# Written Examination EITP01 2019-03-21

## Useful constants:

$$\begin{split} \hbar &= 1.055 \times 10^{-34} \, Js \\ k_B &= 1.381 \times 10^{-23} \, J/K \\ m_0 &= 9.109 \times 10^{-31} \, kg \\ \epsilon_0 &= 8.85 \times 10^{-12} \, Fm^{-1} \\ e &= q = 1.602 \times 10^{-19} \, C \\ c &= 2.998 \times 10^8 \, m/s \end{split}$$

## 1. Ballistic transport in QWFET

(15 p)

An InGaAs QWFET has the crossectional band structure shown below, with the following parameters:

t<sub>w</sub> = t<sub>ox</sub> = 5 nm  $\varepsilon_{ox} = 20, \varepsilon_s = 14$ m\* = 0.04m<sub>0</sub> A gate length of 70 m

A gate length of 70 nm and a width of 10  $\mu m.$ 



- a) Calculate the lowest two subband energy levels (E1 and E2) assuming an infinite well.
- b) Calculate the gate capacitance of the device when operated in the on-state.
- c) Explain the mechanism behind the current saturation in a ballistic transistor.
- d) The device is operated at  $V_{DS} = V_{GS} = 0.5$  V. Is the device in saturation?
- e) Calculate the (quasi-)ballistic current I<sub>DS</sub> assuming a transmission coefficient of 0.6.
- f) Calculate the transconductance at these operation conditions.

### 2. High frequency operation

(15 p)

Another QWFET device as seen below has  $C_{ox} = 0.033 F/m^2$ ,  $C_q = 0.028 F/m^2$  and  $C_c = 0.057 F/m^2$ , width of 10 µm and gate length of 90 nm. g<sub>m</sub> = 55 mS and g<sub>d</sub> = 5 mS.



- a. Calculate the intrinsic value of  $f_T$  for this device.
- b. In reality, the contact and source and drain resistances lead to finite values of  $R_s$  and  $R_D$ . This device has a specific contact resistivity of 10  $\Omega\mu m^2$ , and a doping level of  $1 * 10^{19} \ cm^{-3}$  and electron mobility of 500 cm<sup>2</sup>/Vs in the source/drain regions, while the channel itself has a mobility of 10000 cm<sup>2</sup>/Vs and doping level of  $1.2 * 10^{16} \ cm^{-3}$ . Due to a spacer process the low-doped channel region extends 5 nm outside of the gated area, while the gate-contact separation is 20 nm. Calculate  $R_s$  and  $R_D$  and comment on what is the largest contributor to the resistance.
- c. The fact that the contacts and gate are so closely spaced leads to a significant parasitic capacitance of  $C_{gs,p} = C_{gd,p} = 5 fF$ . Calculate  $f_T$  including the effect of source/drain resistance and parasitic capacitances.

#### 3. Power Gain

(15 p)

A transistor device is modelled by a hybrid- $\pi$  small signal model (including parasitics):

 $R_{G} = 20\Omega$   $C_{gd} = 5 \text{ fF}$   $R_{D} = 50\Omega$   $C_{gs} = 12 \text{ fF}$   $V_{1}$   $g_{d} = 5 \text{ mS}$   $g_{m} = 40 \text{ mS}$   $R_{S} = 50\Omega$ 

Here we have assumed that  $C_{sd} = C_{dg} = C_{dd} = C_m = 0$  for simplicity.

- a) Explain the reason for introducing the channel resistance  $R_i = 1/(1.4g_m)$ .
- b) Determine the z-parameters of the model at f = 100 GHz.
- c) Will the device be stable at this frequency?
- d) Use the proper metric to determine the power gain at this frequency.
- e) Determine  $f_{max}$  of the device. What could be done to improve  $f_{max}$  further?

# 4. Designing a Low noise amplifier

#### (15 p)

A transistor with  $R = R_G + R_i = 44 \Omega$ ,  $g_m = 20 \text{ mS}$ ,  $\gamma = 2/3$  and  $C_{gs} = 10.5 \text{ fF}$  is connected to a source with source impedance  $Z_s = Z_0 = 50 \Omega$  and will be used as a low-noise amplifier at f = 50 GHz.



- a) Determine the source impedance that would optimize the noise figure and calculate the resulting minimum noise factor.
- b) Design an input matching network using 2.0  $\mu$ m wide microstrip transmission line and stub to obtain an optimal low noise amplifier. Assume a dielectric spacer with dielectric constant of  $\varepsilon_r = 3$  and thickness of 5.0  $\mu$ m. (hint: Use a Smith chart)
- c) As an alternative, you now have the freedom to design the width of the transmission line freely. Design a matching network using a  $\frac{\lambda}{4}$  transformer and a reactive element in series. (hint: Use a Smith chart)
- d) Which of these two networks is the most preferable? Motivate your answer.

Good luck!

Maximum score: 60 points