



# Electrodynamics, lecture 5, 2019

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Electrical and information technology

# Last lecture

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- ▶ Cavities
- ▶ Circular cylindric cavity
- ▶  $TM_{010}$  mode

# Resonance cavities

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Applications of cavities:

- ▶ High  $Q$  band-pass and band-stop filters
- ▶ Cavities in accelerators
- ▶ Klystrons
- ▶ Magnetrons

Shumann resonances

# Resonance cavities

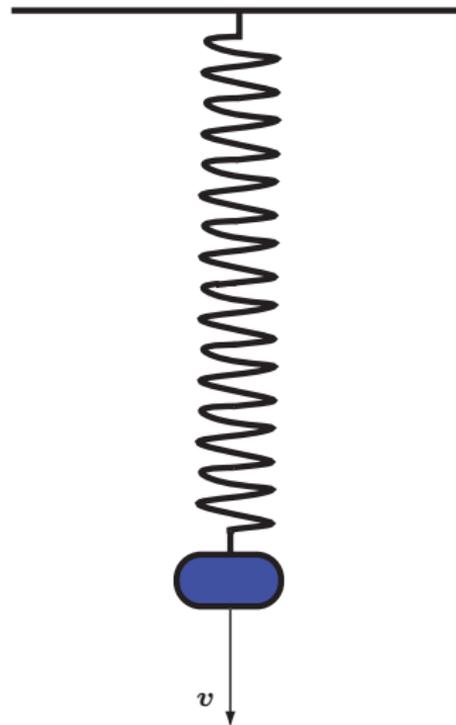
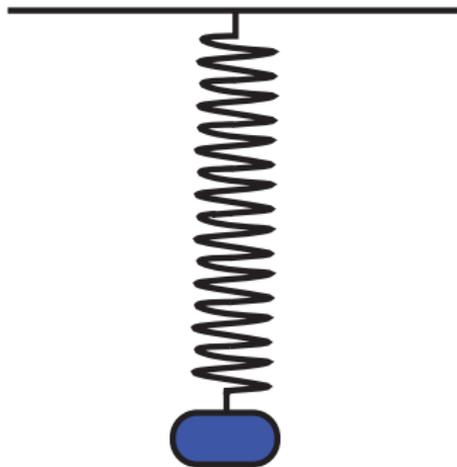
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To get a resonance you need two energy states!  
Potential energy  $\leftrightarrow$  kinetic energy



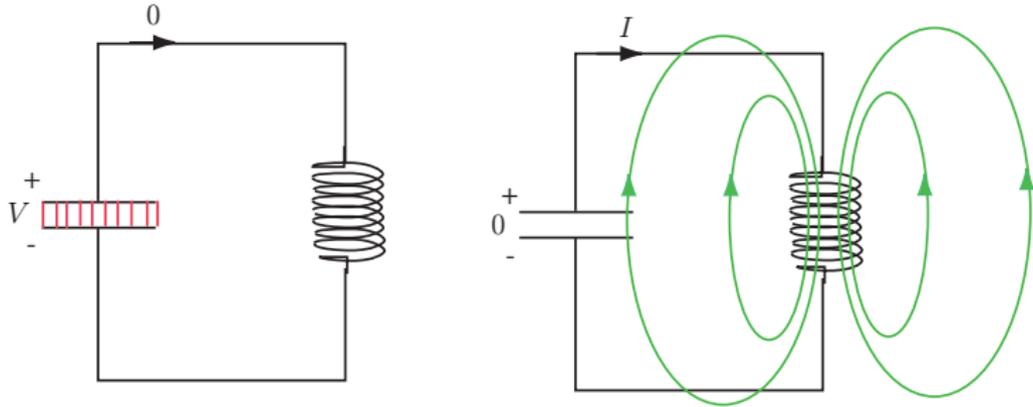
# Resonance cavities

Potential energy  $\leftrightarrow$  kinetic energy



# Resonance cavities

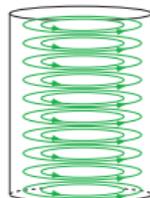
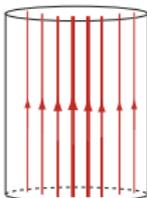
Electric energy  $\leftrightarrow$  magnetic energy



# Resonance cavities

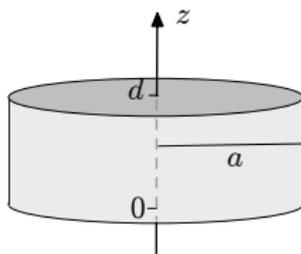
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Electric energy  $\leftrightarrow$  magnetic energy



# The pillbox cavity

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TM<sub>010</sub>

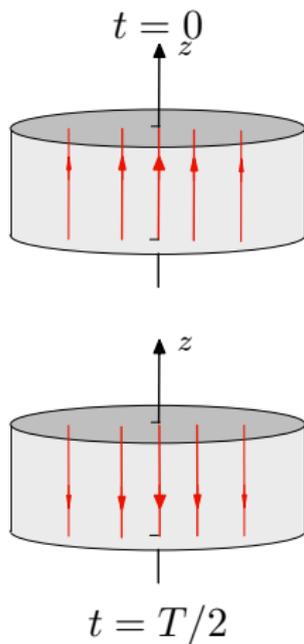
$$\mathbf{E}(\rho, t) = E_0 J_0(k\rho) \cos(\omega t) \hat{z}$$

$$\text{Wavenumber} = k = \frac{2.405}{a}$$

$$\text{Resonance frequency} = f = \frac{kc}{2\pi}$$

# The pillbox cavity $TM_{010}$ mode

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# Outline today

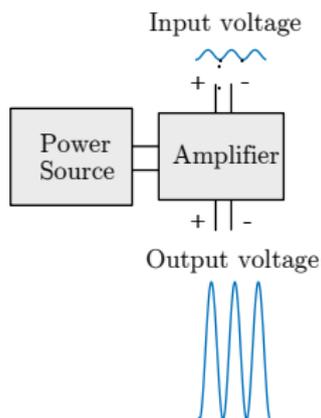
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- ▶ RF-systems for particle accelerators
- ▶ Q-factor
- ▶ Evaluating Q-factor with COMSOL

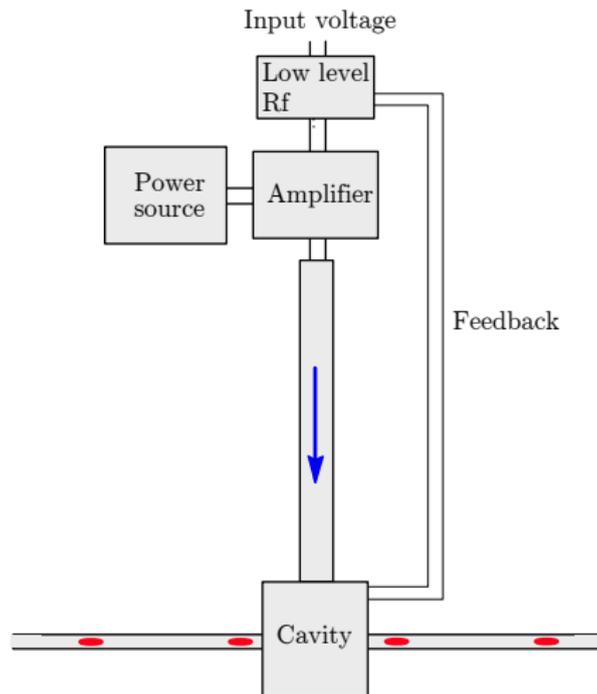
# The RF-system for accelerators

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The RF-system uses time-harmonic signals

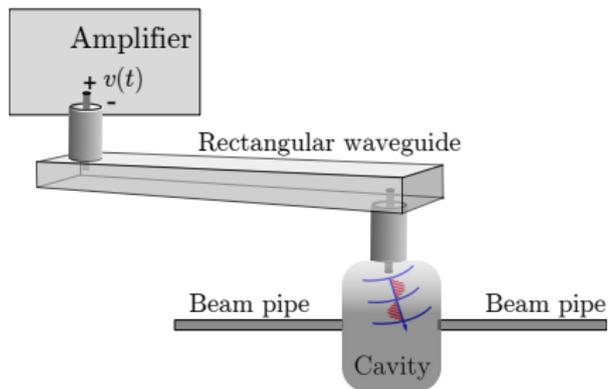


# The RF-system



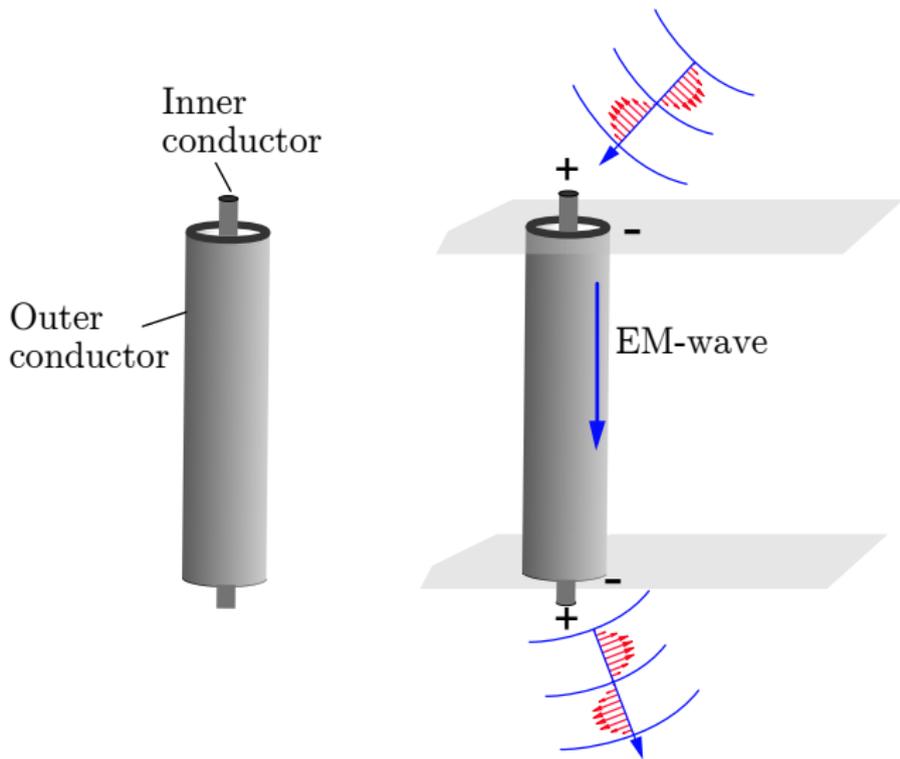
# The RF-system

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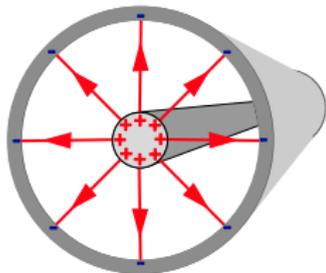
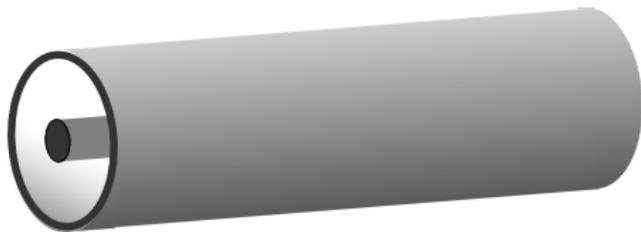
# The RF-system: waveguide system

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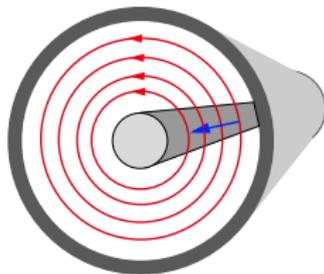


# The RF-system: waveguide system

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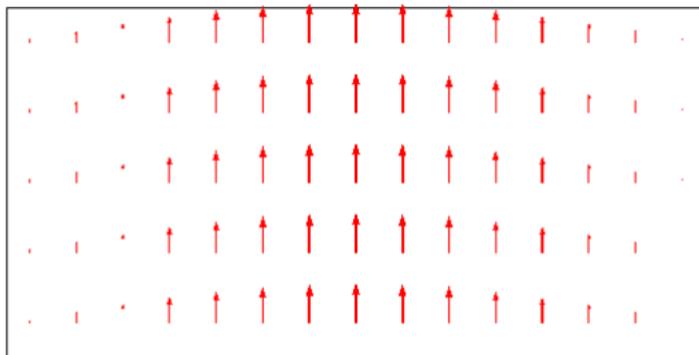
**Electric field**



**Magnetic field**

# The RF-system: waveguide system

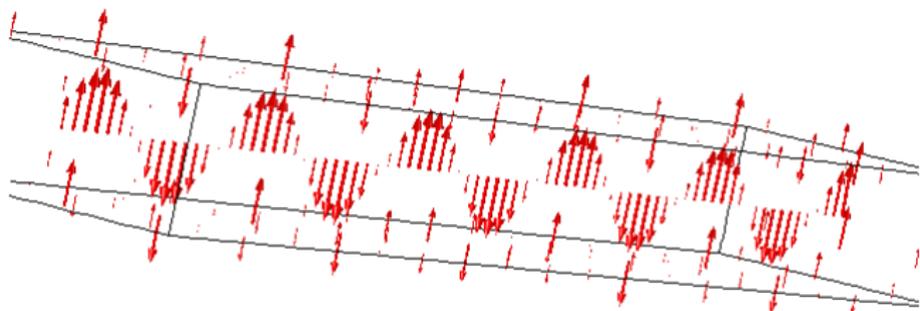
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$TE_{10}$ -mode: Cross section.

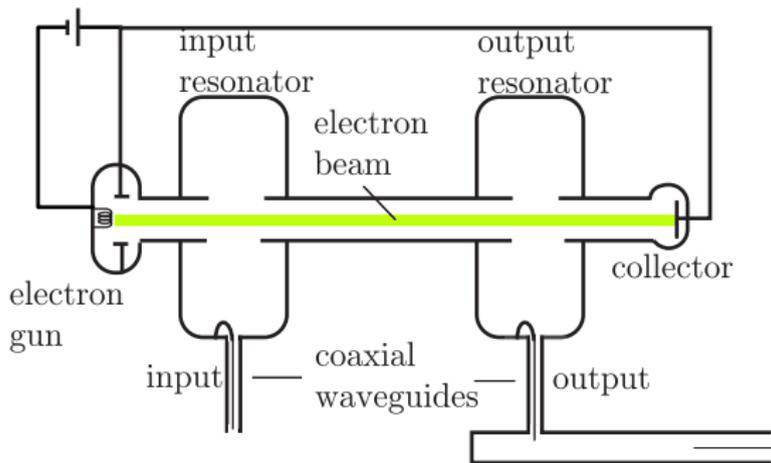
# The RF-system: waveguide system

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TE<sub>10</sub>-mode: Along waveguide

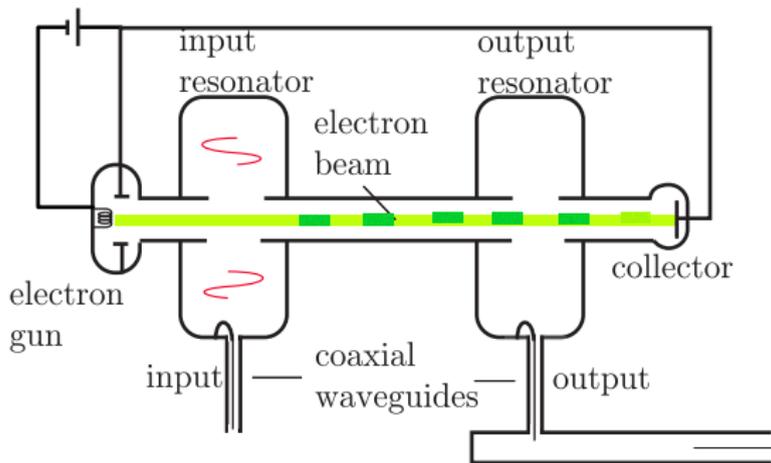
# The RF-system: klystron



input resonator= buncher,

output resonator=catcher

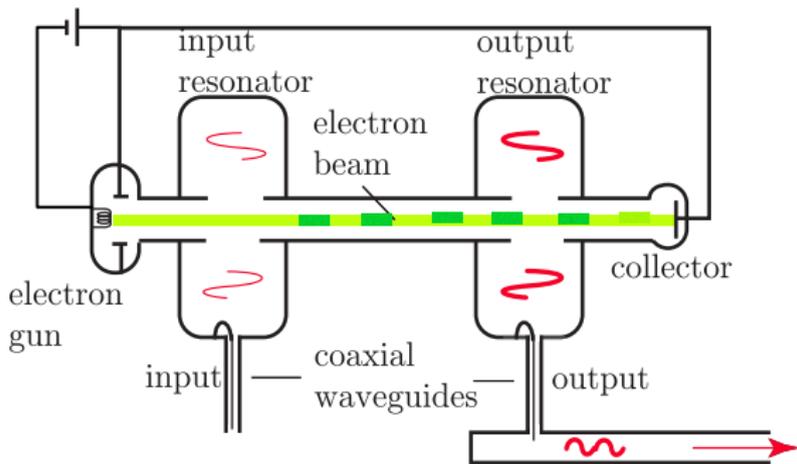
# The RF-system: klystron



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# The RF-system: klystron

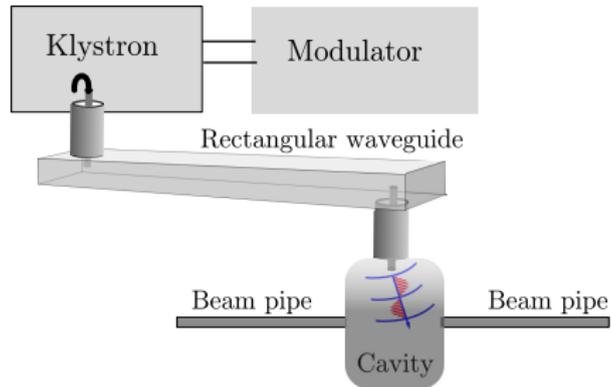


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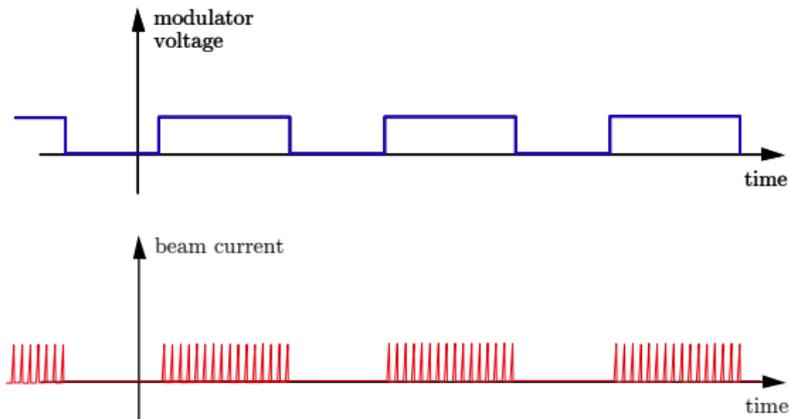
# The RF-system

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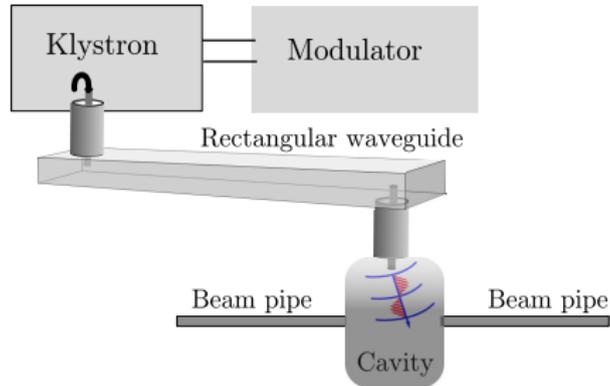
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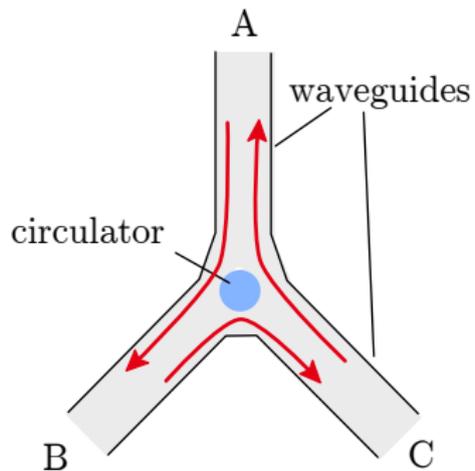
# The RF-system: waveguide system

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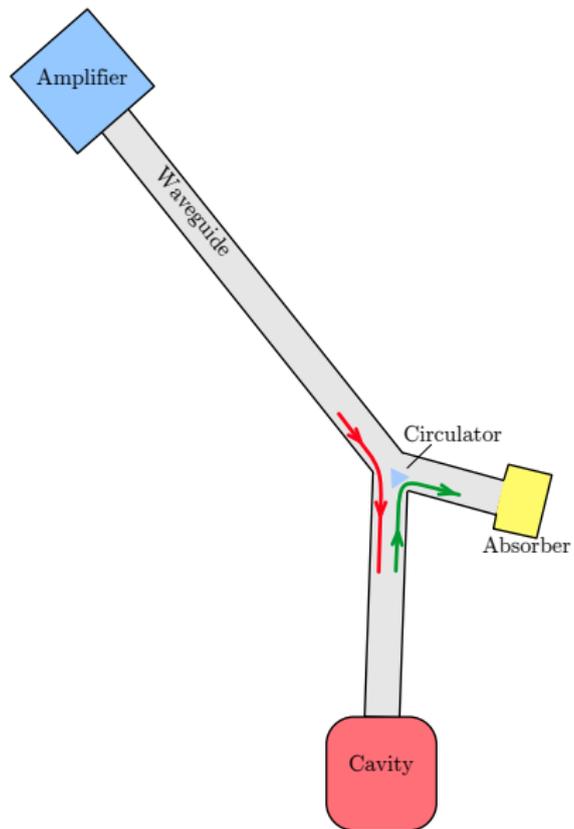
# The RF-system: Circulator

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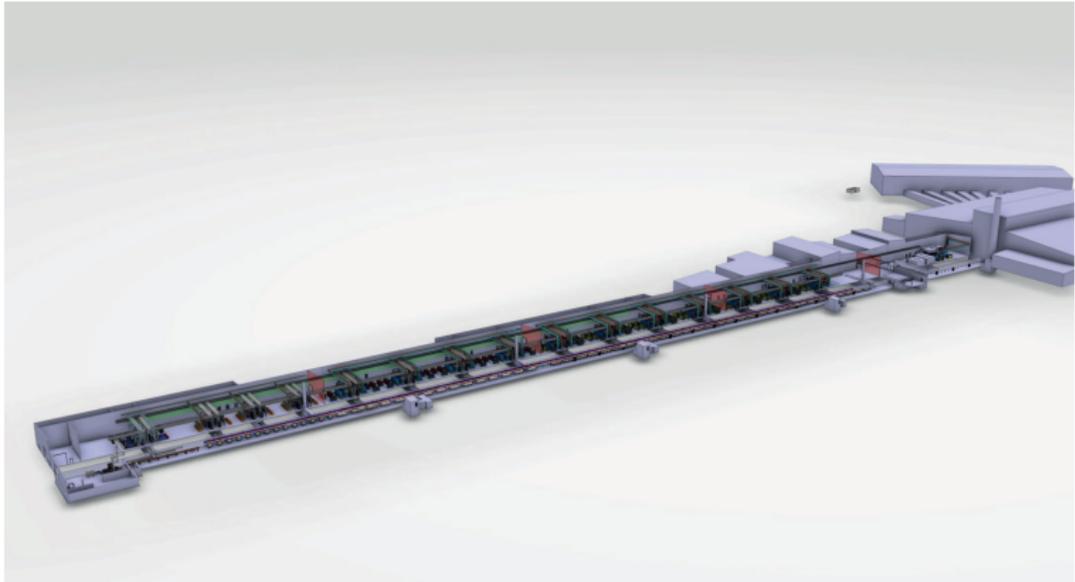
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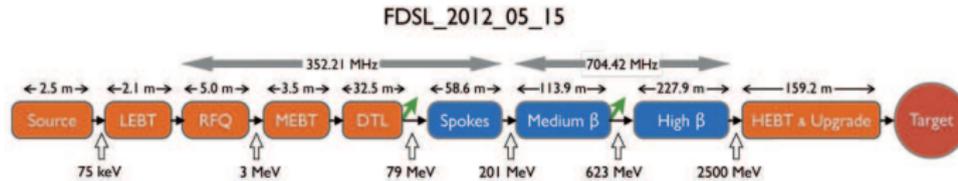


# ESS

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# ESS

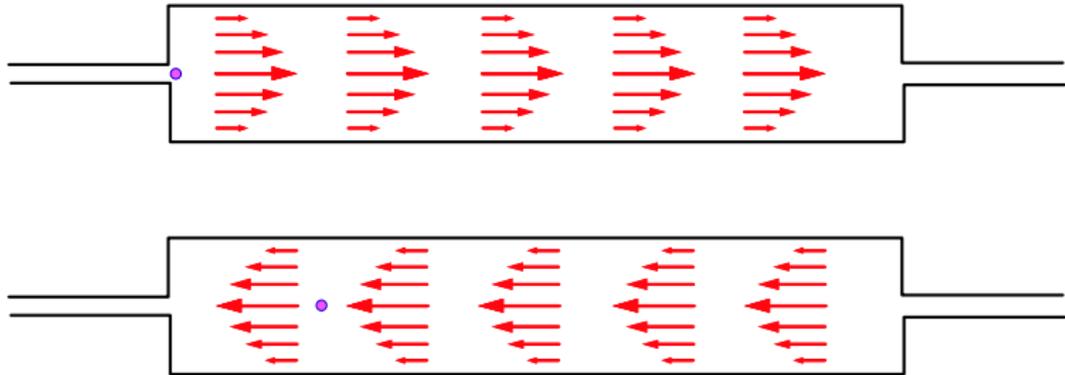


# ESS: DTL

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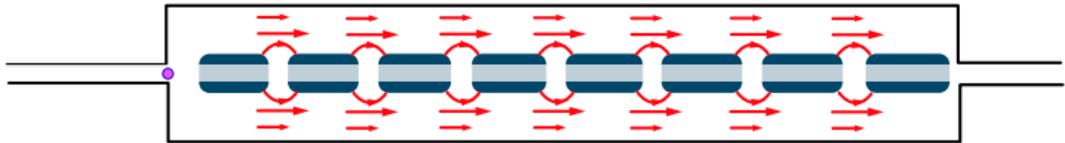


# ESS: DTL



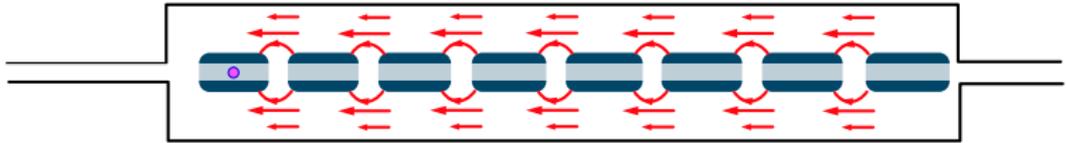
# ESS: DTL

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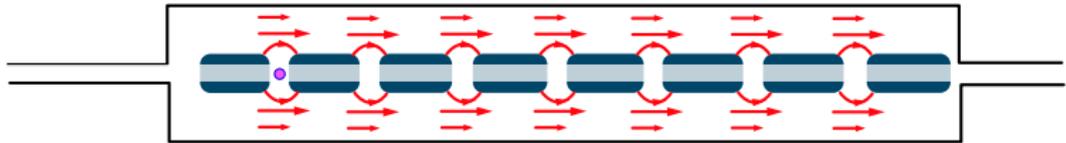
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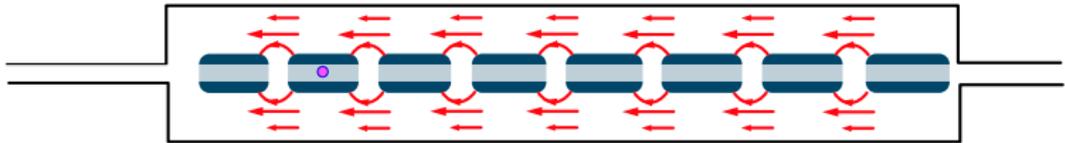
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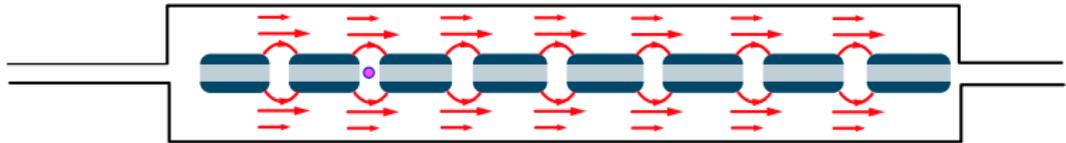
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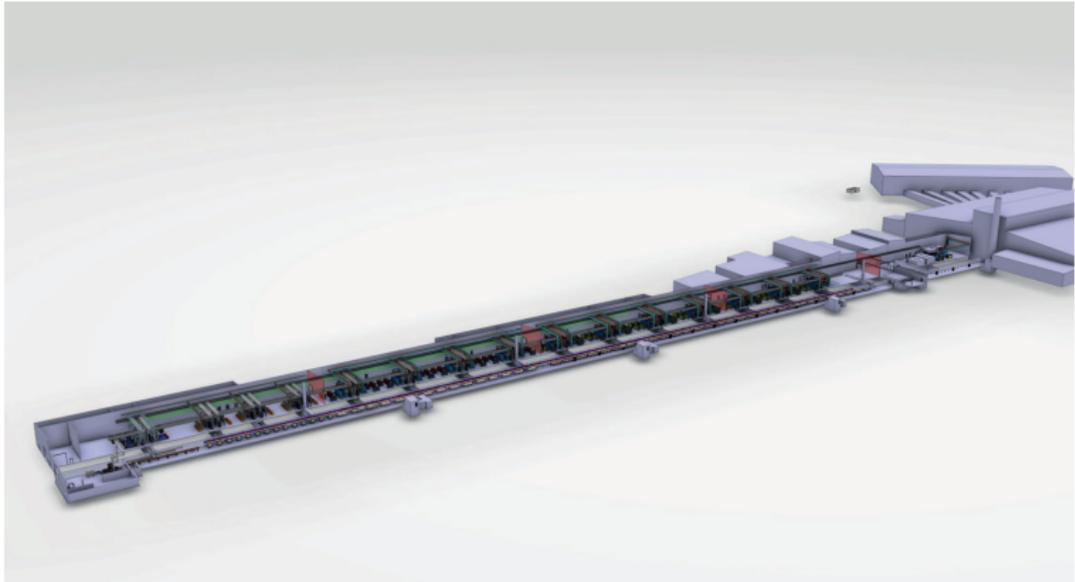
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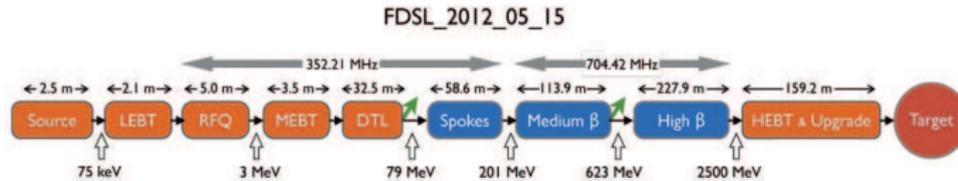


# ESS

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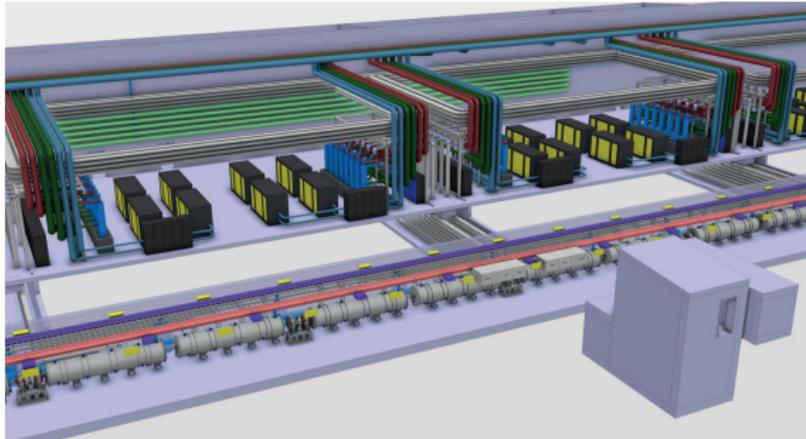


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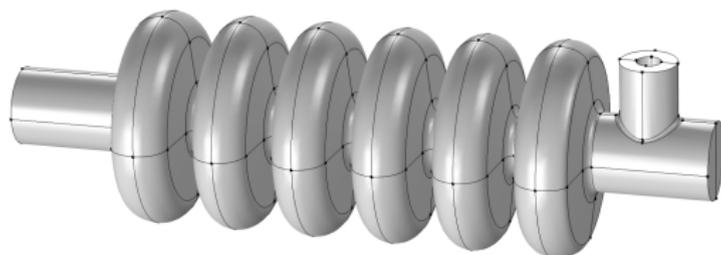
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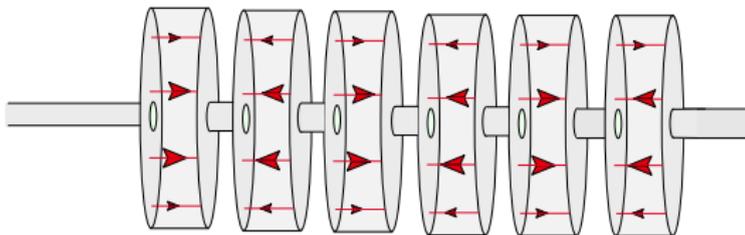
# ESS: Elliptic cavity

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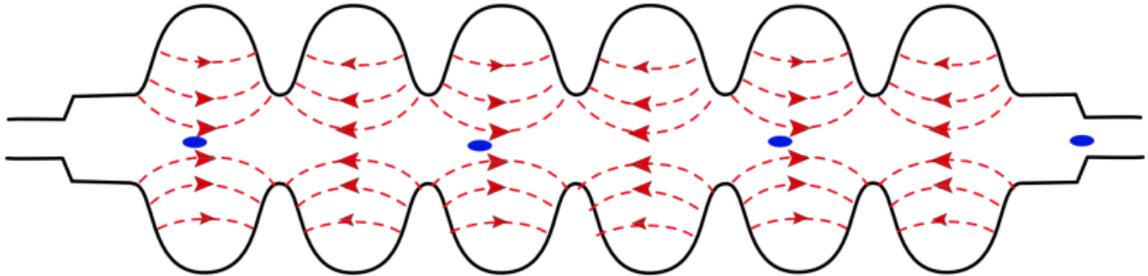


$TM_{010}$ -mode in every cell.

$\pi$ -mode

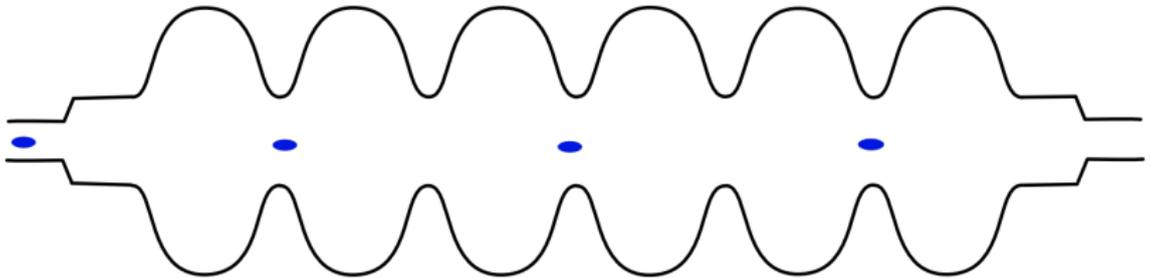
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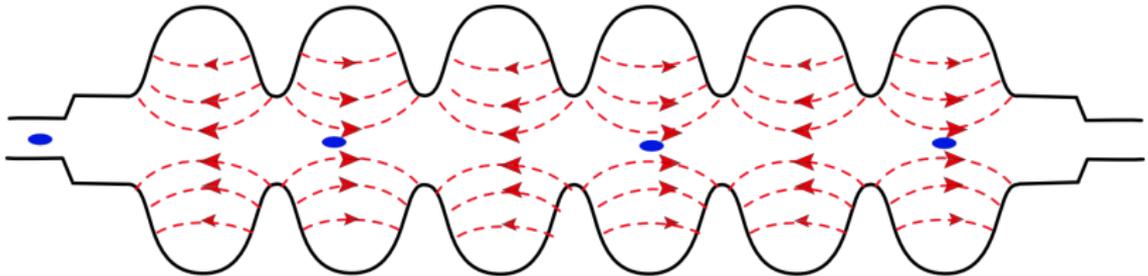
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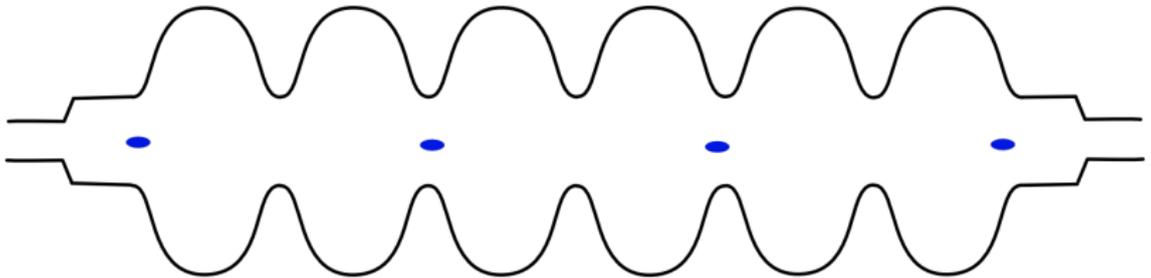
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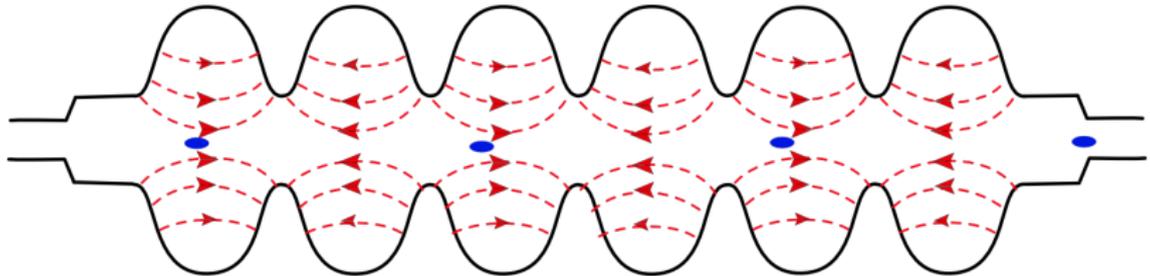
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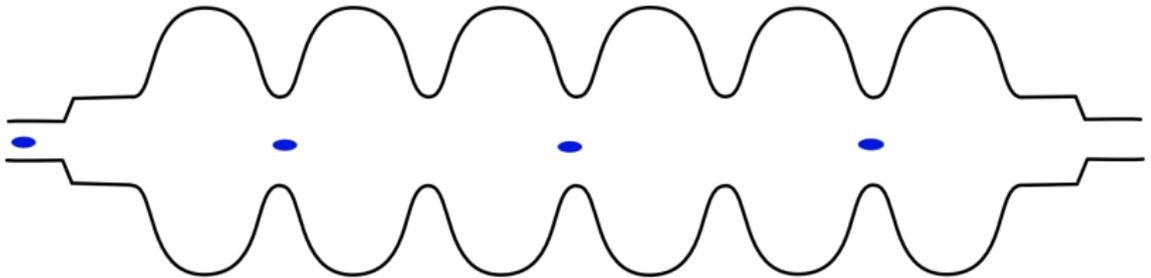
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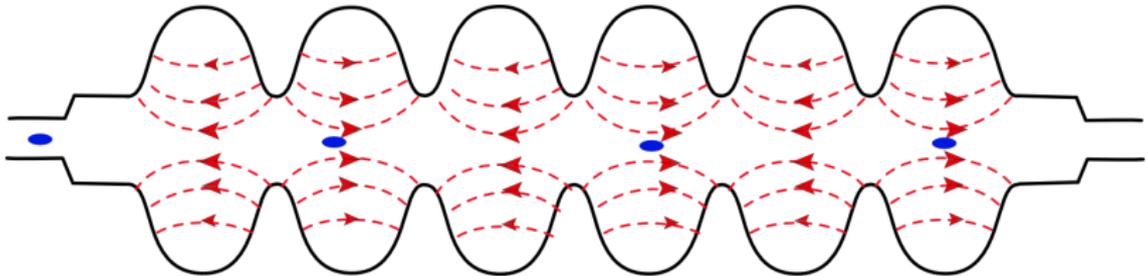
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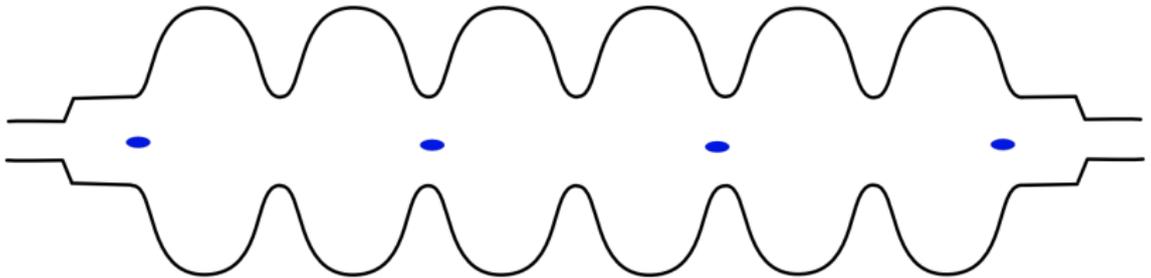
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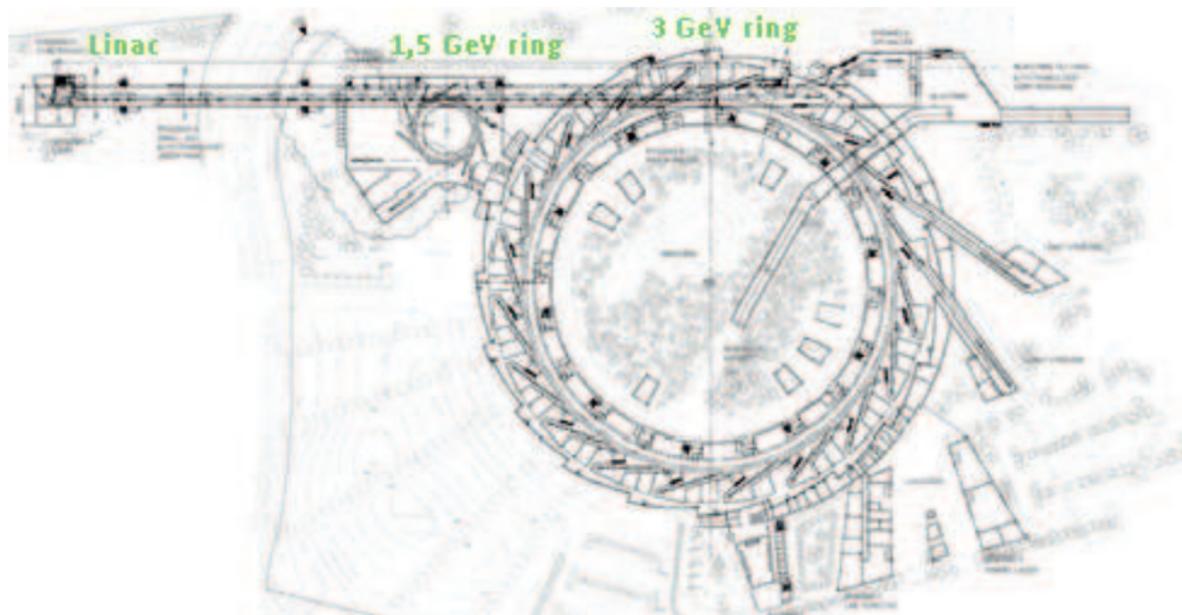
# ESS: Elliptic cavity

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# MAX IV

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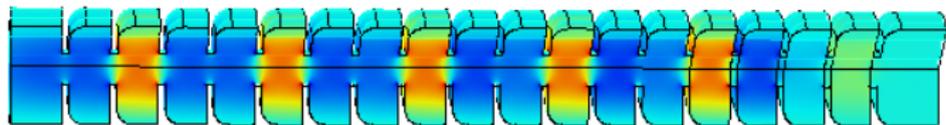
# MAX IV: Linac

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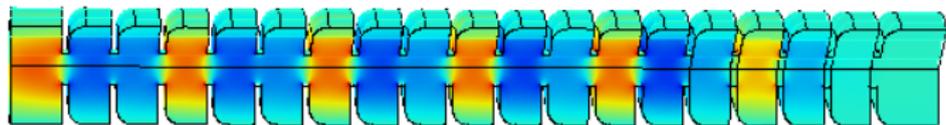
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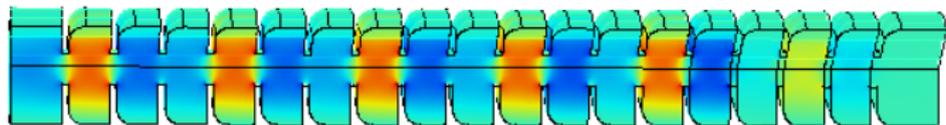
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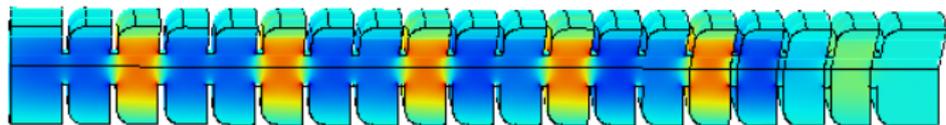
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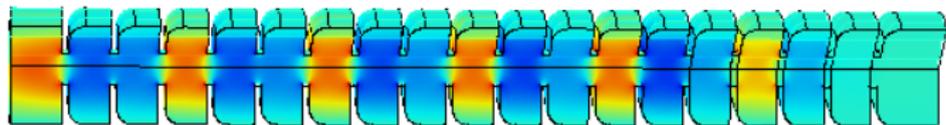
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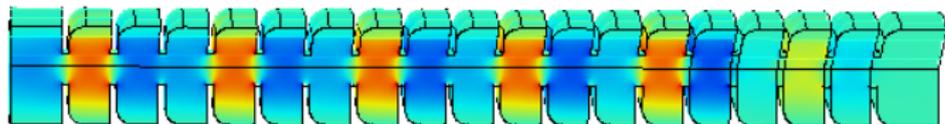
# MAX IV: Linac

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# MAX IV: Linac

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# MAX IV: Undulator

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