_{access} &= \frac{\rho_{s,access}L_{access}}{t_{w}W} = \frac{1.25E - 5 \times 15 nm}{6 nm \times 10 \mu m} = 3.1 \ \Omega \\ R_{spacer} &= \frac{\rho_{s,spacer}L_{spacer}}{t_{w}W} = \frac{5.2E - 4 \times 5 nm}{6 nm \times 10 \mu m} = 43 \end{split}$$

- c. (5p) $C_{gg} = C_{gg,0}$ (from 2a) + $C_{gs,p}$ + $C_{gd,p}$ = 17.4 fF. Add $R_S = R_D = 62$ Ohm \rightarrow f_T = 138 GHz.
- 3. Power gain
 - a. (2 p) The finite transconductance of the channel in a ballistic transistor induces a phase shift between input (gate) and output (drain) as well as limiting the power transfer. This is modelled by a channel resistance R_i.
 - b. (5 p) Parameters excluding R_G, R_D, and R_S:

$$y_{11} = \left(\frac{1}{j\omega C_{gs}} + R_i\right)^{-1} + j\omega C_{gd}$$

$$y_{12} = -j\omega C_{gd}$$

$$y_{21} = \frac{g_m}{1 + j\omega C_{gs} R_i} - j\omega C_{gd}$$

$$y_{22} = g_d + j\omega C_{gd}$$

$$\Rightarrow Y = \begin{bmatrix} 0.0010 + 0.011j & -0.0031j \\ 0.040 - 0.0084j & 0.0050 + 0.0031 \end{bmatrix}$$

$$\Rightarrow Z = \begin{bmatrix} 17.26 - 28.1j & 17.6 + 0.16j \\ 49.1 + 219j & 58.8 - 6.1j \end{bmatrix}$$

Add
$$Z_{res} = \begin{bmatrix} 70 & 50 \\ 50 & 100 \end{bmatrix} \rightarrow Z' = Z + Z_{res} = \begin{bmatrix} 87 - 28j & 68 + 0.16j \\ 99 + 219j & 159 - 6.1j \end{bmatrix}$$

- c. (2 p) Using z-parameters including R_s , R_D and $R_G \rightarrow k = 1.29 > 1$. Yes, it is stable.
- d. (2 p) For a stable device, use MAG. Use z_{21} and $z_{12} \rightarrow MAG = 1.68 = 2.25 \text{ dB}$.
- e. (4 p) $f_T = 140 \text{ GHz} \rightarrow f_{max} = 195 \text{ GHz}$ using model including R_i (197 GHz with standard model). Except for increasing f_T more, one could work on reducing R_G and g_d as well as Cgd.
- 4. Designing a Low noise amplifier
 - a. (3 p) $\omega_T = \frac{g_m}{c_{as}} = 1.9 THz$, $\omega = 314 GHz \ll \omega_T$, $Z_{opt} = 351 + j303 \rightarrow z_{opt} = 7 + j303 \rightarrow z_{o$ i6

 $F_{\rm min} = 1.25 \rightarrow NF = 0.96 \, dB$

b. (5 p) The distance from Z₀ (center) to Z_{opt} is 6.5 cm in the Smith chart. Draw a circle with this radius and find the intercept going from Z_{opt} "towards generator" (i.e. clockwise) with the "admittance = 1" at $z_1 = 0.09 - 0.28j$. The angle between these corresponds to a phase shift (read scales) from 0.239 λ to 0.457 λ = 0.218 λ . The length of the microstrip TRL should thus be $l_{phys} = \frac{0.218}{\beta} = 0.218 * \frac{c}{\sqrt{\varepsilon_{r,eff}\omega}}$. $\varepsilon_{r,eff} = 2.18 \rightarrow \lambda = 4.06 \text{ mm} \rightarrow \beta = \frac{2\pi}{\lambda} = 1.55 \text{ }mm^{-1} \rightarrow \text{length of TRL} = 141 \text{ }\mu\text{m}.$ A shorted stub is used to shift to from z_1 to the center (z_0), since $z_1 \rightarrow y_1 = 1 + 3.24j$ this requires a normalized susceptance of -j3.24 \rightarrow normalized impedance of j0.31. The characteristic impedance of the stub is $Z_{stub} = \approx \frac{60}{\epsilon_r} \ln \left(\frac{8H}{W} + \frac{W}{4H} \right) = 60 \Omega \rightarrow a$ changing $l_{stub} = \frac{1}{\beta} \operatorname{atan} \left(\frac{Z_0}{Z_{stub}} \right) = 160 \, \mu \text{m}$. (one can also use an open stub of length 1.

c. (5 p) The $\lambda/4$ transformer should transform from Z₀ = 50 Ω to 351 Ω . \rightarrow Z_{trans} = 132 Ω . This means W = 54 nm $\rightarrow \varepsilon_{r,eff} = 2.09 \rightarrow \lambda = 4.1 \text{ mm} \rightarrow \beta = 1.52 \text{ mm}^{-1} \rightarrow \lambda = 4.1 \text{ mm}$

$$l_{phys} = \frac{0.25}{\beta} = \underline{165 \ \mu m}.$$

Then a positive normalized reactance of 6j is needed to move from z = 351/50 to Z_{opt} . An inductor with L = 0.95 nH in series can be used to shift to Z_{opt} . Alternatively one can view the process in reverse, but have then to start at Z_{opt}^* .

d. (2 p) The network in c is more preferable from a robustness perspective since the path to Z_{opt} stays close to the center line of the Smith chart → low Q factor. This means that the design works for a larger frequency band around f = 100 GHz. (However, the narrow width of this line ~ 50 nm means that it may be problematic to make in practice).