



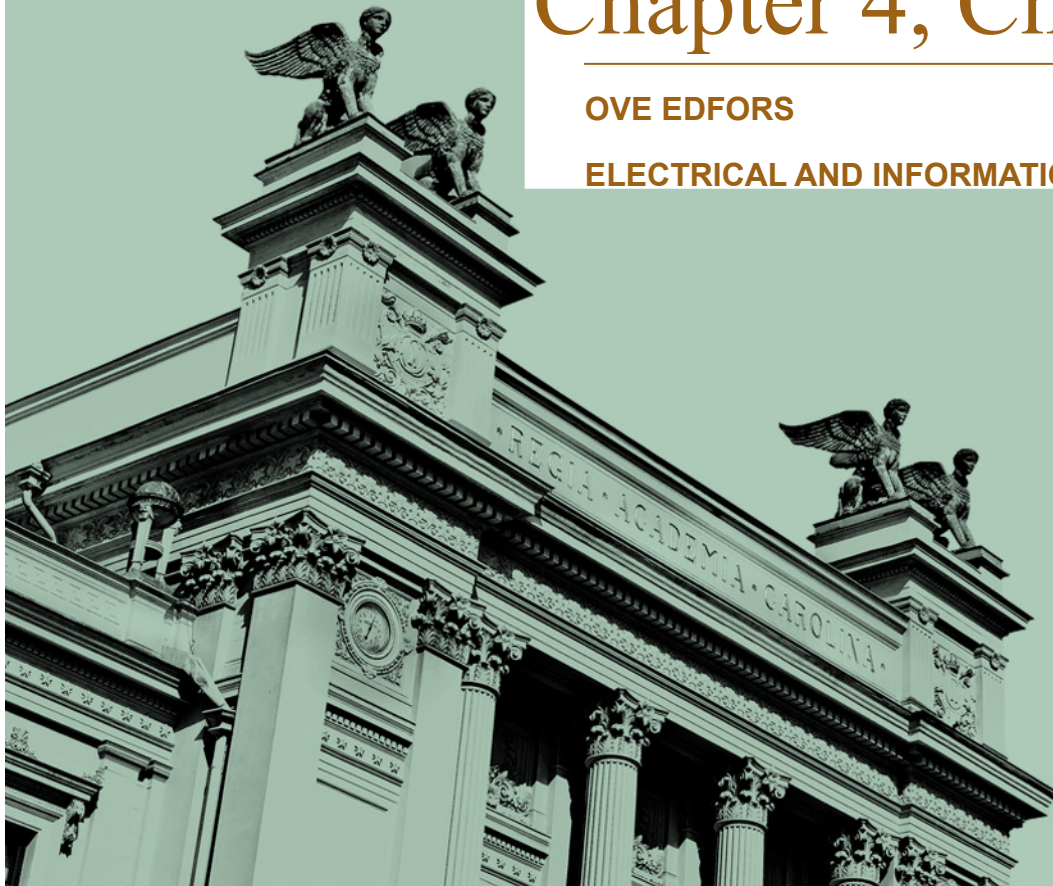
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Information Transmission

Chapter 4, Channels

OVE EDFORS

ELECTRICAL AND INFORMATION TECHNOLOGY

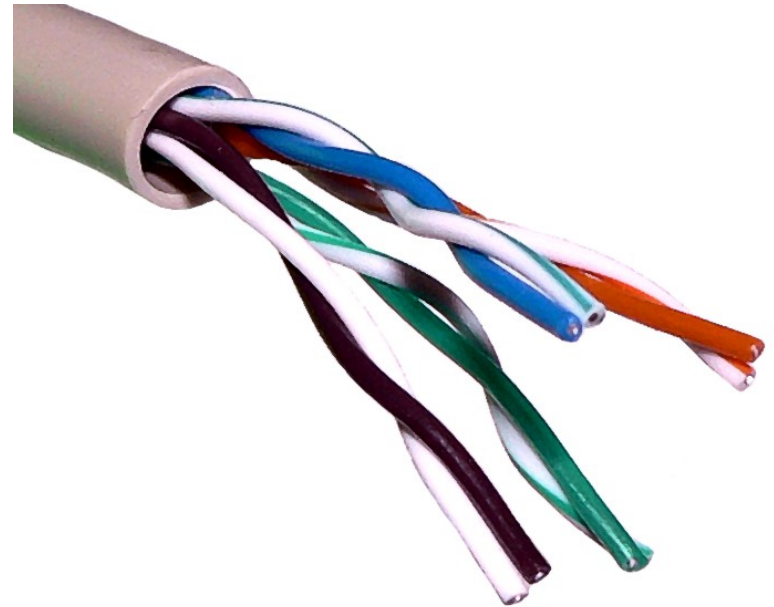
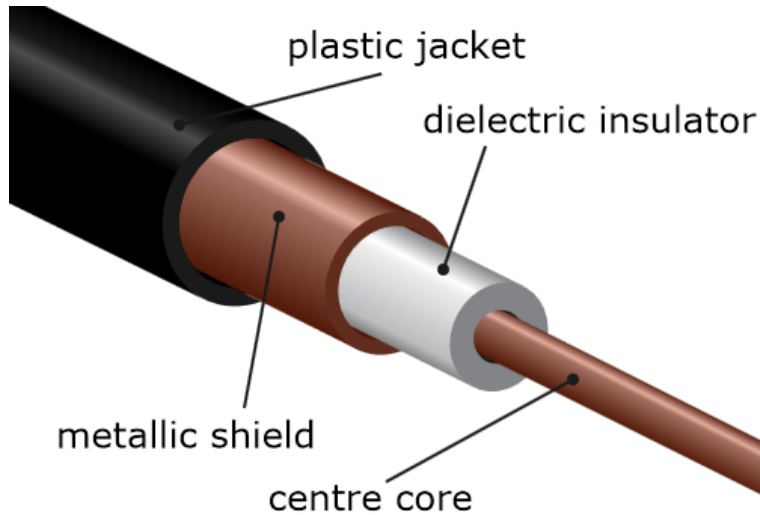


Learning outcomes

- After this lecture the student should
 - understand the basic properties of wired channels, such as cables and optical fibers,
 - know the basic properties of wireless channels, including propagation loss in free space and antenna gains,
 - understand how noise enters the system and how it is characterized,
 - understand the basic principles of how movements and multiple wireless propagation paths create Doppler effects and fading (variations in signal strength), and
 - be familiar with the principle of the magnetic recording channel (for storing data).



Wires, cables and fibers

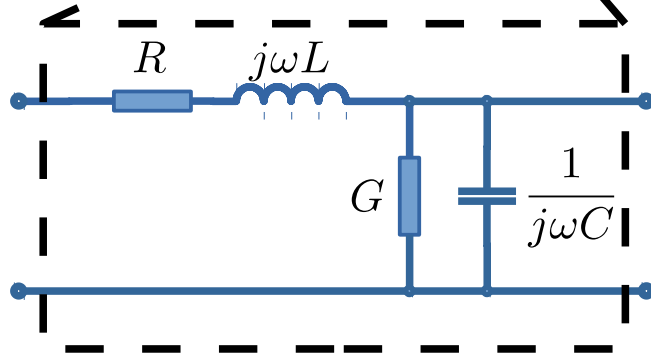
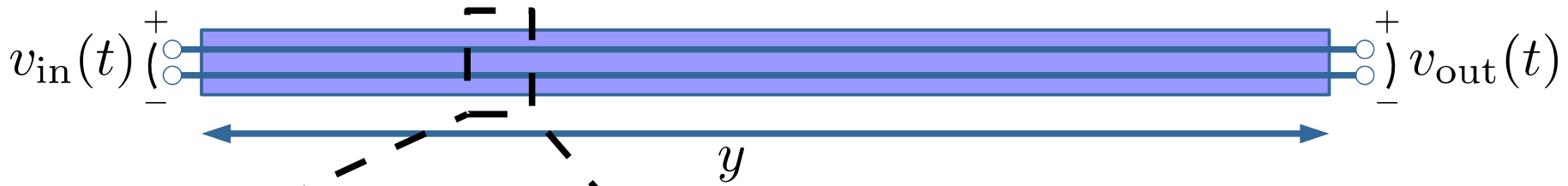


- » Coaxial cable
- » Used for high frequency transmission
- » Shielded and controlled properties

- Twisted pair
- Standard telephone line



Model of a transmission line (wire)



Model of short (unit length) section of line:

- R - resistive loss
- L - inductance from wires
- G - "short circuit" resistance
- C - capacitance between wires

Model of entire wireline



y unit length sections in series



Wires, cables and fibers

- Wires and cables have quite high attenuation

$$v_{\text{out}}(t) \leftarrow v(t) = V_0 e^{j\omega t} e^{-y\gamma} \text{ at distance } y \leftarrow v_{\text{in}}(t)$$

- Where the propagation constant is given by

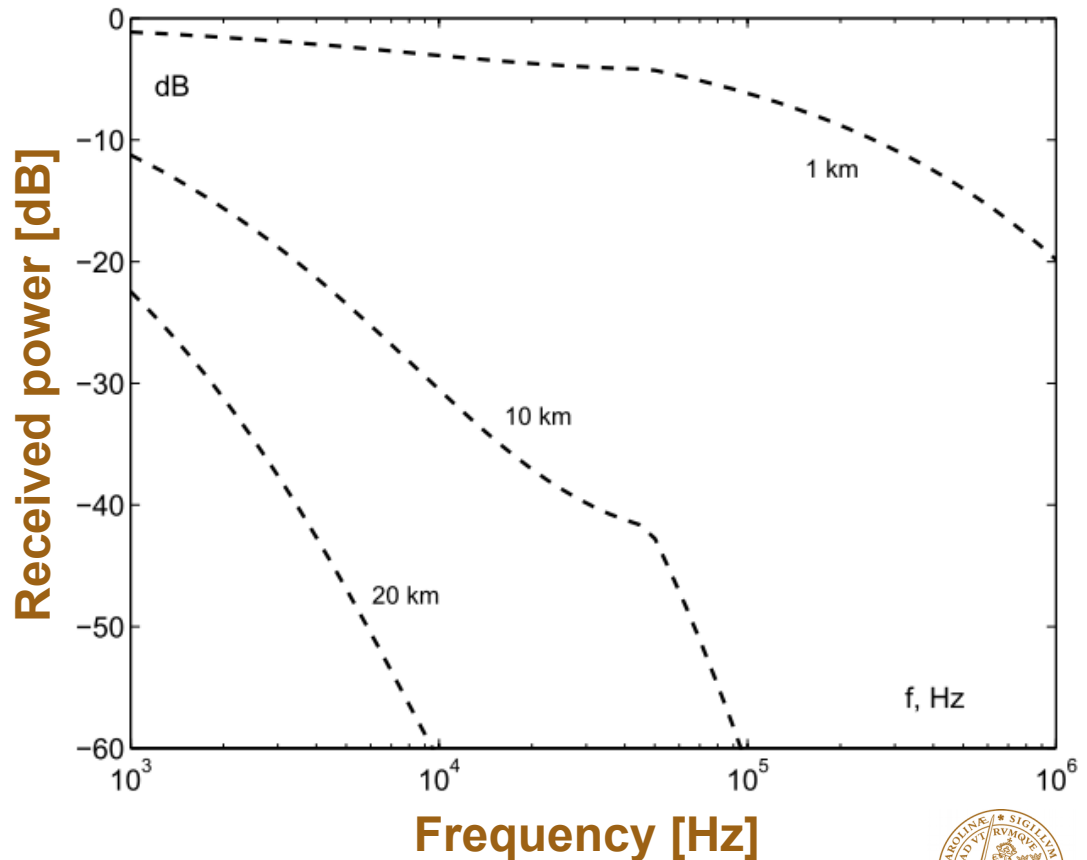
$$\gamma(\omega) = \sqrt{(R(\omega) + j\omega L)(G + j\omega C)}, \quad \omega = 2\pi f$$

- Sinus in – sinus out, but with an attenuation and phase shift

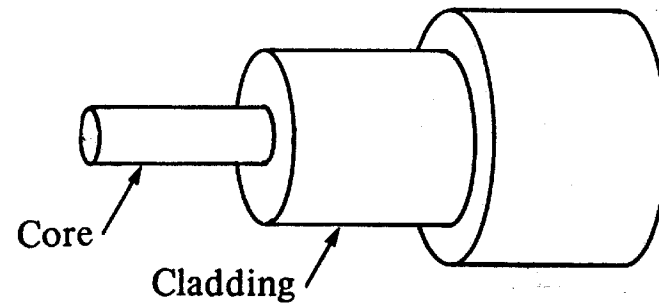
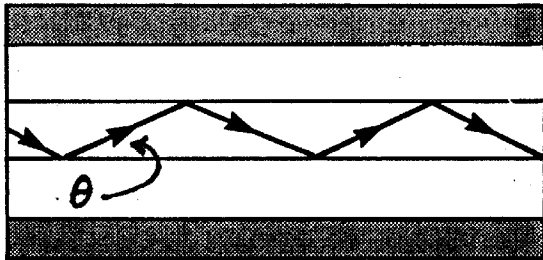


Attenuation of a wire pair (telephone line)

- For longer wire lengths the attenuation is huge at higher frequencies.
- They are already in place, so let's use them...



Propagation in a fiber

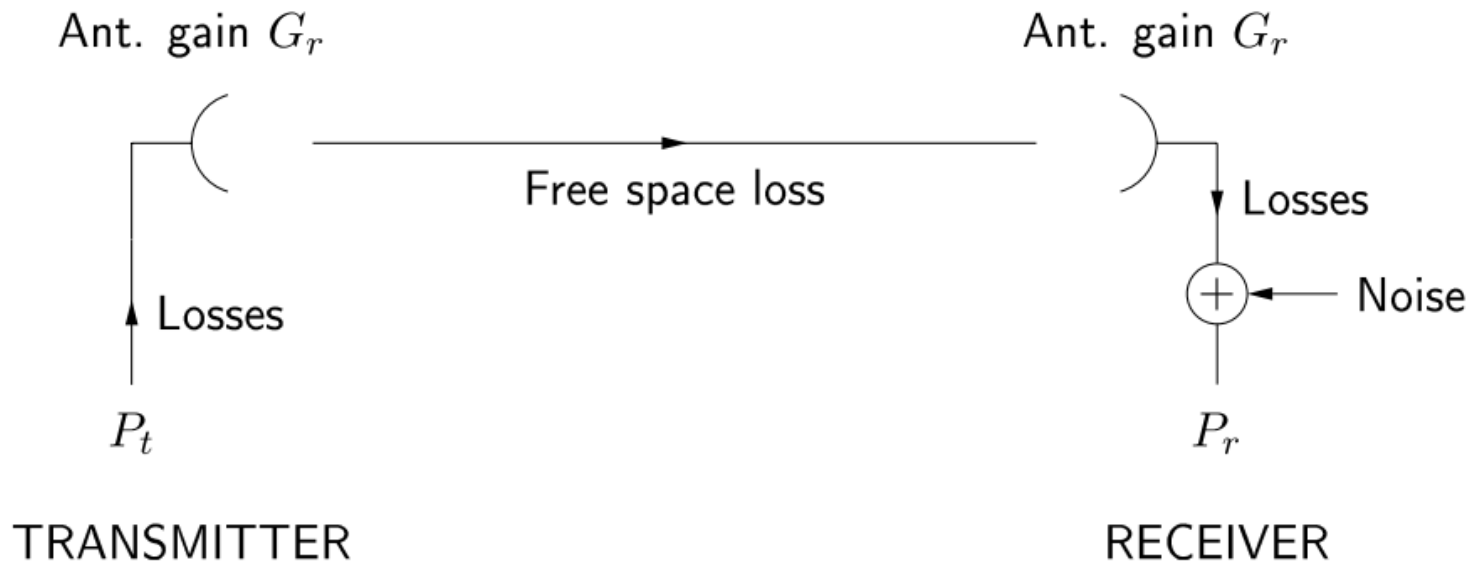


Fibers have low attenuation (< 0.5 dB/km).

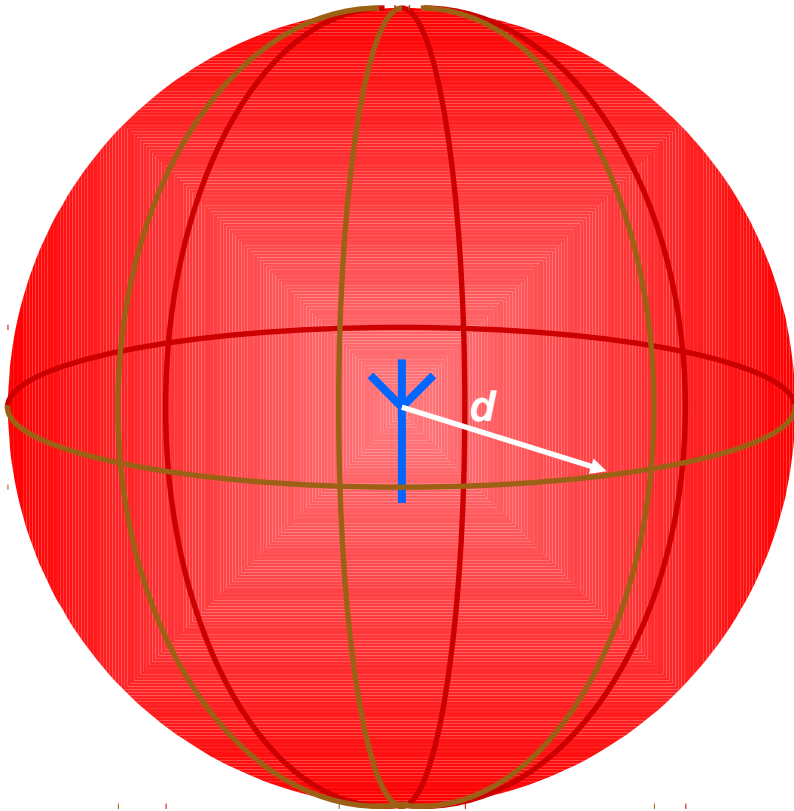
Reflections inside the fiber lead to dispersion – the light pulse will smear out in time.



Radio Channels – Free space



Free-space loss



If we assume RX antenna to be isotropic:

$$P_{\text{RX}}(d) = \left(\frac{\lambda}{4\pi d} \right)^2 P_{\text{TX}}$$

Attenuation between two isotropic antennas in free space is (free-space loss):

$$L_{\text{free}}(d) = \left(\frac{4\pi d}{\lambda} \right)^2$$

$$P_{\text{RX}}(d) = \frac{1}{L_{\text{free}}(d)} P_{\text{TX}}$$



Antenna gain

- An antenna will collect its power from an effective area A .
The larger antenna the more power it will collect

$$G = \frac{4\pi A}{\lambda^2}$$

- Similarly, it will focus its transmit power in a certain direction where the power density then will be higher



Free-space loss, Friis' law

Received power, with antenna gains G_{TX} and G_{RX} :

$$P_{\text{RX}}(d) = \frac{G_{\text{RX}}G_{\text{TX}}}{L_{\text{free}}(d)} P_{\text{TX}} = P_{\text{TX}} \left(\frac{\lambda}{4\pi d} \right)^2 G_{\text{RX}}G_{\text{TX}}$$



If we write the expression in dB ...

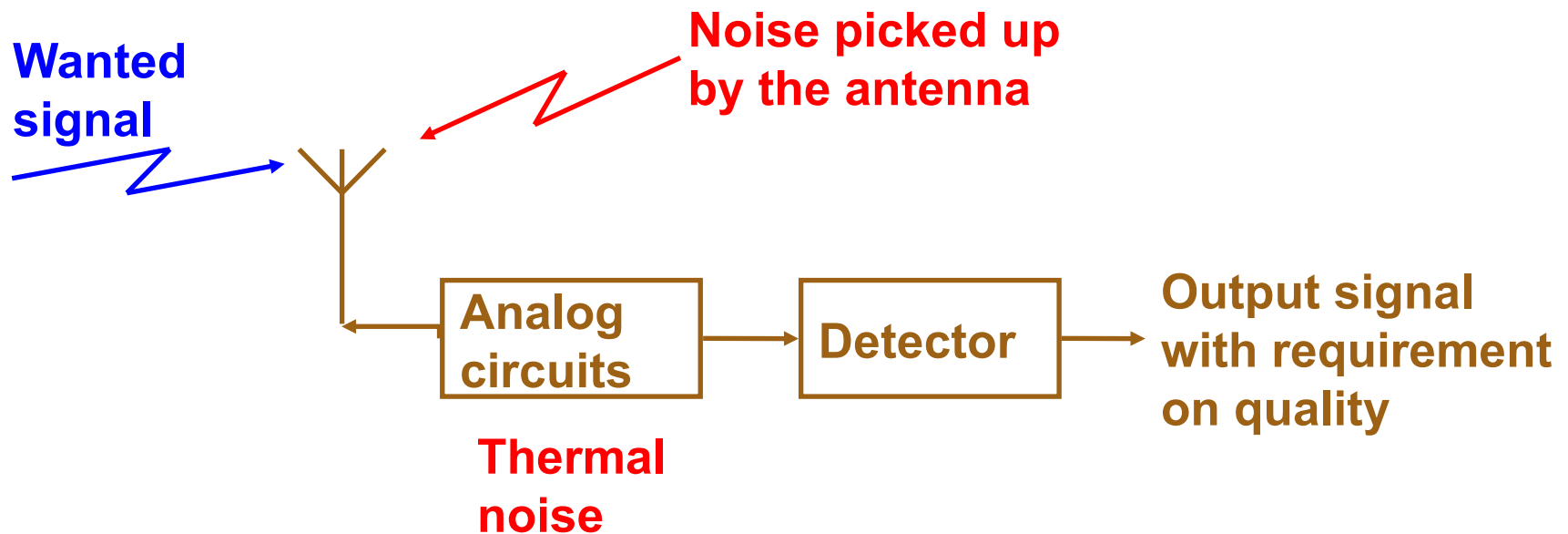
$$\begin{aligned} P_{\text{RX}|_{\text{dB}}}(d) &= P_{\text{TX}|_{\text{dB}}} + G_{\text{RX}|_{\text{dB}}} - L_{\text{free}|_{\text{dB}}}(d) + G_{\text{TX}|_{\text{dB}}} \\ &= P_{\text{TX}|_{\text{dB}}} + G_{\text{RX}|_{\text{dB}}} - 10 \log_{10} \left(\frac{4\pi d}{\lambda} \right)^2 + G_{\text{TX}|_{\text{dB}}} \end{aligned}$$

In free space, the received power decays with distance at a rate = 20 dB/decade



Noise sources

The noise situation in a receiver depends on several noise sources



Receiver noise: Noise sources (1)

The power spectral density of a noise source is usually given in one of the following ways:

1) Directly [W/Hz]

$$kT_K \text{ [W/Hz]}$$

2) Noise temperature [Kelvin]

The power N of the noise is also determined by the bandwidth

$$N = kT_K B_m$$

Here k is Boltzmann's constant (1.38×10^{-23} W/Hz) and T_K is the temperature of the noise source in Kelvin.



Distribution of the noise

- The noise is most often assumed to have a Gaussian distribution

$$f(x) = \frac{1}{\sqrt{N\pi}} e^{-x^2/N}$$

- With this distribution it is possible to calculate the probability that a noise sample exceeds a certain level.

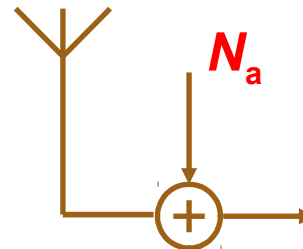
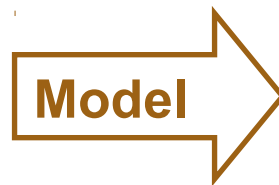


Receiver noise: Noise sources (2)

Antenna example



Noise temperature
of antenna 1600 K



Noise free
antenna

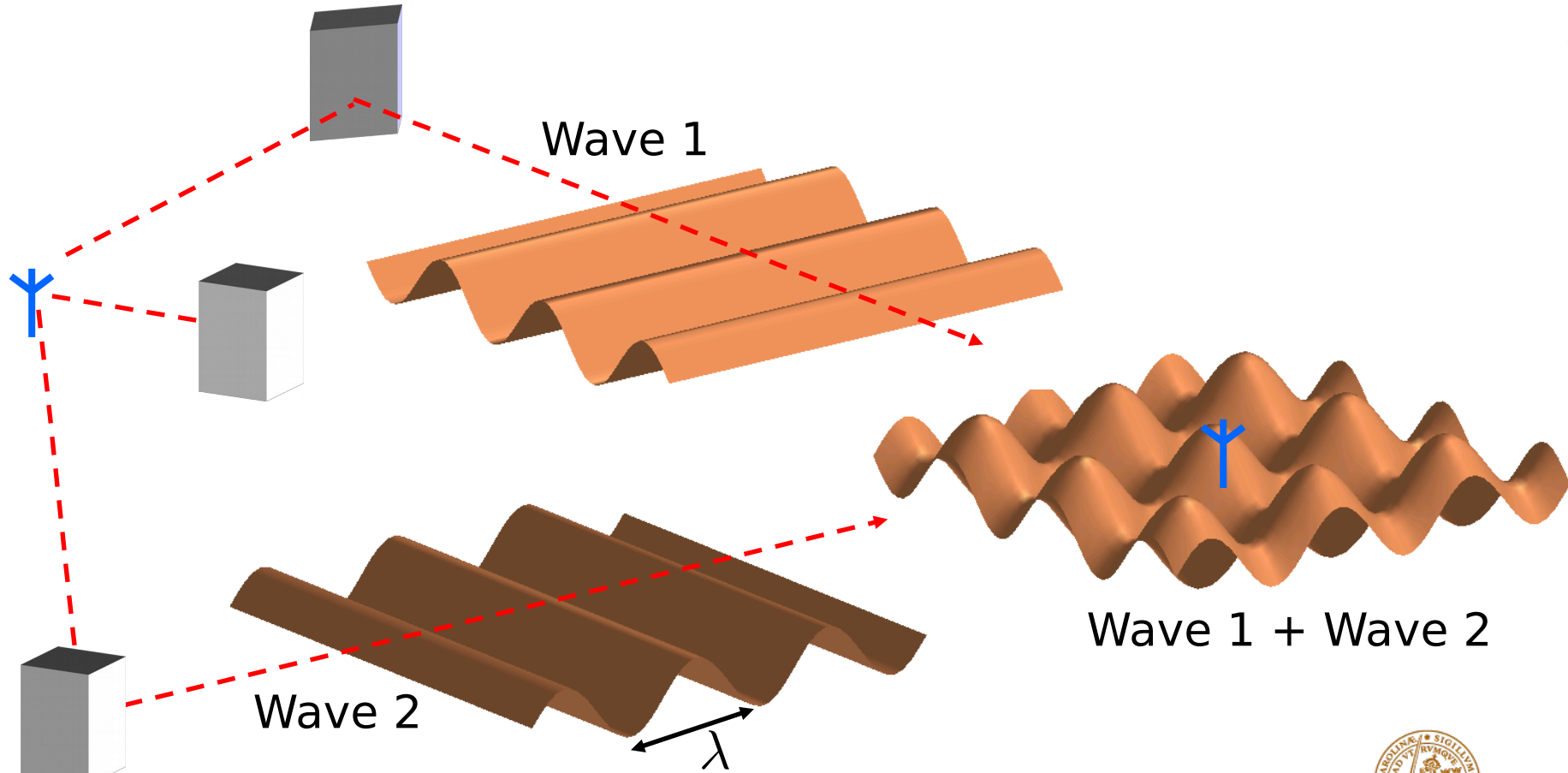
Power spectral density of antenna noise is

$$\begin{aligned} N_a &= kT_a = 1.38 \times 10^{-23} \times 1600 \\ &= 2.21 \times 10^{-20} \text{ W/Hz} = -196.6 \text{ dB[W/Hz]} \end{aligned}$$

Multiply with bandwidth to get noise power



Multi-path propagation, Two waves



At least in this case, we can see that the interference pattern changes on the wavelength scale.



Small-scale fading

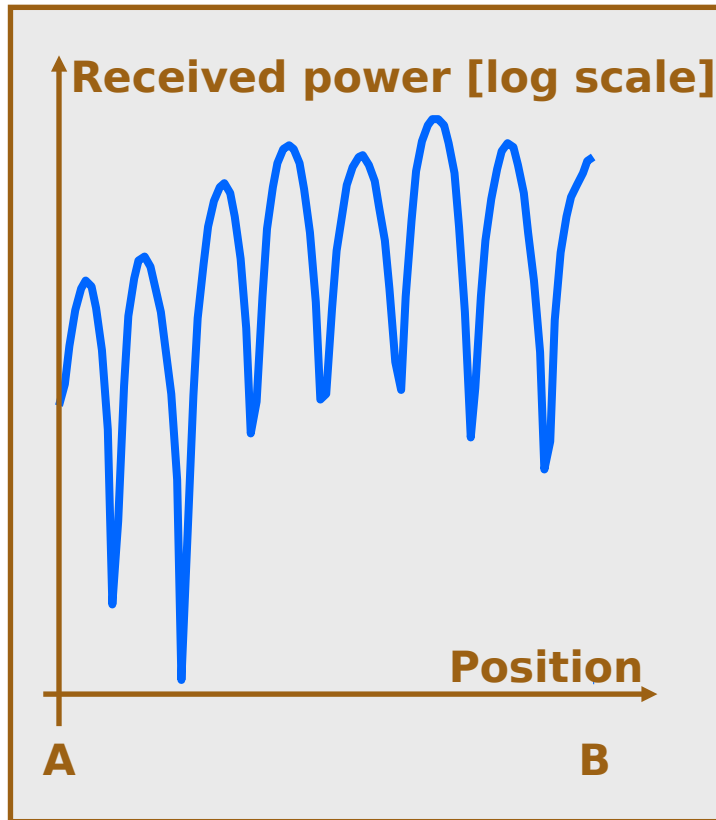
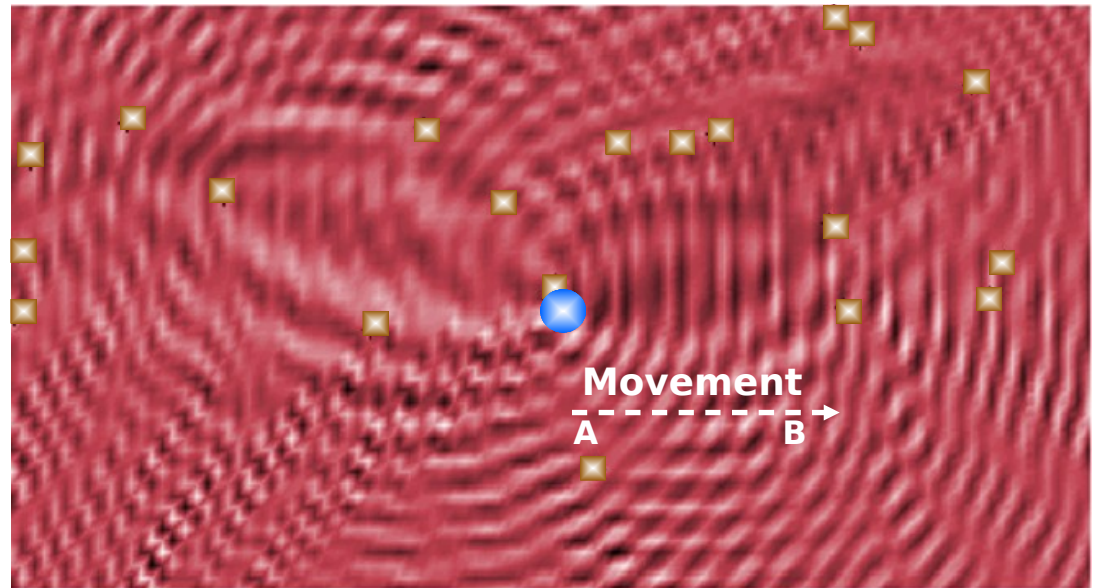


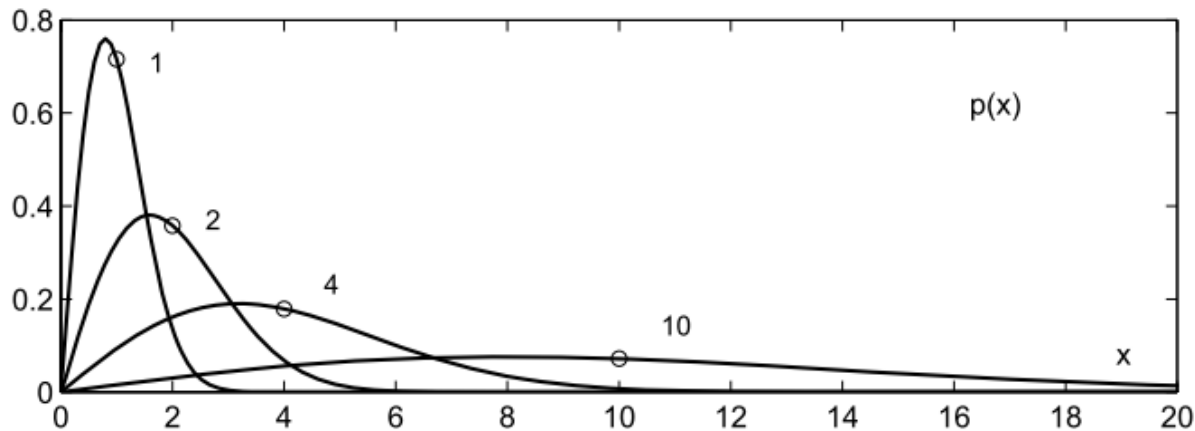
Illustration of interference pattern from above



- Transmitter
- Reflector



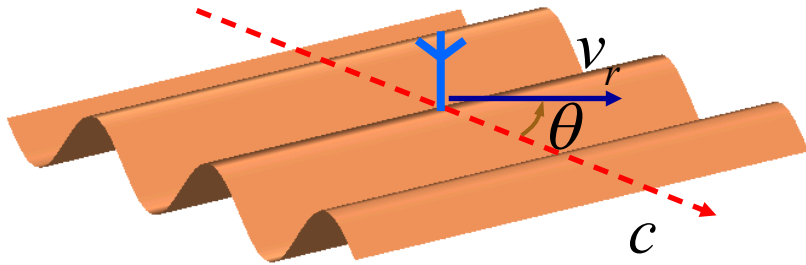
Small-scale fading - Rayleigh fading



$$p(x) = \begin{cases} \frac{x}{\rho} e^{-x^2/2\rho} & x > 0 \\ 0 & \text{otherwise} \end{cases}$$



Doppler shifts



Receiving antenna moves with speed v_r at an angle θ relative to the propagation direction of the incoming wave, which has frequency f_0 .

Frequency of received signal:

$$f = f_0 + \nu$$

where the Doppler shift is

$$\nu = -f_0 \frac{v_r}{c} \cos(\theta)$$

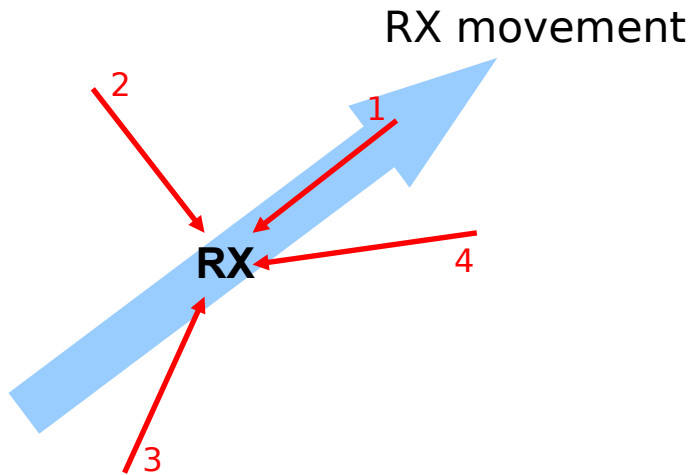
The maximal Doppler shift is

$$\nu_{\max} = f_0 \frac{v}{c}$$



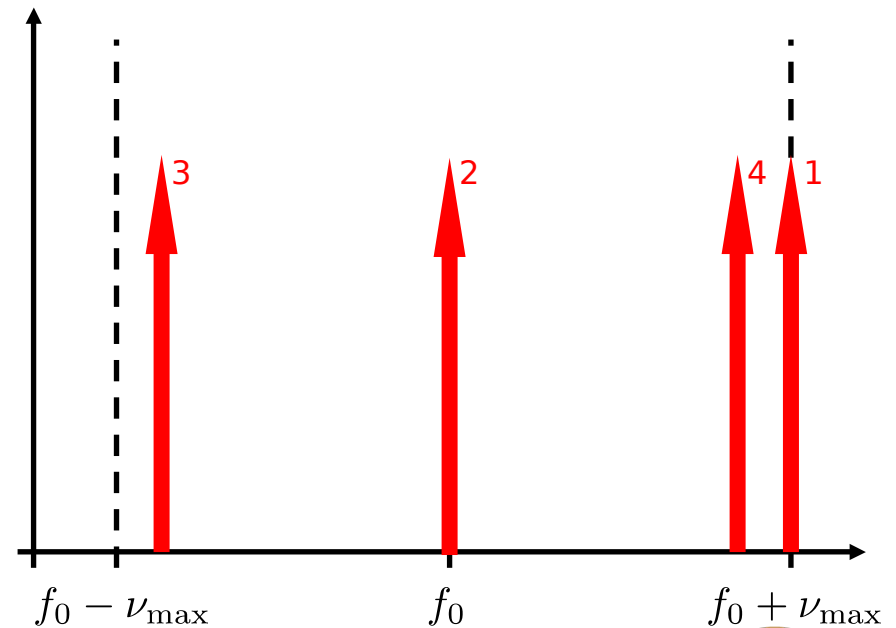
More than one incoming wave

Incoming waves from several directions
(relative to movement or RX)



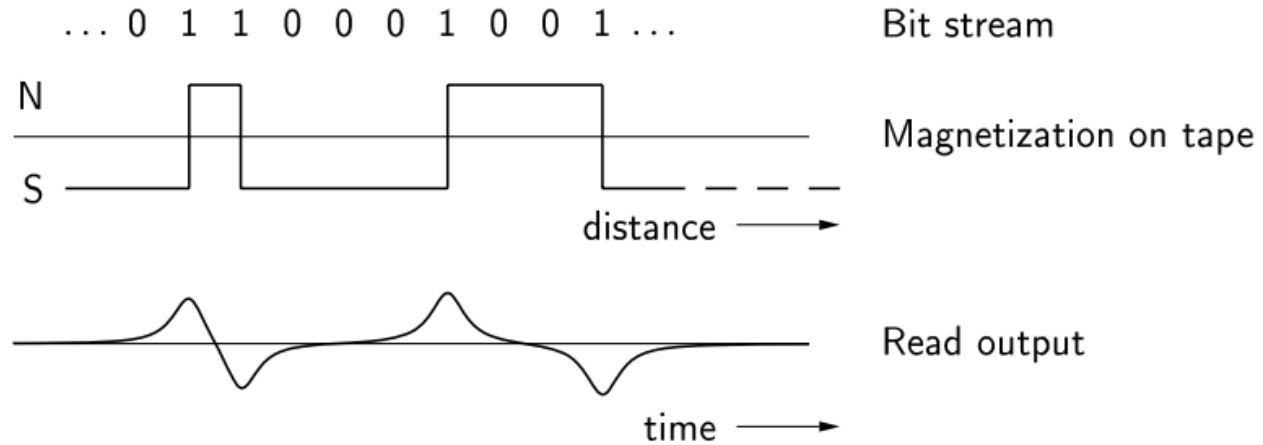
All waves of equal strength in this example, for simplicity.

Spectrum of received signal when a f_0 Hz signal is transmitted.



Magnetic recording

- Store magnetic field with different orientation



SUMMARY

- Wires, cables and fibers
 - Wires and cables are LTI systems
 - Bandwidth of wires and cables depend on length
 - Coaxial cables can carry higher bandwidths than wires
 - Fibers have low attenuation
- Radio channels
 - Free-space propagation
 - Antenna gains
 - Friis' law
 - Noise properties and calculation
 - Multi-path propagation: Fading and Doppler shifts
- Magnetic recording
 - Storing messages by changing magnetization of tape
(Transmitting to another time)





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