

EITG05 – Digital Communications

Week 3, Lecture 1

Information Transmission with Carrier Modulation Techniques

Michael Lentmaier Monday, September 11, 2017

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Week 3, Lecture 1

Chapter 3: Information Transmission with Carrier Modulation Techniques

- ▶ 3.1 Bandpass signals: basic concepts
- ▶ 3.2 Digital information transmission
- ▶ 3.3 Analog information transmission
 - 3.3.1 Amplitude modulation
 - 3.3.2 Frequency modulation

Pages 117 - 136 and 139 - 152

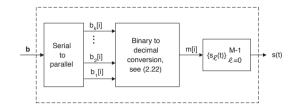
Exercises: 2.26, 2.27 (only 2,3,4,7), 2.30,

Example 3.1 on page 121, 3.1, 3.2, 3.3



Where are we now?

What we have done so far: (Chapter 2)



- ► Concepts of digital signaling: bits to analog signals
- ▶ Average symbol energy \overline{E}_s , Euclidean distance $D_{i,j}$
- ► Bandwidth of the transmit signal

Now: Carrier Modulation Techniques (Chapter 3)

- ▶ Bandpass signals, digital modulation, analog modulation
- ▶ *N*-ray channel model, noise

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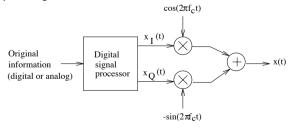


Bandpass Signals

► A general bandpass signal can always be written as

$$x(t) = x_I(t) \cos(2\pi f_c t) - x_Q(t) \sin(2\pi f_c t), \quad -\infty \le t \le \infty$$

- $x_I(t)$: inphase component $x_Q(t)$: quadrature component
- ► Corresponding transmitter structure:



► The information is contained in the signals $x_I(t)$ and $x_Q(t)$ (for both analog or digital modulation)

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▶ Not only wireless systems use carrier modulation

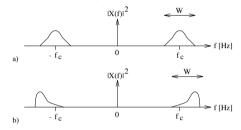


Spectrum of bandpass signals

ightharpoonup Computing the Fourier transform of x(t) we get

$$X(f) = \frac{X_I(f + f_c) - j \, X_Q(f + f_c)}{2} \, + \, \frac{X_I(f - f_c) + j \, X_Q(f - f_c)}{2}$$

- Normally, $X_I(t)$ and $X_Q(t)$ have baseband characteristic, and f_C is much larger than their bandwidth
- ightharpoonup The spectrum can be symmetric or non-symmetric around f_c

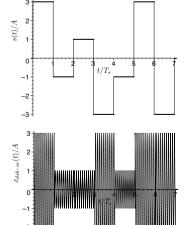


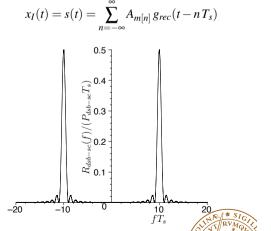
Remember: real signals x(t) always have even |X(f)|

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Example 3.1: 4-ary PAM





DSB-SC Carrier Modulation

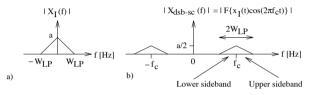
- ► Double sideband-suppressed (DSB-SC) carrier modulation is a special case of our general model
- ▶ In this case only $x_I(t)$ contains information and $x_O(t) = 0$, i.e.,

$$x_{dsb-sc}(t) = x_I(t)\cos(2\pi f_c t)$$

▶ The Fourier transform then simplifies to

$$X(f) = \frac{X_I(f + f_c)}{2} + \frac{X_I(f - f_c)}{2}$$

▶ $X_I(f)$ is symmetric around $f = 0 \implies X_I(f)$ is symmetric around f_c



Where does the name come from?

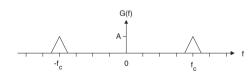
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How can we revert the frequency shift to f_c ?

Hint: check Example 2.19 (p. 68)

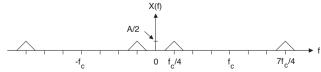


Find the frequency content of

$$x(t) = g(t) \cos(2\pi f_0 t)$$
, $f_0 = 3f_c/4$

Solution:

If we apply (2.157) using G(f) above, we obtain the frequency content in x(t) as

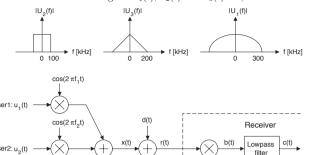


How should we choose f_0 to get the baseband signal back?



Problem 3.9

In the three-user (digital) communication system below, the frequency content in the user information signals $u_1(t)$, $u_2(t)$ and $u_3(t)$ are,



It is known that the individual carrier frequencies are: $f_1=3.5$ MHz, $f_2=4.0$ MHz, $f_3=3$ MHz. The disturbance d(t) is $d(t)=\cos(2\pi 2f_dt)$ where $f_d=1.7$ MHz.

Only frequencies up to 100 kHz pass the lowpass filter.

cos(2 πf. t)



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cos(2 \pi f_t)

I-Q Diagram

► In the representation

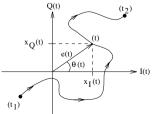
$$x(t) = x_I(t)\cos(2\pi f_c t) - x_Q(t)\sin(2\pi f_c t)$$

the information is contained in the inphase component $x_I(t)$ and quadrature component $x_Q(t)$

► In the representation

$$x(t) = e(t)\cos(2\pi f_c t + \theta(t)), \quad -\infty \le t \le \infty$$

the information is contained in the envelope e(t) and instantaneous phase $\theta(t)$



connection: I-Q diagram



Envelope and Phase

- ▶ A frequency shift corresponds to a multiplication with $e^{j2\pi f_c t}$
- ▶ For connecting this to the cosine and sine function we use

$$e^{j2\pi f_c t} = \cos(2\pi f_c t) + j\sin(2\pi f_c t)$$

► The general bandpass signal can then be written in terms of a frequency shifted version of a complex signal $x_I(t) + jx_O(t)$

$$x(t) = x_I(t) \cos(2\pi f_c t) - x_Q(t) \sin(2\pi f_c t)$$

= $Re\left\{ \left(x_I(t) + j x_Q(t) \right) e^{j2\pi f_c t} \right\}$

ightharpoonup Expressing $x_I(t) + jx_O(t)$ in terms of magnitude and phase we get

$$x(t) = e(t)\cos(2\pi f_c t + \theta(t)), \quad -\infty \le t \le \infty$$

with

$$e(t) = \sqrt{x_I^2(t) + x_Q^2(t)} \ge 0$$

$$x_I(t) = e(t)\cos(\theta(t))$$

$$x_O(t) = e(t) \sin(\theta(t))$$

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Digital Information Transmission

- ▶ In Chapter 2 the signal alternatives $s_{\ell}(t)$ could have arbitrary shape within the signaling interval $0 \le t \le T_s$
- ► The bandpass signal for digital modulation then has the form

$$x(t) = x_I(t)\cos(2\pi f_c t) - x_Q(t)\sin(2\pi f_c t)$$

$$= \left(\sum_{n=-\infty}^{\infty} s_{m[n],I}(t-nT_s)\right)\cos(2\pi f_c t)$$

$$-\left(\sum_{n=-\infty}^{\infty} s_{m[n],Q}(t-nT_s)\right)\sin(2\pi f_c t)$$

► In case of *M*-ary QAM we have

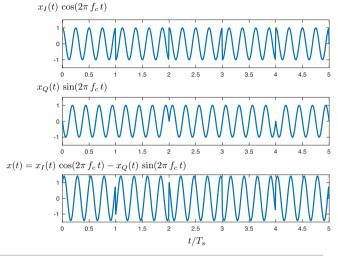
$$x_I(t) = \sum_{n=-\infty}^{\infty} A_{m[n]} g(t - nT_s) , \quad x_Q(t) = \sum_{n=-\infty}^{\infty} B_{m[n]} g(t - nT_s)$$

► Also *M*-ary FSK signals have bandpass characteristics



A simple Matlab exercise

How does a QPSK signal look like? Here is an example:



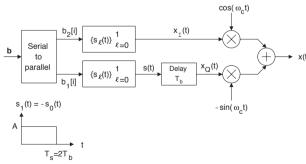


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Example 3.5: offset QPSK

Below, two information carrying baseband signals $x_I(t)$ and s(t) are first generated. Binary antipodal signaling with a rectangular pulse shape is used for both $x_I(t)$ and s(t). The signal $x_O(t)$ is a delayed version of s(t), $x_O(t) = s(t - T_b)$.



The information bit rate (in b) is $R_b = 1/T_b$. Hence, the signaling rate in the quadrature components is $R_s = R_b/2$.

QPSK signal with delayed transmission of $x_O(t)$

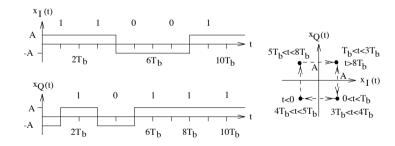
And how it was done:

```
t=0:0.01:5;
 4 -
5 -
6 -
           fc=4;
          pRec=ones(1,(length(t)-1)/5);
sI=zeros(1,length(t)); s0=zeros(1,length(t));
          indPulse=1:(length(t)-1)/5;
 10 -
11 -
12 -
          for i=1:length(dataI),
sI(indPulse)=dataI(i)*pRec;
             indPulse=indPulse+length(indPulse);
 13
14
15 - 16 - 17 - 18 - 19 - 20 - 21 - 22 - 25 - 26 - 27 - 28 - 29 - 30 - 31 - 32 - 33 - 33 - 33 - 34
           dataQ=[-1 -1 1 1 -1];
           indPulse=1:(length(t)-1)/5;
           for i=1:length(dataQ),
            sQ(indPulse)=dataQ(i)*pRec;
indPulse=indPulse+length(indPulse);
          sCarI=cos(2*pi*t*fc); sCarQ=sin(2*pi*t*fc);
          subplot(3,1,1); plot(t,sI.*sCarI);
          set(gca, 'YLim', [-1.5 1.5]); xlabel('fT_s');
          subplot(3,1,2); plot(t,sQ.*sCarQ);
          set(gca, 'YLim', [-1.5 1.5]); xlabel('fT_s');
          subplot(3,1,3); plot(t,sI.*sCarI - sQ.*sCarQ);
          set(gca, 'YLim', [-1.5 1.5]); xlabel('fT_s');
                                                                                  Ln 32 Col 30
```

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Example 3.5: offset QPSK



► Special feature:

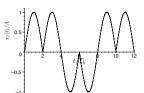
 $x_I(t)$ and $x_Q(t)$ can never change at the same time

- ightharpoonup it follows that the envelope does not pass the origin, i.e., e(t) > 0
- ▶ the variation of instantaneous power $\mathcal{P}(t) = e^2(t)/2$ is small, which allows more efficient power amplifiers

Example 3.6: constant envelope signaling

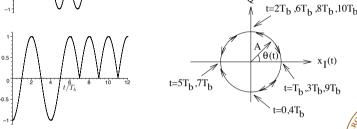
Change pulse shape:

half cycle sinusoidal $g_{hcs(t)}$ instead of $g_{rec}(t)$



The squared envelope becomes

$$\begin{split} e^2(t) &= x_I^2(t) + x_Q^2(t) \\ &= A^2 \sin^2(\pi t/(2T_b)) + A^2 \cos^2(\pi t/(2T_b)) \\ &= A^2 \quad \Rightarrow \text{constant envelope } e(t) = A \end{split}$$



Continuous phase modulation (CPM) is used in GSM

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From 2G to 4G

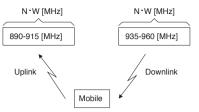
- GSM: (Global System for Mobile Communications)
 based on combined time-division multiple access (TDMA) and frequency division multiple access (FDMA)
- ▶ UMTS: (Universal Mobile Telecommunications Service) based on wideband code division multiple access (W-CDMA) each user has an individual code, no TDMA or FDMA
- LTE (advanced): (Long Term Evolution) orthogonal frequency-division multiple access (OFDMA)

Multiple access:

refers to how different active users are separated

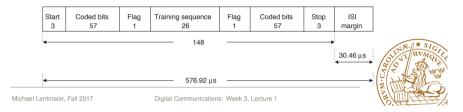


Example 3.7: GSM



Each sub-band of W [Hz] carries information from X users, which are time-multiplexed using X time-slots. The total number of speech-channels (or data-channels) in the uplink (and in the downlink) is $N \cdot X$.

A specific user is allocated one of the N sub-bands, and one of the X time-slots. A time-slot has duration 576.92 [μ s], and 148 binary symbols are transmitted within this time, see the figure below.



Analog Information Transmission

- Suppose that the information signal is an analog waveform a(t) Examples: music, speech, video
- ▶ If we use digital modulation, the waveform a(t) is first converted to a binary sequence b[i], which then is mapped to signals $s_{\ell}(t)$
- ▶ In case of analog modulation, the waveform a(t) is used directly to modulate the carrier signal
- lackbox Let v(t) denote the bandpass signal of an analog transmitter

$$v(t) = v_I(t)\cos(2\pi f_c t) - v_Q(t)\sin(2\pi f_c t), \quad -\infty \le t \le \infty$$

= $e(t)\cos(2\pi f_c t + \theta(t))$

Amplitude modulation (AM):

the waveform a(t) modulates the envelope e(t) only

► Frequency modulation (FM):

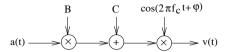
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here a(t) modulates the instantaneous phase $\theta(t)$ only

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Amplitude Modulation (AM)



► The AM signal is the sum of a DSB-SC signal and carrier wave

$$v(t) = (a(t)B + C)\cos(2\pi f_c t + \varphi)$$

= $a(t)B\cos(2\pi f_c t + \varphi) + C\cos(2\pi f_c t + \varphi)$

► Let us introduce the modulation index

$$m = \frac{B a_{max}}{C} \le 1$$
, where $a_{max} = \max |a(t)|$

▶ Using the normalized signal $a_n(t) = a(t)/a_{max}$ we can write

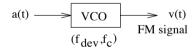
$$v(t) = (1 + ma_n(t)) C \cos(2\pi f_c t + \varphi)$$

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Frequency Modulation (FM)



▶ With FM modulation, the transmitted signal

$$v(t) = \sqrt{2P}\cos(2\pi f_c t + \theta(t))$$

is generated by a voltage controlled oscillator (VCO)

 \blacktriangleright The information carrying signal a(t) is related to the phase $\theta(t)$ by

$$\frac{1}{2\pi} \frac{d\theta(t)}{dt} = f_{dev} \cdot a(t)$$

ightharpoonup The signal a(t) hence modulates the instantaneous frequency

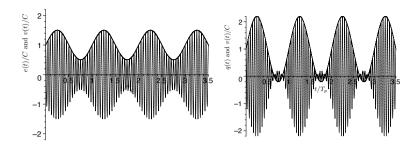
$$f_{ins}(t) = f_c + \frac{1}{2\pi} \frac{d\theta(t)}{dt} = f_c + f_{dev} a(t)$$

► FM modulation is a non-linear operation, hard to analyze



Example: AM signal

$$e(t)/C = 1 + ma(t)$$
, $a_n(t) = \sin(2\pi f_p t)$, $f_p = 1/Tp$



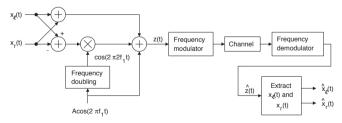
- ► m = 0.5 < 1: the information signal $a_n(t)$ is contained in the envelope e(t)
- m=1.2>1: (right picture) overmodulation: the baseband signal $q(t)=(1+1.2\,a_n(t))$ is no longer equal to e(t)

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Example 3.13: FM stereo

A possible block-diagram of conventional analog FM stereo is shown below.



 $x_\ell(t)$ and $x_r(t)$ denotes the left and the right audio-channel, respectively, and they are both bandlimited to 15 [kHz]. The frequency $f_1=19$ [kHz] (often referred to as a so-called pilot-tone).

