

EITG05 – Digital Communications

Lecture 1

Introduction, Overview, Basic Concepts (p. 1–32)

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Digital Communications

We are in a global digital (r)evolution

- ▶ Mobile data and telephony (GSM, EDGE, 3G, 4G, 5G)
- ▶ Digital radio and television, Bluetooth, WLAN
- ▶ Data storage, CD, DVD, Flash, magnetic storage
- ▶ Optical fiber, DSL (long range, high rate)
- ▶ Cloud computing, big data, distributed storage
- ▶ Connected devices, Internet of things, machine-to-machine communication, distributed control, cyber physical systems

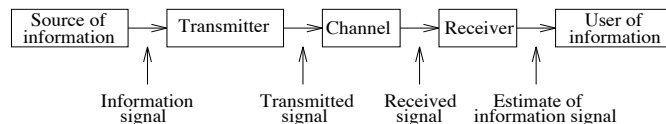
The large number of different application scenarios require flexible communication solutions (data rate / delay / reliability / complexity)

Remark storage of data falls also into the category of a communication system (why?)



What is communication?

- ▶ The purpose of a communication system is to **transmit messages** (information) from a source to a destination
Examples: sound, picture, movie, text, etc.
- ▶ The messages are converted into **signals** that are suitable for transmission
- ▶ The physical medium for transmission is called the **channel**



- ▶ The received signal is used to estimate the messages

What are analog / digital signals?

Analog versus digital

- ▶ **Analog communication:**
both source and processing are analog
- ▶ **Digital communication:**
the source messages are digital, i.e., can be represented by discrete numbers (digits)

Example 1: I speak and you listen to the acoustic sound wave

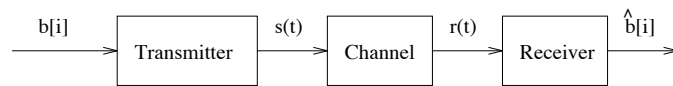
Example 2: I record my speech to MP3 and send it to you, who plays it back on your computer or phone

Example 3: I use morse code and a flashlight to transmit a message to my neighbor

In all cases some analog medium has to be used during the transmission at some point



Scope of this course



- ▶ Transmitter principles: bits to analog signals (Chap. 2)
- ▶ Receiver principles: analog noisy signals to bits (Chap. 4,5,6)
- ▶ Characteristics of the communication link (Chap. 3,6)

Requirements:

- ▶ Data should arrive correctly at the receiver
- ▶ High bit rates are desirable
- ▶ Energy/power efficiency
- ▶ Bandwidth efficiency

What are the technical solutions and challenges?



Not in this course

- ▶ Analog to digital conversion, sampling theorem, quantization
⇒ basic signals & systems or signal processing course
- ▶ Source coding (compression)
⇒ covered in information theory course (elective)
- ▶ Channel coding (robust and reliable communication)
⇒ covered in separate course (elective)
- ▶ Cryptography (secure communication)
⇒ covered in separate course (elective)

There exist a large number of specialized courses that can be taken after this basic course.

There is also a project course in wireless communications.



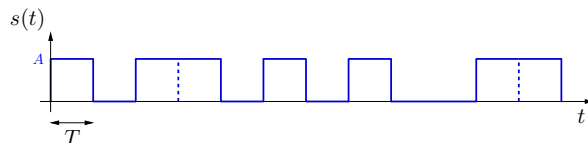
The Transmitter

How can we map digital data to analog signals?

$$b[i] = 1 \ 0 \ 1 \ 1 \ 0 \ 1 \ 0 \ 1 \ 0 \ 0 \ 1 \ 1$$

A simple approach:

apply some voltage A during transmission of a 1



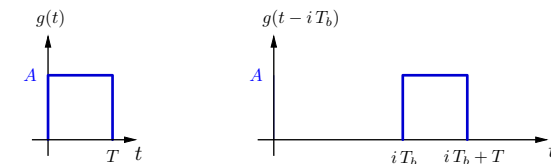
Basic operation: (more general)

represent the sequence of information bits $b[i]$ by a sequence of analog waveforms, resulting in the transmit signal $s(t)$



The Transmitter

- ▶ The analog waveform corresponding to the bit $b[i]$ can be written as a time-shifted version of an elementary pulse $g(t)$



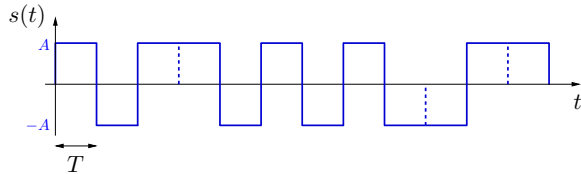
- ▶ T_b is the **information bit interval**, while T is the **pulse duration**
- ▶ For now we assume that $T \leq T_b$, i.e., the pulses do not overlap
- ▶ We can now represent the transmit sequence $s(t)$ as follows

$$s(t) = b[0]g(t) + b[1]g(t - T_b) + b[2]g(t - 2T_b) + \dots$$



Variations of our signaling example

- ▶ In our example we only send a signal when $b[i] = 1$
This modulation type is called **on-off signaling**
- ▶ Instead we could send a pulse with amplitude $-A$ for $b[i] = 0$:



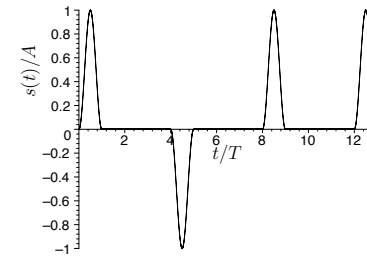
This modulation type is called **antipodal signaling**

- ▶ We could also choose a different **pulse shape** $g(t)$

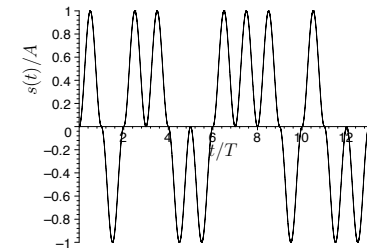
In this chapter: different modulation types and their properties



Another pulse example (→ p. 10)

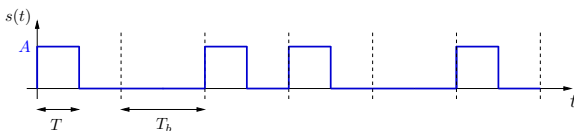


What are the input sequences $b[i]$ here?



What data rate can we achieve?

- ▶ We could also choose a shorter pulse, with $T < T_b$ (what for?)



- ▶ An important parameter is the **information bit rate**

$$R_b = \frac{B}{\tau} \text{ [bps] (bits per second) ,}$$

if the source produces B information bits during τ seconds

- ▶ If we avoid overlapping pulses we need $T \leq T_b$ and

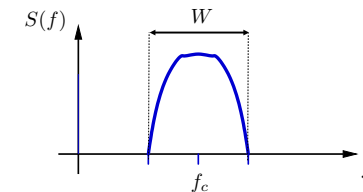
$$R_b = \frac{1}{T_b} \leq \frac{1}{T}$$

Observe: T determines the pulse length and T_b the rate



What bandwidth is required?

- ▶ The **bandwidth** W of the transmit signal is a valuable resource



- ▶ For typical pulses $g(t)$ the bandwidth W is proportional to $\frac{1}{T}$
- ▶ More details about the bandwidth of $s(t)$ follow next week
- ▶ A challenging goal is to achieve a large **bandwidth efficiency**

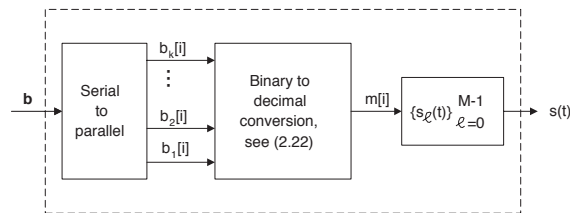
$$\rho = \frac{R_b}{W} \left[\frac{\text{b/s}}{\text{Hz}} \right]$$

Question: What happens when the pulse duration gets small?



Increasing the message alphabet

- Up to this point we have considered **binary signaling** only
- Each bit $b[i]$ was mapped to one of two signals $s_0(t)$ or $s_1(t)$
- More generally, we can combine k bits $b_1[i], b_2[i], \dots, b_k[i]$ to a single message $m[i]$, which then is mapped to a signal $s_\ell(t)$



- In case of **M-ary signaling**, one of $M = 2^k$ messages $m[i]$ is transmitted by its corresponding signal alternative

$$s_\ell(t) \in \{s_0(t), s_1(t), \dots, s_{M-1}(t)\}$$



M-ary signaling

Example: $k = 2, M = 2^2 = 4$

The binary sequence

$$b_n[i] = 1 \ 0 \ 1 \ 1 \ 0 \ 1 \ 0 \ 1 \ 0 \ 0 \ 1 \ 1$$

is mapped by

$$m[i] = \sum_{n=1}^k b_n[i] 2^{n-1} = b_1[i] + b_2[i] \cdot 2$$

to $M = 4$ signal alternatives

$$\begin{aligned} b[i] = 00 &\leftrightarrow m[i] = 0 \leftrightarrow s_0(t) & b[i] = 10 &\leftrightarrow m[i] = 1 \leftrightarrow s_1(t) \\ b[i] = 01 &\leftrightarrow m[i] = 2 \leftrightarrow s_2(t) & b[i] = 11 &\leftrightarrow m[i] = 3 \leftrightarrow s_3(t) \end{aligned}$$

The message sequence becomes

$$m[i] = 1 \ 3 \ 2 \ 2 \ 0 \ 3$$

With $k = 14$ there are $M = 16384$ signal alternatives



Symbol rate versus bit rate

- Since k information bits are transmitted with each symbol, the **symbol interval** (symbol time) becomes

$$T_s = k T_b$$

- Accordingly, the **symbol rate** (signaling rate) is given by

$$R_s = \frac{1}{T_s} \left[\frac{\text{symbols}}{\text{s}} \right] = \frac{R_b}{k}$$

- When the message equals $m[i] = j$ then $s_j(t - iT_s)$ is sent

$$s(t) = s_{m[0]}(t) + s_{m[1]}(t - T_s) + s_{m[2]}(t - 2T_s) + \dots$$

How does k affect the bandwidth efficiency ρ ?

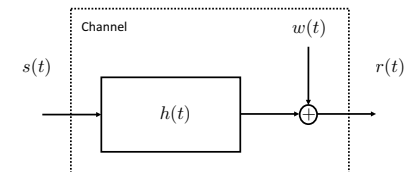
Remark: Be careful with the different definitions of time:

t : time variable T : pulse duration T_b : bit time T_s : symbol time



The Channel

- The channel is often modeled as time-invariant filter with noise



- $h(t)$ is the channel impulse response and $w(t)$ the additive noise
- The received signal becomes

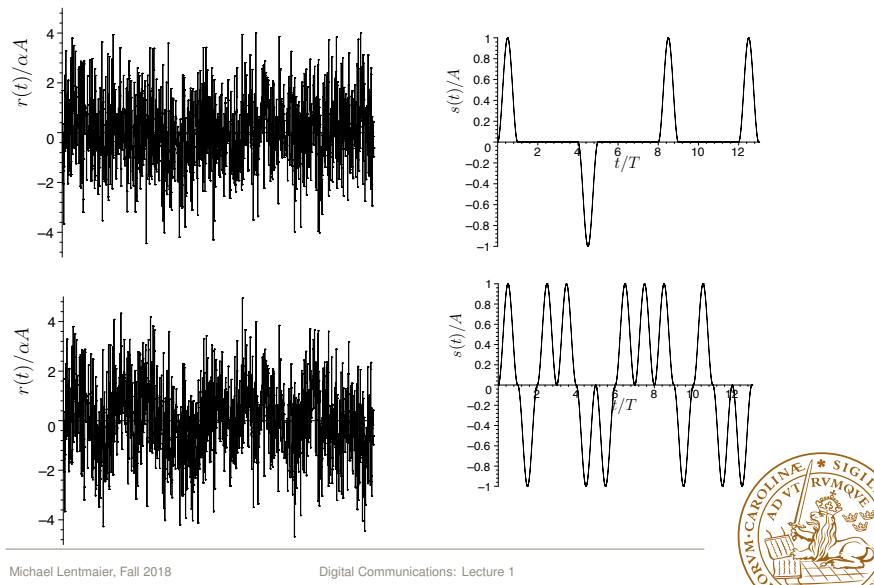
$$r(t) = s(t) * h(t) + w(t) = \int_{-\infty}^{\infty} h(\tau) s(t - \tau) d\tau + w(t)$$

- For now we assume the simple case (α : attenuation)

$$h(t) = \alpha \delta(t) \Rightarrow r(t) = \alpha s(t) + w(t)$$



Example: noisy signal at the receiver (p. 13)

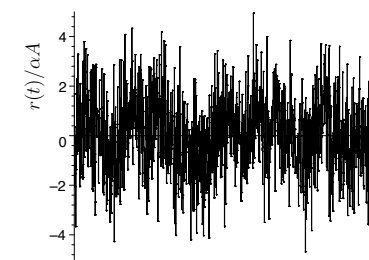


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The Receiver



- ▶ Due to the attenuation α during transmission, the noise $w(t)$ has a strong impact on the received signal $r(t)$
- ▶ A well designed receiver can still detect the symbols correctly!
In this example, only 1 of 10^5 bits will be wrong in average
- ▶ We will learn about the receiver and its performance later, in Chapters 4 and 5

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Bit Errors

- ▶ The **bit error probability** is an important measure of communication performance
- ▶ It is defined as the average number of information bit errors per detected information bit

$$P_b = \frac{E\{B_{err}\}}{B}$$

Example:

- ▶ Assume a bit rate of 1 Mbps and that 10 bit errors occur per hour on the average. What is the bit error probability?
- ▶ The total number of bits in an hour is

$$B = 1000000 \cdot 60 \cdot 60 = 3.6 \cdot 10^9$$

This gives

$$P_b = \frac{10}{B} = 2.78 \cdot 10^{-9}$$

⇒ Computer simulations become very time consuming!

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Signal energy and power

- ▶ The **symbol energy** E_ℓ of a signal alternative $s_\ell(t)$ is given by

$$E_\ell = \int_0^{T_s} s_\ell^2(t) dt < \infty, \quad \ell = 0, 1, \dots, M-1$$

- ▶ An important system parameter is the **average symbol energy**

$$\bar{E}_s = \sum_{\ell=0}^{M-1} P_\ell E_\ell, \quad P_\ell = \Pr\{m[i] = \ell\}$$

and the **average signal energy per information bit**

$$\bar{E}_b = \frac{\bar{E}_s}{k}$$

- ▶ The **average signal power** is then given by

$$\bar{P} = R_s \bar{E}_s = \frac{R_b}{k} \cdot k \bar{E}_b = R_b \bar{E}_b$$

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Signal energy and power

- ▶ The attenuation α and the noise $w(t)$ determine the quality of a communication link

$$r(t) = \alpha s(t) + w(t)$$

Example:

If a transmitted signal $s(t)$ has energy \bar{E}_b , how much energy \mathcal{E}_b is then in the received signal $z(t) = \alpha \cdot s(t)$ if $\alpha = 0.001$?

- ▶ Using $z^2(t) = \alpha^2 s^2(t)$ we obtain

$$\bar{P}_z = \alpha^2 \bar{P} = \alpha^2 R_b \bar{E}_b$$

$$\text{and } \mathcal{E}_b = \frac{\bar{P}_z}{R_b} = \alpha^2 \frac{\bar{P}}{R_b} = \alpha^2 \bar{E}_b$$

- ▶ If $\alpha = 0.001$ then the power is reduced by a factor 10^{-6}

This will increase the bit error probability!



How well can we distinguish two signals?

- ▶ The **squared Euclidean distance** between two signals $s_i(t)$ and $s_j(t)$ is defined as

$$\begin{aligned} D_{ij}^2 &= \int_0^{T_s} (s_i(t) - s_j(t))^2 dt \\ &= \int_0^{T_s} s_i^2(t) + s_j^2(t) - 2s_i(t)s_j(t) dt \\ &= E_i + E_j - 2 \int_0^{T_s} s_i(t)s_j(t) dt \end{aligned}$$

- ▶ Two signals are **antipodal** if

$$s_i(t) = -s_j(t), \quad 0 \leq t \leq T_s$$

- ▶ Two signals are **orthogonal** if

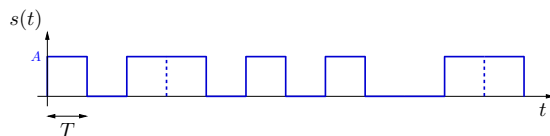
$$\int_0^{T_s} s_i(t)s_j(t) dt = 0$$

Antipodal signals have larger Euclidean distance



Euclidean distance example $M = 2$

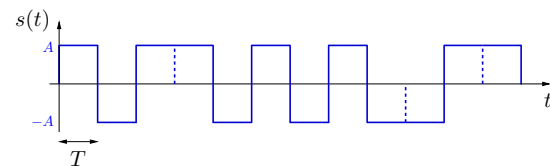
Case 1: on-off signaling



$s_0(t) = A$ and $s_1(t) = 0$ for $0 < t < T_s = T$, which gives $D_{0,1}^2 = 2\bar{E}_b$

Observe: on-off signaling is orthogonal

Case 2: antipodal signaling



$s_0(t) = A$ and $s_1(t) = -A$ for $0 < t < T_s = T$, and $D_{0,1}^2 = 4\bar{E}_b$



Examples of pulse shapes: Appendix D

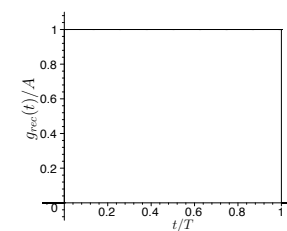


Figure D.1: $g_{rec}(t)/A$.

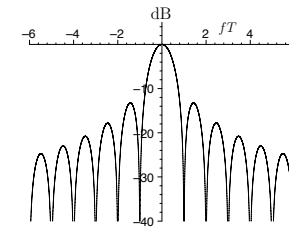


Figure D.2: $\frac{|G_{rec}(f)|^2}{E_g T}$ in dB.

1. The rectangular pulse:

$$g_{rec}(t) = \begin{cases} A & , \quad 0 \leq t \leq T \\ 0 & , \quad \text{otherwise} \end{cases} \quad (\text{D.1})$$

$$E_g = \int_0^T g_{rec}^2(t) dt = \int_{-\infty}^{\infty} |G_{rec}(f)|^2 df = A^2 T \quad (\text{D.2})$$



Examples of pulse shapes: Appendix D

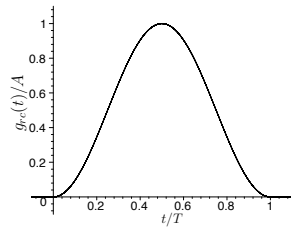


Figure D.9: $g_{rc}(t)/A$.

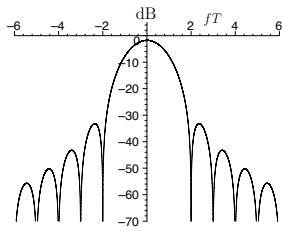


Figure D.10: $\frac{|G_{rc}(f)|^2}{E_g T}$ in dB.

5. The time raised cosine pulse:

$$g_{rc}(t) = \begin{cases} \frac{A}{2} (1 - \cos(2\pi t/T)) & , \quad 0 \leq t \leq T \\ 0 & , \quad \text{otherwise} \end{cases} \quad (\text{D.18})$$

$$E_g = 3A^2 T/8 \quad (\text{D.19})$$

