ETSF15 Analog/Digital

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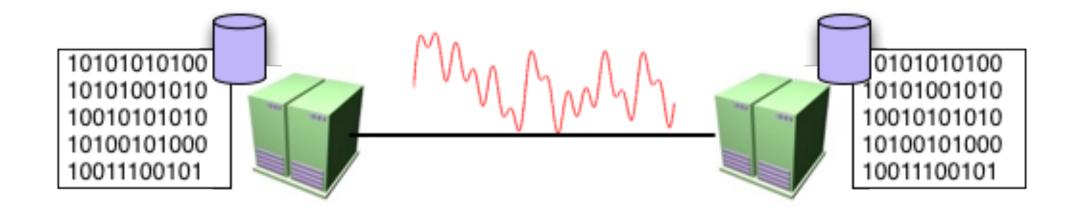


Physical layer

- Analog vs digital
 - Sampling, quantisation
- Modulation
 - Represent digital data in a continuous world
- Disturbances
 - Noise and distortion
 - Digital data processing
 - Information

Data vs Signal vs Information

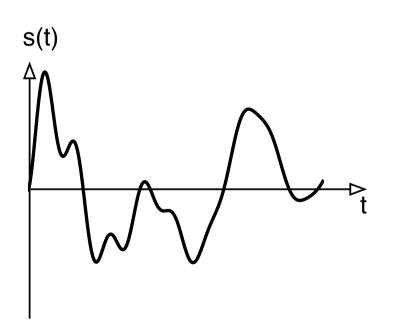
- **Data**: Static representation of information
- Signal: Dynamic representation of information
- Information: Information content in data or signal



Analog vs digital

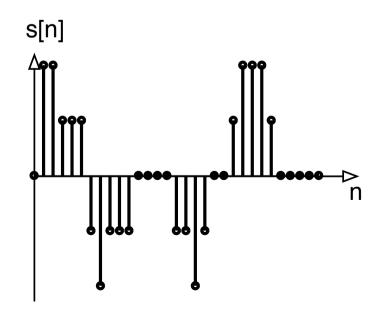
Analog

- Continuous time and amplitude signal
- Electrical/optical domain



Digital

- Discrete time and amplitude
- Binary representation



Digitalization of analog signals

Performed in three steps:

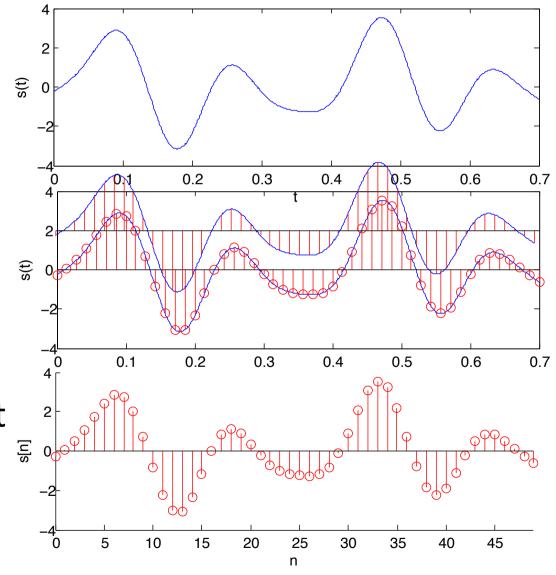
- 1. Sampling: Discretization in time
- 2. Quantization: Discretization in amplitude
- 3. Encoding: Binary representation of amplitude levels

In practice:

- ADC: Analog to Digital Converter
- DAC: Digital to Analog Converter

Sampling

- The process of discretizing time of a continuous signal. $s[n] = s(nT_s)$
- Sample time: T_s
- Sample frequnecy: $F_s = 1/T_s$
- Loose information about time



Shannon-Nyquist Sampling Theorem

• If s(t) is a band limited signal with highest frequency component F_{max} , then s(t) is uniquely determined by the samples $s[n] = s(nT_s)$ if and only if

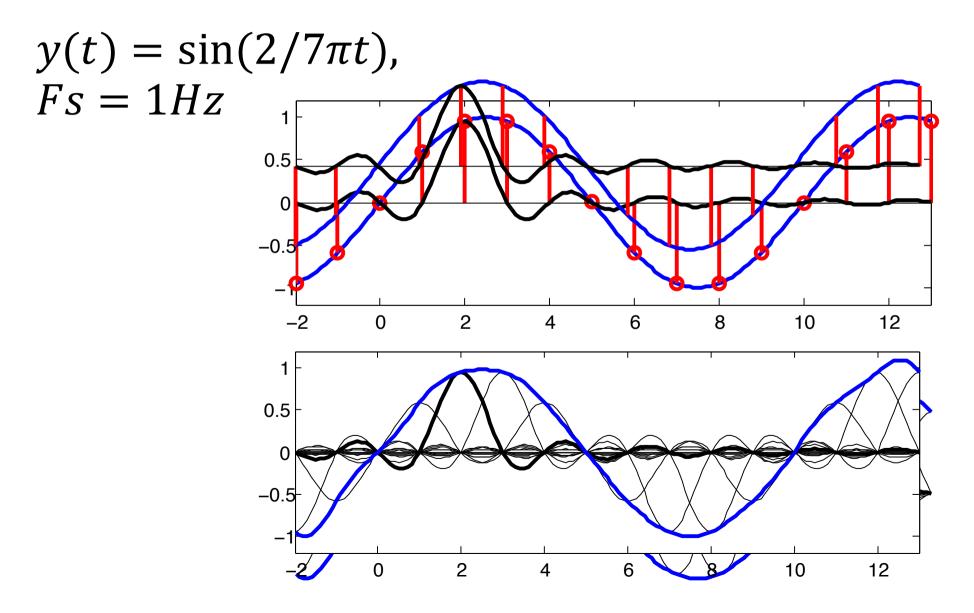
$$F_s = \frac{1}{T_s} \ge 2F_{max}$$

The signal can be (perfectly) reconstructed with

$$s(t) = \sum_{n=-\infty}^{\infty} s[n]sinc\left(\frac{t-nT_s}{T_s}\right)$$

• Fs/2 is the Nyquist frequency and $2F_{max}$ the Nyquist rate

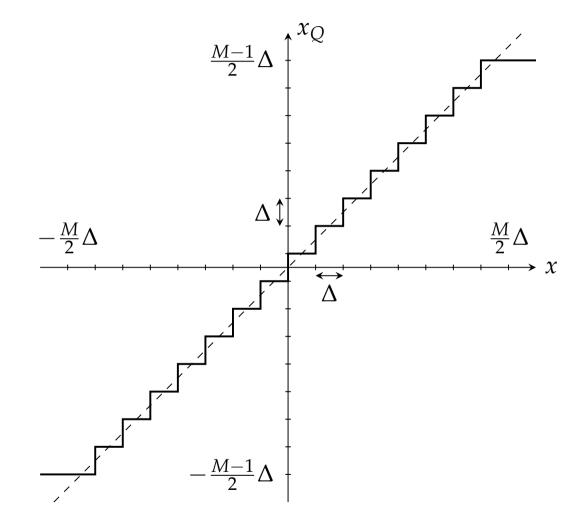
Reconstruction Example



Aliasing 0.5 $y(t) = \cos(2\pi7t)$ 0 $F_s = 10 Hz$ -0.5 0.7 0.5 03 0.2 06 0 4 Reconstruction to lowest possible frequency Reconstruct freq: $f_{rec} = f_{rec}$ $-F_{s}/2$ λkF_s s.t. $f_{rec} \leq F_{s}$ $y(t) = \cos(2\pi 3t)$ 0.5 0 -0.5 0.1 0.2 0.3 0.6 0.7 0.4 0 0.5

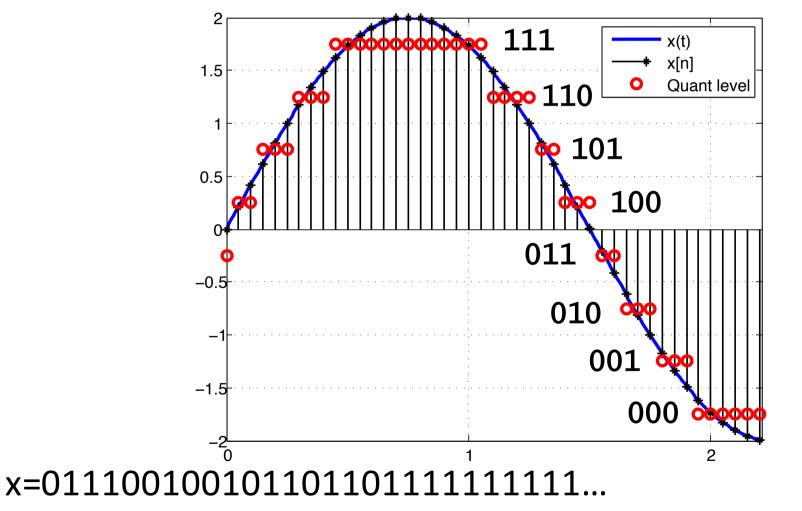
Quantization

- Uniform quantization for k bits
- *M=2^k* equidistant levels
- Represent sample with k bits



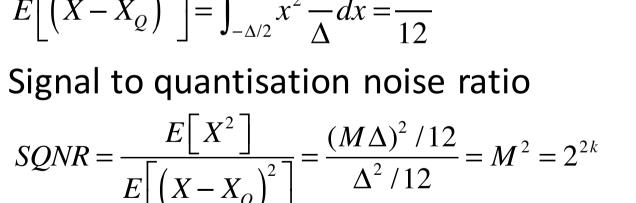
Encoding

Representation of quantized samples in bits

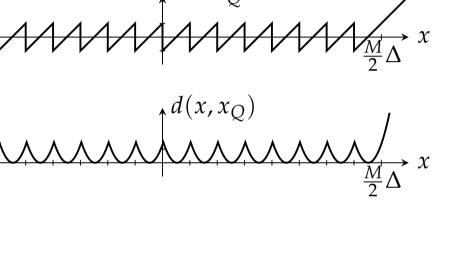


Quantisation distortion

- Distortion (noise): $d(x,x_o) = (x - x_o)^2$
- Average distortion for uniform input: $E\left[\left(X - X_Q\right)^2\right] = \int_{-\Lambda/2}^{\Lambda/2} x^2 \frac{1}{\Lambda} dx = \frac{\Delta^2}{12}$

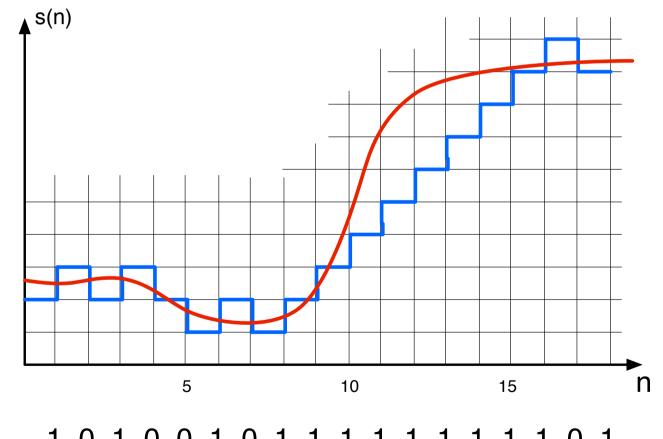


$$SQNR_{dB} = 10\log 2^{2k} = k \cdot 6dB$$



Delta modulation

- Represent change in amplitude with 1 bit
 - 1:+1
 - 0: -1
- Must use higher sampling rate



101001011111111101

Examples

Telephony

F_{max}= 4 kHz F_s= 8 kHz (samples per sec) 8 bit/sample => 64 kb/s

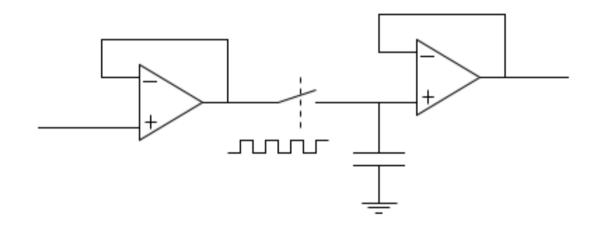
CD

F_{max}= 20 kHz F_s= 44.1 kHz (samples per sec) 16 bit/sample => 705.6 kb/s 2 channels (stereo) => 1.4 Mb/s

Principles of circuits

- Sample and hold (sampling)
- ADC (quantisation)
- DAC (reconstruction)

Sample and hold

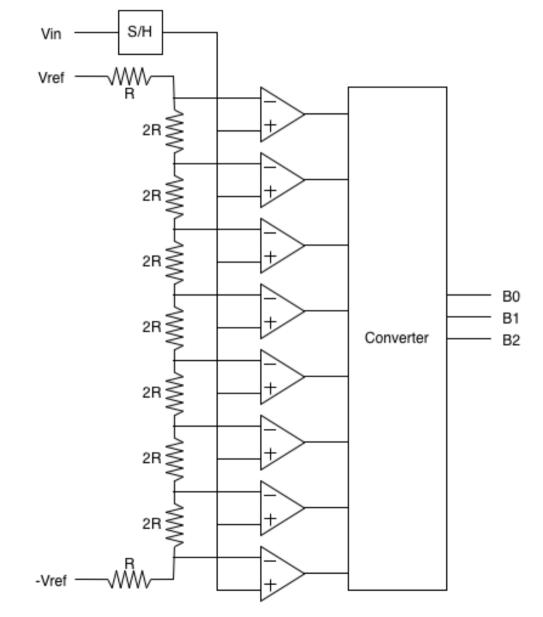


ADC Analog to Digital Converter

- Sample and hold circuit freeze the analog value during conversion
- ADC methods
 - Direct conversion (flash ADC)
 - Integrating
 - Wilkinson
 - Sigma-delta
 - Etc (see e.g.

https://en.wikipedia.org/wiki/Analog-to-digital_converter)

ADC Direct conversion example (3 bit)



DAC Digital to Analaog Coverter

- Pulse width modulator
- R-2R ladder
- Interpolating
- Binary weighting

See more on https://en.wikipedia.org/wiki/Digital-to-analog_converter

DAC Example

Weighted resistor

R-2R ladder

