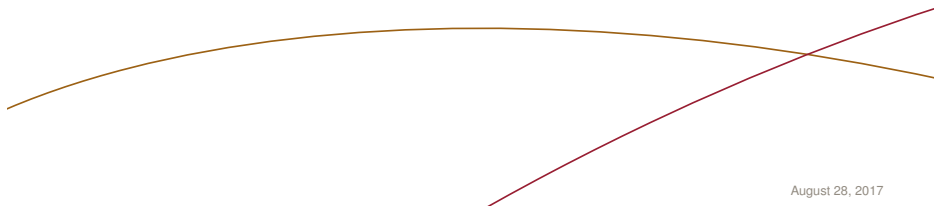


# EITG05 – Digital Communications

## Week 1, Lecture 1

Introduction, Overview, Basic Concepts (p. 1–32)

Michael Lentmaier  
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## Analog versus digital

- ▶ **Analog communication:**  
the original messages produced by the source are analog
- ▶ **Digital communication:**  
the messages are digital, i.e., can be represented by discrete numbers (digits)

**Example 1:** I speak and you listen to the acoustic sound wave

**Example 2:** I record my speech to MP3 and send it to you, who plays it back on your computer or phone

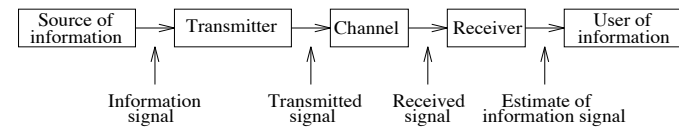
**Example 3:** I use morse code and a flashlight to transmit a message to my neighbor

In all cases some analog medium has to be used during the transmission at some point



## What is communication?

- ▶ The purpose of a communication system is to **transmit messages** (information) from a source to a destination  
**Examples:** sound, picture, movie, text, etc.
- ▶ The messages are converted into **signals** that are suitable for transmission
- ▶ The physical medium for transmission is called the **channel**



- ▶ The received signal is used to estimate the messages

Can you give some examples?



## Digital Communications

### We are in a global digital (r)evolution

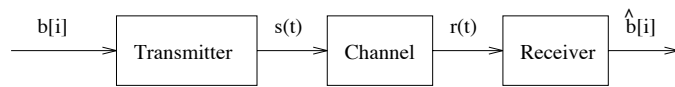
- ▶ Mobile data and telephony (GSM, EDGE, 3G, 4G, 5G)
- ▶ Digital radio and television, Bluetooth, WLAN
- ▶ Data storage, CD, DVD, Flash, magnetic storage
- ▶ Optical fiber, DSL (long range, high rate)
- ▶ Cloud computing, big data, distributed storage
- ▶ Connected devices, Internet of things, machine-to-machine communication, distributed control, cyber physical systems

The large number of different application scenarios require flexible communication solutions (data rate / delay / reliability / complexity)

**Remark** storage of data falls also into the category of our communication system model (check why)



## Scope of this course



- ▶ Transmitter principles: bits to analog signals (Chap. 2)
- ▶ Characteristics of the communication link (Chap. 3,6)
- ▶ Receiver principles: analog noisy signals to bits (Chap. 4,5,6)

Requirements:

- ▶ Data should arrive correctly at the receiver
- ▶ High bit rates are desirable
- ▶ Energy/power efficiency
- ▶ Bandwidth efficiency

What are the technical solutions and challenges?



## Not in this course

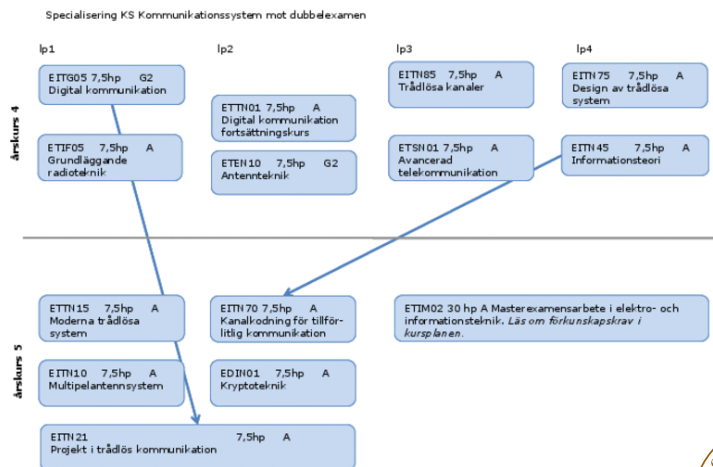
- ▶ Analog to digital conversion, sampling theorem, quantization  
⇒ basic signals & systems or signal processing course
- ▶ Source coding (compression)  
⇒ covered in information theory course (elective)
- ▶ Channel coding (robust and reliable communication)  
⇒ covered in separate course (elective)
- ▶ Cryptography (secure communication)  
⇒ covered in separate course (elective)

There exist a large number of specialized courses that can be taken after this basic course.

There is also a project course in wireless communications.



## Related courses from the wireless program



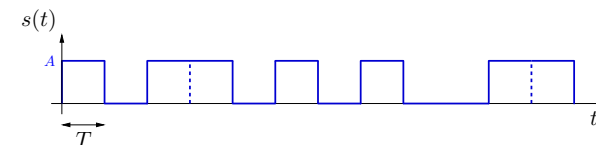
## The Transmitter

How can we map digital data to analog signals?

$$b[i] = 1 \ 0 \ 1 \ 1 \ 0 \ 1 \ 0 \ 1 \ 0 \ 0 \ 1 \ 1$$

A simple approach:

apply some voltage  $A$  during transmission of a 1



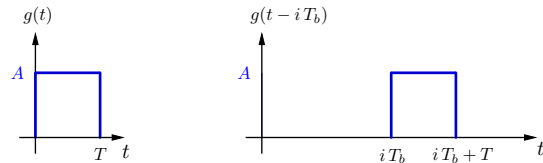
**Basic operation:** (more general)

represent the sequence of information bits  $b[i]$  by a sequence of analog waveforms, resulting in the transmit signal  $s(t)$



## The Transmitter

- ▶ The analog waveform corresponding to the bit  $b[i]$  can be written as a time-shifted version of an elementary pulse  $g(t)$



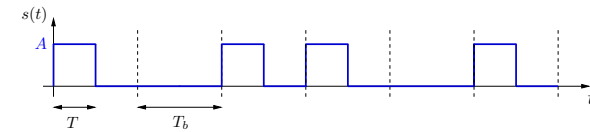
- ▶  $T_b$  is the **information bit interval**, while  $T$  is the **pulse duration**
- ▶ For now we assume that  $T \leq T_b$ , i.e., the pulses do not overlap
- ▶ We can now represent the transmit sequence  $s(t)$  as follows

$$s(t) = b[0]g(t) + b[1]g(t - T_b) + b[2]g(t - 2T_b) + \dots$$



## What data rate can we achieve?

- ▶ We could also choose a shorter pulse, with  $T < T_b$



- ▶ An important parameter is the **information bit rate**

$$R_b = \frac{B}{\tau} \text{ [bps] (bits per second) ,}$$

if the source produces  $B$  information bits during  $\tau$  seconds

- ▶ We can write

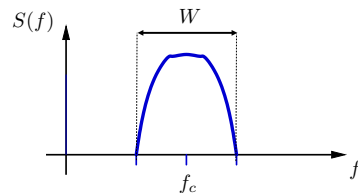
$$T_b = \frac{1}{R_b}$$

**Question:** What happens with  $R_b$  if  $T_b$  is larger than  $T$ ?



## What bandwidth is required?

- ▶ The **bandwidth**  $W$  of the transmit signal is a valuable resource



- ▶ For typical pulses  $g(t)$  the bandwidth  $W$  is proportional to  $\frac{1}{T}$
- ▶ More details about bandwidth follow next week
- ▶ A challenging goal is to achieve a large **bandwidth efficiency**

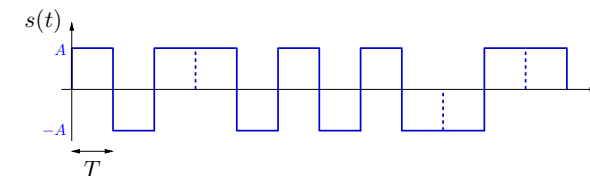
$$\rho = \frac{R_b}{W} \left[ \frac{\text{b/s}}{\text{Hz}} \right]$$

**Question:** What happens when the pulse duration gets small?



## Variations of our signaling example

- ▶ In our example we only send a signal when  $b[i] = 1$ . This modulation type is called **on-off signaling**
- ▶ Instead we could send a pulse with amplitude  $-A$  for  $b[i] = 0$ :



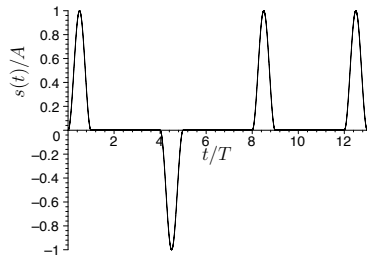
This modulation type is called **antipodal signaling**

- ▶ We could also choose a different **pulse shape**  $g(t)$

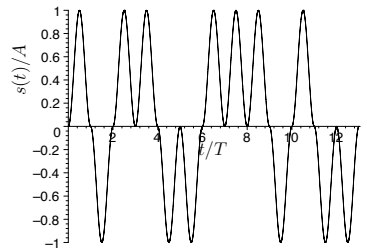
**In this chapter:** different modulation types and their properties



## Another pulse example ( → p. 10)

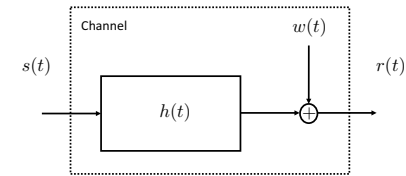


What are the input sequences  $b[i]$  here?



## The Channel

- ▶ The channel is often modeled as time-invariant filter with noise



- ▶  $h(t)$  is the channel impulse response and  $w(t)$  the additive noise
- ▶ The received signal becomes

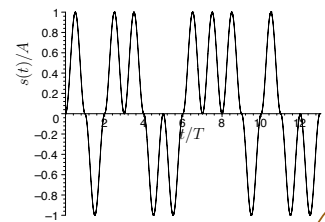
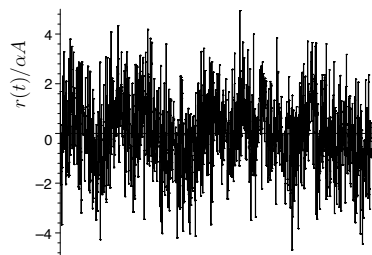
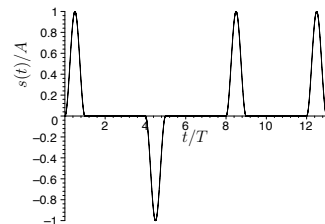
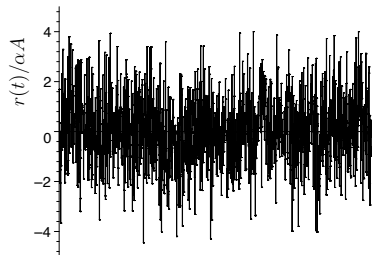
$$r(t) = s(t) * h(t) + w(t) = \int_{-\infty}^{\infty} h(\tau) s(t - \tau) d\tau + w(t)$$

- ▶ For now we assume the simple case ( $\alpha$ : attenuation)

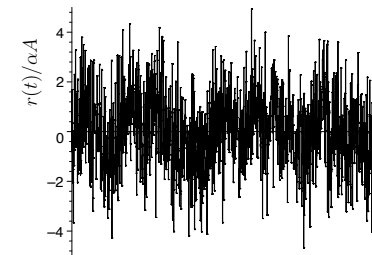
$$h(t) = \alpha \delta(t) \Rightarrow r(t) = \alpha s(t) + w(t)$$



## Example: noisy signal at the receiver (p. 13)



## The Receiver



- ▶ Due to the attenuation  $\alpha$  during transmission, the noise  $w(t)$  has a strong impact on the received signal  $r(t)$
- ▶ A well designed receiver can still detect the symbols correctly!  
In this example, only 1 of  $10^5$  bits will be wrong in average
- ▶ We will learn about the receiver and its performance later, in Chapters 4 and 5



## Bit Errors

- ▶ The **bit error probability** is an important measure of communication performance
- ▶ It is defined as the average number of information bit errors per detected information bit

$$P_b = \frac{E\{B_{err}\}}{B}$$

### Example:

- ▶ Assume a bit rate of 1 Mbps and that 10 bit errors occur per hour *on the average*. What is the bit error probability?
- ▶ The total number of bits in an hour is

$$B = 1000000 \cdot 60 \cdot 60 = 3.6 \cdot 10^9$$

This gives

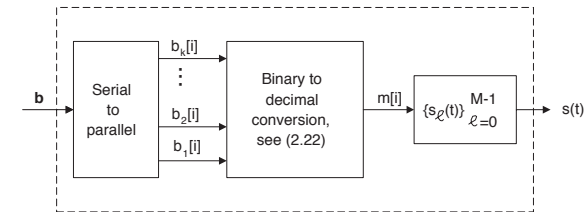
$$P_b = \frac{10}{B} = 2.78 \cdot 10^{-9}$$

⇒ **Computer simulations become very time consuming!**



## Increasing the message alphabet

- ▶ Up to this point we have considered **binary signaling** only
- ▶ Each bit  $b[i]$  was mapped to one of two signals  $s_0(t)$  or  $s_1(t)$
- ▶ More generally, we can combine  $k$  bits  $b_1[i], b_2[i], \dots, b_k[i]$  to a single message  $m[i]$ , which then is mapped to a signal  $s_\ell(t)$



- ▶ In case of **M-ary signaling**, one of  $M = 2^k$  messages  $m[i]$  is transmitted by its corresponding signal alternative

$$s_\ell(t) \in \{s_0(t), s_1(t), \dots, s_{M-1}(t)\}$$



## M-ary signaling

**Example:**  $k = 2, M = 2^2 = 4$

The binary sequence

$$b_n[i] = 1 \ 0 \ 1 \ 1 \ 0 \ 1 \ 0 \ 1 \ 0 \ 0 \ 1 \ 1$$

is mapped by

$$m[i] = \sum_{n=1}^k b_n[i] 2^{n-1} = b_1[i] + b_2[i] \cdot 2$$

to  $M = 4$  signal alternatives

$$\begin{aligned} b[i] = 00 &\leftrightarrow m[i] = 0 \leftrightarrow s_0(t) & b[i] = 10 &\leftrightarrow m[i] = 1 \leftrightarrow s_1(t) \\ b[i] = 01 &\leftrightarrow m[i] = 2 \leftrightarrow s_2(t) & b[i] = 11 &\leftrightarrow m[i] = 3 \leftrightarrow s_3(t) \end{aligned}$$

The message sequence becomes

$$m[i] = 1 \ 3 \ 2 \ 2 \ 0 \ 3$$

With  $k = 14$  there are  $M = 16384$  signal alternatives



## Symbol rate versus bit rate

- ▶ Since  $k$  information bits are transmitted with each symbol, the **symbol interval** (symbol time) becomes

$$T_s = k T_b$$

- ▶ Accordingly, the **symbol rate** (signaling rate) is given by

$$R_s = \frac{1}{T_s} \left[ \frac{\text{symbols}}{\text{s}} \right] = \frac{R_b}{k}$$

- ▶ When the message equals  $m[i] = j$  then  $s_j(t - iT_s)$  is sent

$$s(t) = s_{m[0]}(t) + s_{m[1]}(t - T_s) + s_{m[2]}(t - 2T_s) + \dots$$

How does  $k$  affect the bandwidth efficiency  $\rho$ ?

**Remark:** Be careful with the different definitions of time:  
 $t$ : time variable  $T$ : pulse duration  $T_b$ : bit time  $T_s$ : symbol time



## Signal energy and power

- The **symbol energy**  $E_\ell$  of a signal alternative  $s_\ell(t)$  is given by

$$E_\ell = \int_0^{T_s} s_\ell^2(t) dt < \infty, \quad \ell = 0, 1, \dots, M-1$$

- An important system parameter is the **average symbol energy**

$$\bar{E}_s = \sum_{\ell=0}^{M-1} P_\ell E_\ell$$

and the **average signal energy per information bit**

$$\bar{E}_b = \frac{\bar{E}_s}{k}$$

- The **average signal power** is then given by

$$\bar{P} = R_s \bar{E}_s = \frac{R_b}{k} \cdot k \bar{E}_b = R_b \bar{E}_b$$



## Signal energy and power

- The attenuation  $\alpha$  and the noise  $w(t)$  determine the quality of a communication link

$$r(t) = \alpha s(t) + w(t)$$

### Example:

If a transmitted signal  $s(t)$  has energy  $\bar{E}_b$ , how much energy  $\mathcal{E}_b$  is then in the received signal  $z(t) = \alpha \cdot s(t)$  if  $\alpha = 0.001$ ?

- Using  $z^2(t) = \alpha^2 s^2(t)$  we obtain

$$\bar{P}_z = \alpha^2 \bar{P} = \alpha^2 R_b \bar{E}_b$$

$$\text{and } \mathcal{E}_b = \frac{\bar{P}_z}{R_b} = \alpha^2 \frac{\bar{P}}{R_b} = \alpha^2 \bar{E}_b$$

- If  $\alpha = 0.001$  then the power is reduced by a factor  $10^{-6}$

This will increase the bit error probability!



## How well can we distinguish two signals?

- The **squared Euclidean distance** between two signals  $s_i(t)$  and  $s_j(t)$  is defined as

$$\begin{aligned} D_{i,j}^2 &= \int_0^{T_s} (s_i(t) - s_j(t))^2 dt \\ &= \int_0^{T_s} s_i^2(t) + s_j^2(t) - 2s_i(t)s_j(t) dt \\ &= E_i + E_j - 2 \int_0^{T_s} s_i(t)s_j(t) dt \end{aligned}$$

- Two signals are **antipodal** if

$$s_i(t) = -s_j(t), \quad 0 \leq t T_s$$

- Two signals are **orthogonal** if

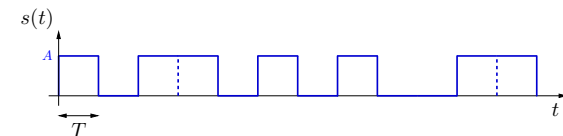
$$\int_0^{T_s} s_i(t)s_j(t) dt = 0$$

Antipodal signals have larger Euclidean distance



## Euclidean distance example $M = 2$

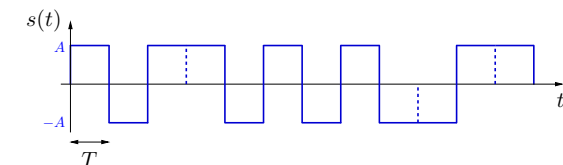
### Case 1: on-off signaling



$s_0(t) = A$  and  $s_1(t) = 0$  for  $0 < t < T_s = T$ , which gives  $D_{0,1}^2 = 2\bar{E}_b$

**Observe:** on-off signaling is orthogonal

### Case 2: antipodal signaling



$s_0(t) = A$  and  $s_1(t) = -A$  for  $0 < t < T_s = T$ , and  $D_{0,1}^2 = 4\bar{E}_b$



## Examples of pulse shapes: Appendix D

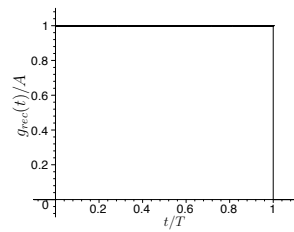


Figure D.1:  $g_{rec}(t)/A$ .

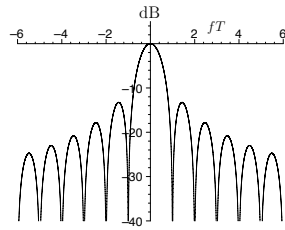


Figure D.2:  $\frac{|G_{rec}(f)|^2}{E_g T}$  in dB.

### 1. The rectangular pulse:

$$g_{rec}(t) = \begin{cases} A & , 0 \leq t \leq T \\ 0 & , \text{otherwise} \end{cases} \quad (\text{D.1})$$

$$E_g = \int_0^T g_{rec}^2(t) dt = \int_{-\infty}^{\infty} |G_{rec}(f)|^2 df = A^2 T \quad (\text{D.2})$$



## Examples of pulse shapes: Appendix D

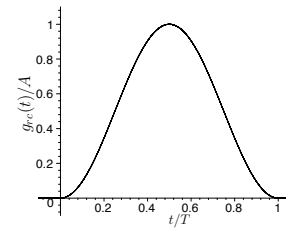


Figure D.9:  $g_{rc}(t)/A$ .

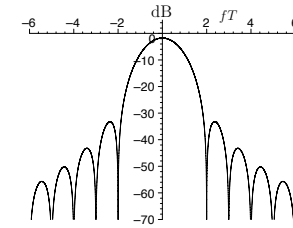


Figure D.10:  $\frac{|G_{rc}(f)|^2}{E_g T}$  in dB.

### 5. The time raised cosine pulse:

$$g_{rc}(t) = \begin{cases} \frac{A}{2} (1 - \cos(2\pi t/T)) & , 0 \leq t \leq T \\ 0 & , \text{otherwise} \end{cases} \quad (\text{D.18})$$

$$E_g = 3A^2 T / 8 \quad (\text{D.19})$$

